Please check the examination details below before entering your candidate information		
Candidate surname	Other i	names
Pearson Edexcel International GCSE	Centre Number	Candidate Number
Tuesday 21 May 2019		
Morning (Time: 2 hours)	Paper Reference	ce 4MA1/1HR
Mathematics A Level 1/2 Paper 1HR Higher Tier	\	
You must have: Ruler graduated in centimetres ar pen, HB pencil, eraser, calculator.	·	· II I

Instructions

- Use **black** ink or ball-point pen.
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer all questions.
- Without sufficient working, correct answers may be awarded no marks.
- Answer the questions in the spaces provided
 - there may be more space than you need.
- Calculators may be used.
- You must NOT write anything on the formulae page.
 Anything you write on the formulae page will gain NO credit.

Information

- The total mark for this paper is 100.
- The marks for **each** question are shown in brackets
 - use this as a guide as to how much time to spend on each question.

Advice

- Read each question carefully before you start to answer it.
- Check your answers if you have time at the end.

Turn over ▶





International GCSE Mathematics

Formulae sheet - Higher Tier

Arithmetic series

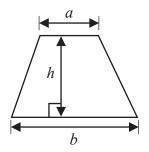
Sum to *n* terms, $S_n = \frac{n}{2} [2a + (n-1)d]$

The quadratic equation

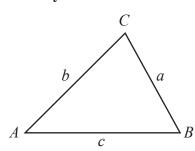
The solutions of $ax^2 + bx + c = 0$ where $a \neq 0$ are given by:

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Area of trapezium = $\frac{1}{2}(a+b)h$



Trigonometry



In any triangle ABC

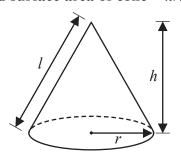
Sine Rule
$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

Cosine Rule $a^2 = b^2 + c^2 - 2bc \cos A$

Area of triangle =
$$\frac{1}{2}ab\sin C$$

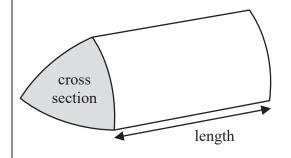
Volume of cone = $\frac{1}{3}\pi r^2 h$

Curved surface area of cone = πrl

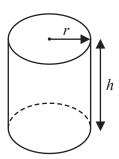


Volume of prism

= area of cross section \times length

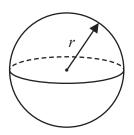


Volume of cylinder = $\pi r^2 h$ Curved surface area of cylinder = $2\pi rh$



Volume of sphere =
$$\frac{4}{3}\pi r^3$$

Surface area of sphere = $4\pi r^2$



Answer ALL TWENTY FIVE questions.

Write your answers in the spaces provided.

You must write down all the stages in your working.

1 The diagram shows a cylinder.

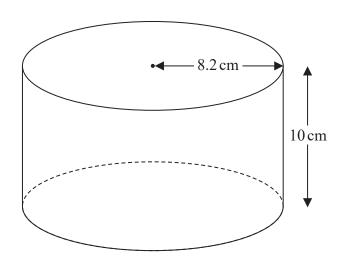


Diagram **NOT** accurately drawn

The cylinder has radius 8.2 cm and height 10 cm. The cylinder is empty.

Pam pours 1.5 litres of water into the cylinder.

Work out the depth of the water in the cylinder. Give your answer correct to 1 decimal place.

$$1.51 = 1500 \text{ mL} = 1500 \text{ cm}^3$$

Area of circle:
$$7 \times 8.2^2 = 211.24...$$
cm² base

Depth:
$$1500 \text{ cm}^3 \div 211.24... \text{ cm}^2$$
= 7.1009... cm

7·1 cm

(Total for Question 1 is 3 marks)



2 Each interior angle of a regular polygon is 162°

Work out the number of sides the polygon has.

$$18 = 360$$

 $\approx n$
 $18n = 360$
 $\frac{18}{18}$
 $n = 20$

20 sides

(Total for Question 2 is 3 marks)

- **3** \mathcal{E} = \{11, 12, 13, 14, 15, 16, 17, 18, 19, 20\}
 - $A = \{\text{even numbers}\}$
 - $B = \{\text{multiples of 3}\}\$

List the members of the set

(i)
$$A \cap B \leftarrow \text{ in List } A \text{ and } B$$

 $L > \text{ even multiple of } 3$

12,18

(ii)
$$A \cup B \leftarrow \text{in A or B}$$

Let $A \cup B \leftarrow A \cap B$

12,14, 15,16,18,20

(iii)
$$A'_-$$
 not in A
 b odd numbers

(Total for Question 3 is 3 marks)

4 Solve
$$4x - 13 = 17 + 8x$$

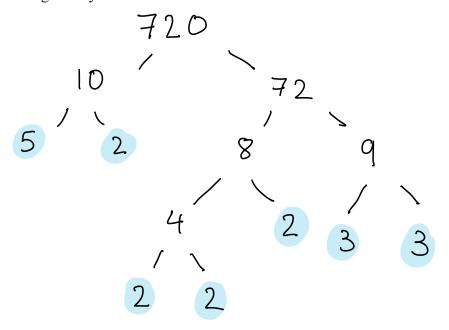
$$4x - 13 = 17 + 8x$$
 $-4x$
 $-13 = 17 + 4x$
 $-13 = 17 + 4x$
 $-17 = 17 + 18x$

$$x = -7.5$$

(Total for Question 4 is 2 marks)



5 (a) Write 720 as a product of its prime factors. Show your working clearly.



2×2×2×2×3×3×5

(b) Find the smallest whole number that 720 can be multiplied by to give a square number.

To be square, all prime factor products must be square.

$$2^4 = 16$$
 - square

 $3^2 = 9$ - square

 $5 = 5$ - not square

 $5 = 5 = 5$ - not square

 $5 = 5 = 5$ - not square

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(Total for Question 5 is 4 marks)

6 Lorenzo increases all the prices on his restaurant menu by 8%

Before the increase, the price of a dessert was \$4.25

(a) Work out the price of the dessert after the increase.

Multiplier:
$$100 + 8 = 108\%$$
 = 108 $4.25 \times 108 = 4.59$ before multiplier

\$ 4.59

After the increase, the price of lasagne is \$9.45

(b) Work out the price of lasagne before the increase.

$$x = \text{price before}$$

multiplier 1.08 $x = 9.45$
 $\frac{1.08}{x} = 8.75$

\$ 7.5

(Total for Question 6 is 6 marks)

7 The diagram shows isosceles triangle *ABC*.

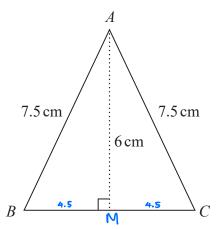


Diagram **NOT** accurately drawn

 $AB = AC = 7.5 \,\mathrm{cm}.$

The height of the triangle is 6 cm.

Pythagoras theorem : $a^2 + b^2 = c^2$

Calculate the area of the triangle.

Area =
$$\frac{1}{2}$$
 × base × height

Base:

$$BM^{2} + AM^{2} = AB^{2}$$

$$BM^{2} = AB^{2} - AM^{2}$$

$$= 7.5^{2} - 6^{2}$$

$$= 20.25$$

$$BM = 4.5$$

$$BC = 4.5 \times 2 = 9 cm$$

Area =
$$\frac{1}{2} \times 9 \times 6 = 27$$

27 cm²

(Total for Question 7 is 4 marks)



8 There are 10 people in a lift.

Work out the mean weight of the 7 people left in the lift.

$$79.2 = \frac{Total}{10}$$

$$\frac{\text{Mean: } 588}{7} =$$

84 kg

(Total for Question 8 is 3 marks)

9 (a) Simplify
$$t^9 \div t^3$$

(b) Simplify $w^5 \times w^7$

(c) Simplify $(5xy^2)^3$

$$= 5^3 \times x^3 \times y^{2\times 3}$$

(Total for Question 9 is 4 marks)



10 Change 22 metres per second to a speed in kilometres per hour. Show your working clearly.

$$\frac{22 \text{ m}}{1 \text{ sec}} \times \frac{1 \text{ km}}{1000 \text{ m}} \times \frac{1 \text{ sec}}{1 \text{ 3600}} \times \frac{22 \text{ m}}{3600} \Rightarrow \frac{3600 \text{ sec}}{79200 \text{ m}} \Rightarrow \frac{3600 \text{ sec}}{3600} \times \frac{22 \text{ m}}{3600} \Rightarrow \frac{3600 \text{ sec}}{1000 \text{ km}} \times \frac{22 \text{ m}}{1000} \times \frac{3600 \text{ sec}}{1000} \times \frac{79200 \text{ m}}{1000} \times \frac{79200 \text{ km}}{1000} \times \frac{22 \text{ m}}{1000} \times \frac{3600 \text{ sec}}{1000} \times \frac{79200 \text{ m}}{1000} \times \frac{79200 \text{ km}}{1000} \times \frac{79200 \text{ km}}{10000 \text{ km}} \times \frac{79200 \text{ km}}{100000 \text{ km}} \times \frac{79200 \text{ km}}{100000 \text{ km}} \times \frac{79200 \text{ km}}{100000 \text{ km}} \times \frac{79200 \text{ km}$$

79.2 km/h

(Total for Question 10 is 3 marks)

11 3 years ago, the ratio of Tom's age to Clemmie's age was 2 : 7 Tom is now 15 years old and Clemmie is now x years old.

Find the value of x.

(Total for Question 11 is 3 marks)



$$pressure = \frac{force}{area}$$

A box, in the shape of a cuboid, is going to be put on a table.

The whole of one face of the box will be in contact with the table. The force exerted by the box on the table is always 105 newtons.

Aneas:

The box is 5 m by 4 m by 3 m.

The greatest pressure exerted by the box on the table is $P \text{ newtons/m}^2 \ 4 \times 3 = 1000 \text{ m}^2$ The least pressure exerted by the box on the table is *Q* newtons/m²

Work out the value of P - Q

Greatest Pressure:
$$\frac{105}{\text{smallest area}} = \frac{105}{12}$$

$$= 8.75 = P$$

Least Pressure:
$$105$$
 = 105 argest area = 20 = $5.25 = Q$

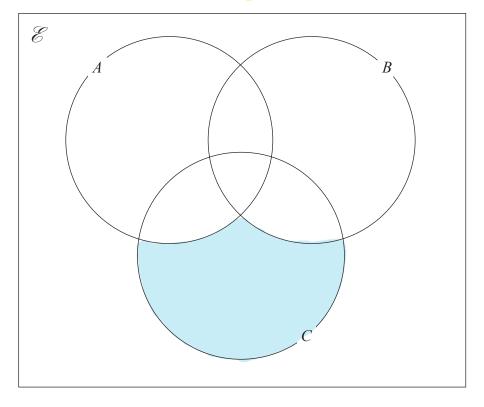
$$P - Q = 8.75 - 5.25$$

(Total for Question 12 is 3 marks)



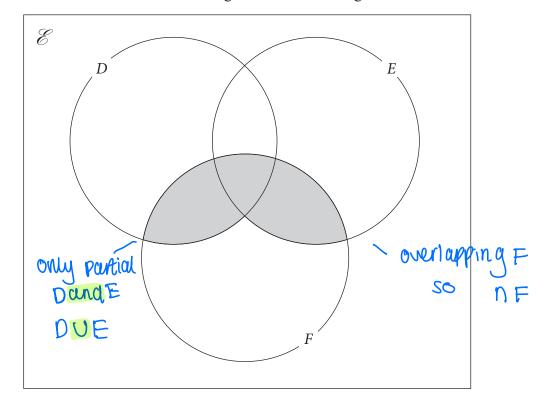
Not (A or B) and C

13 (a) On the Venn diagram, shade the set $(A \cup B)^t \cap C$



(1)

(b) Use set notation to describe the shaded region in the Venn diagram below.



(DUE) NF

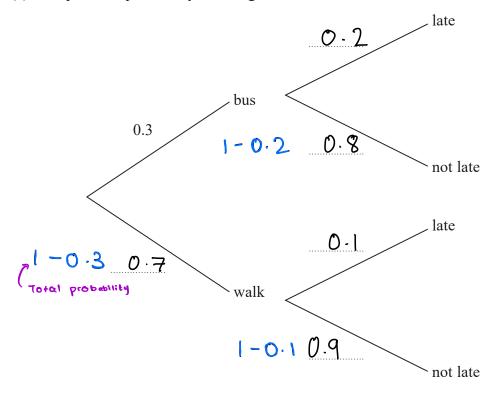
(Total for Question 13 is 2 marks)



14 Each day that Barney goes to college, he either goes by bus or he walks. The probability that Barney will go to college by bus on any day is 0.3

When Barney goes to college by bus, the probability that he will be late is 0.2 When Barney walks to college, the probability that he will be late is 0.1

(a) Complete the probability tree diagram.



(2)

Barney will go to college on 200 days next year.

(b) Work out an estimate for the number of days Barney will be late for college next year.

$$P(Late) = P(Bus \cap Late) + P(wauk \cap Late)$$

= 0.3 x 0.2 + 0.7 x 0.1
= 0.06 + 0.07 = 0.13
Number of days: 0.13 x 200 =

26

(4)

(Total for Question 14 is 6 marks)

15 The straight line L₁ has equation 2y = 6x - 5

The straight line L, is perpendicular to L, and passes through the point (9, -1)

Find an equation for L₂ Give your answer in the form ay + bx = c

L, gradient:
$$2y = 6x - 5$$

 $y = 3x - 5$ $m = 3$

$$m_1 m_2 = -1$$
 $m_2 = -1 \div m_1$
 $m_2 = -\frac{1}{3}$

Lines are perpendicular when the gradients are negative reciprocals.

Lines are perpendicular

$$y = \frac{-1}{3} \times +2$$

$$3y = -3c + 6$$

$$x + 3y = 6$$

$$3y + x = 6$$

(Total for Question 15 is 4 marks)

16 A particle *P* is moving along a straight line.

The fixed point O lies on this line.

At time t seconds, the displacement, s metres, of P from O is given by

$$s = 4t^3 - 6t^2 + 5t$$

At time t seconds, the velocity of P is v m/s.

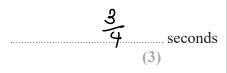
(a) Find an expression for v in terms of t.

$$V = \frac{ds}{dt} = 3 \times 4t^2 - 2 \times 6t + 5$$

$$v = 12t^2 - 12t + 5$$
 (2)

(b) Find the time at which the acceleration of the particle is 6 m/s²

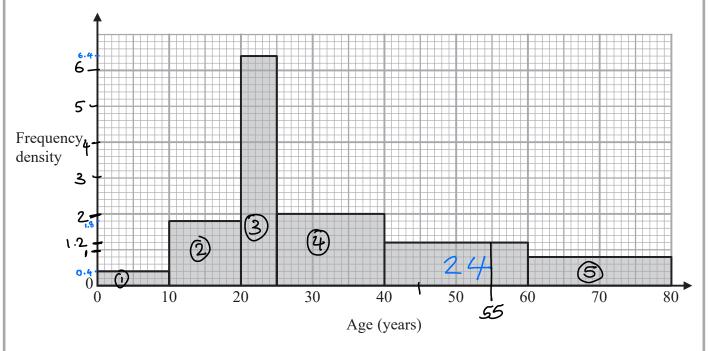
acc =
$$\frac{dv}{dt}$$
 = $2 \times 12t - 12$
= $24t - 12 = 6$
 $+12$
 $24t = 18$
 $+24$
 $t = 3$



(Total for Question 16 is 5 marks)



17 The histogram shows information about the ages of all the passengers travelling on a plane. No one on the plane is older than 80 years.



24 passengers on the plane are aged between 40 years and 60 years.

(a) Work out the total number of passengers on the plane.

Frequency = Freq density × (lass width
$$2.4 = FD \times 20$$
)

$$F = 0.4 \times 10 = 4$$

$$FD = 1.2$$

$$1.8 \times 10 = 18$$
Now draw the scale generalization

Total:

$$36.4 \times 5 = 32$$

(2)
$$1.8 \times 10 = 18$$
(3) $6.4 \times 5 = 32$
(4) $2 \times 15 = 30$
(5) $0.8 \times 20 = 16$
(7) $0.8 \times 20 = 16$
(8) Now draw the scale accordingly
Total:
$$4 + 18 + 32 + 30 + 24 + 16$$

$$= 124$$
(3)

A passenger on the plane is picked at random.

(b) Work out an estimate for the probability that this person is older than 55 years.

>55 =
$$16 + \frac{1}{4} \times 24$$

= $16 + 6 = 22$
 $P = \frac{22}{124} = \frac{11}{62}$

(Total for Question 17 is 5 marks)

18 (a) Expand and simplify (x+2)(2x+3)(x-7)Show your working clearly.

$$2x^{2}+3x+4x+6$$
 $(x-7)$
 $2x^{2}+7x+6$ $(x-7)$

$$2x^{3} - 14x^{2} + 7x^{2} - 49x + 6x - 42$$
$$2x^{3} - 7x^{2} - 43x - 42$$

(3

(b) Make m the subject of $p^2 = \frac{x+m}{2m-y}$ Solute m (2m-y)

$$2mp^{2}-p^{2}y = x + m$$

$$+p^{2}y = x + m$$

$$-m$$

$$+p^{2}y - m = x + p^{2}y - all non-m terms$$

$$+p^{2}y - m = x + p^{2}y$$

$$+(2p^{2}-1) = x + p^{2}y$$

$$+(2p^{2}-1)$$

$$M = \frac{x + p^2 y}{2p^2 - 1}$$
(3)

(Total for Question 18 is 6 marks)



19 The 25th term of an arithmetic series is 44.5

The sum of the first 30 terms of this arithmetic series is 765

Find the 16th term of the arithmetic series. Show your working clearly.

$$S_n = \frac{n}{2} (2a + (n-1)d)$$
 $a_n = a + (n-1)d$

$$0$$
 a+24d = 44.5

$$15(2a + 29d) = 765$$

$$16^{th} \text{ term} = 25^{th} - 9d$$

$$= 44.5 - 9(2)$$

$$= 26.5$$

26.5

(Total for Question 19 is 5 marks)



20 $a = 25 \times 10^{14n}$ where *n* is an integer.

Find an expression, in terms of n, for $a^{\frac{3}{2}}$. Give your answer in standard form.

$$q^{\frac{3}{2}} = (25 \times 10^{14n})^{\frac{3}{2}}$$

$$= (\sqrt{25})^{3} \times 10^{14n \times 3/2}$$

$$= 5^{3}$$

$$= 125 \times 10^{21n} - \frac{14 \times \frac{3}{2}}{2} = 1$$

$$= 1.25 \times 10^2 \times 10^{21}$$

Standard add powers
form

1.25 × 10 21n+2

(Total for Question 20 is 3 marks)

21 A curve has equation y = f(x)

There is only one maximum point on the curve.

The coordinates of this maximum point are (4, 3)

(a) Write down the coordinates of the maximum point on the curve with equation

(i)
$$y = f(x-5)$$

(5 to the right

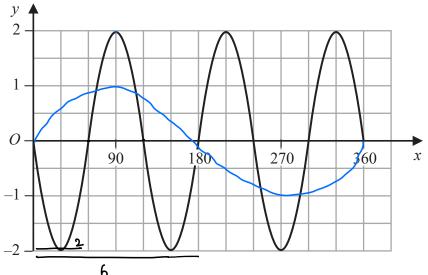
(x,y) \Longrightarrow ((x+5),y)

(____9___,__3___)

(ii)
$$y = 3f(x)$$

stretch y by 3
$$(x,y) \Rightarrow (x,3y)$$

Here is the graph of $y = a \sin(bx)^{\circ}$ for $0 \le x \le 360$



(b) Find the value of a and the value of b.

$$f(x) = \sin x$$

Looking at difference:

y values by stretched by a factor 2 and have been reflected.

(Total for Question 21 is 4 marks)

22 Solve the simultaneous equations

$$2x^2 + 3y^2 = 5$$

$$y = 2x + 1$$
2

Show clear algebraic working.

Substitute 2 into 1

$$2x^2 + 3(2x+1)(2x+1) = 5$$

$$2x^{2} + 3(4x^{2} + 2x + 2x + 1) = 5$$

$$2x^{2} + 12x^{2} + 12x + 3 = 5$$

$$-5$$

$$14x^{2} + 12x - 2 = 0$$

$$\div 2$$

$$7x^2 + 6x - 1 = 0$$

By inspection:
$$(7x-1)(x+1)=0$$

$$7x - 1 = 0$$

$$7x = 1$$

$$x = \frac{1}{7}$$

$$x = -1$$

$$z = -1$$

Subs x into
$$y = 2\left(\frac{1}{7}\right) + 1$$

$$y = 2x + 1 + 0$$

$$= \frac{9}{7}$$

$$y = 2(-1) + 1$$
 $y = -1$

$$x = -1, y = -1$$
 and $x = \frac{1}{7}, y = \frac{9}{7}$

(Total for Question 22 is 5 marks)

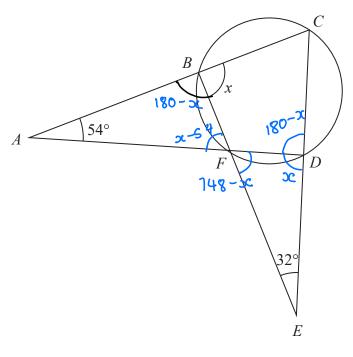


Diagram NOT accurately drawn

B, C, D and F are points on a circle. ABC, AFD, BFE and CDE are straight lines.

Work out the size of angle x. Show your working clearly.

∠ ABF = 180 - oc Angles on a straight line add to 180.

Opposite angles in a cyclic quadrilateral add to 180

$$\angle EDF = 180 - (180 - 3c)$$

$$= \infty$$

 \angle EDF = 180 - (180 - 5c) Angles on a straight line add to 180.

$$\angle DFE = 180 - 3c - 32$$
 Angles in a triangle add b
= $148 - x$

$$\angle AFB = 180 - 54 - (180 - \infty)$$
 Angles in triangle = 180°

$$x - 54 = 148 - x$$
 Vertically opposite angles are equal $2x = 202$

DC = 10)

(Total for Question 23 is 4 marks)

24

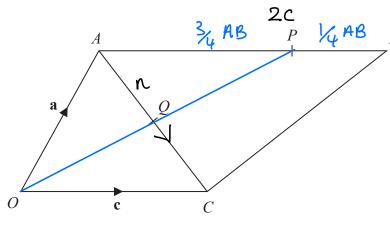


Diagram **NOT** accurately drawn

$$\overrightarrow{OA} = \mathbf{a}$$
 $\overrightarrow{OC} = \mathbf{c}$ $\overrightarrow{AB} = 2\mathbf{c}$

P is the point on AB such that AP : PB = 3 : 1Q is the point on AC such that OQP is a straight line. QP = QP = QP

Use a vector method to find \overline{AQ} : \overline{QC} Show your working clearly.

$$AC = -a + c$$
 $AP = \frac{3}{4}(2c) = \frac{3}{2}c$

$$OQ = \frac{\partial^2}{\partial a} + n(c-a) = (1-n)a + nc$$

$$OP = a + \frac{3}{2} c$$

O QP is a straight line so OQP is multiple of OQ

$$(1-n)ka + nkc = a + \frac{3}{2}c$$

Equate a and c:

(a)
$$K - nk = 1$$

(c) $nk = 3/2$
 $k = 5/6$

$$n\left(\frac{5}{2}\right) - \frac{3}{55/2} \quad \text{or} \quad x = \frac{3}{2}$$

$$n = 3/2$$

$$AQ is \frac{3}{5} \text{ of } AC$$

$$QC = \frac{2}{5}$$

$$AQ:QC = 3 \cdot 2$$

(Total for Question 24 is 5 marks)

25 A boat sails from point X to point Y and then to point Z. $a^2 = b^2 - 2bc \cos A$

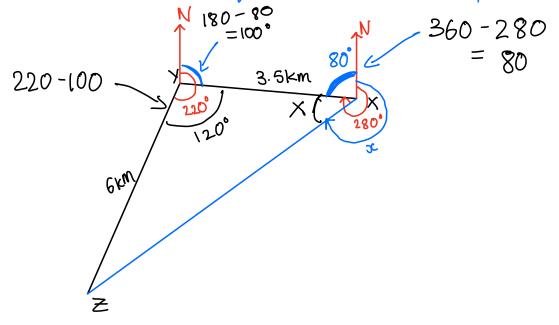
Y is on a bearing of 280° from X. Z is on a bearing of 220° from Y. SinA = SinB

The distance from X to Y is 3.5 km. The distance from Y to Z is 6 km.

Work out the bearing of Z from X.

corresponding angles. Angles around a point add uph 360°

Give your answer correct to 1 decimal place.



$$XZ^{2} = 6^{2} + 3.5^{2} - 2x6 \times 3.5 \cos 120$$

= $48.25 - (-21)$

$$X \ge^{2} = 277$$

$$\downarrow 4$$

$$X \ge = \sqrt{277}$$

$$\downarrow 2$$

$$\frac{\sin X}{6} = \frac{\sin 120}{\frac{\sqrt{277}}{2}}$$

$$Sin X = \frac{12sin 120}{\sqrt{277}}$$

 $X = 38.639.$

$$280 - 38.639...$$
= $241.36...$

Fround up

241.4

(Total for Question 25 is 5 marks)

TOTAL FOR PAPER IS 100 MARKS