## Cambridge Assessment



### Cambridge IGCSE<sup>™</sup>

CANDIDATE NAME				
CENTRE NUMBER		CANDIDATE NUMBER		
CAMBRIDGE INTERNATIONAL MATHEMATICS 0607/63				
Paper 6 Investigation and Modelling (Extended)		October/Nove	October/November 2020	

1 hour 40 minutes

You must answer on the question paper.

No additional materials are needed.

#### INSTRUCTIONS

- Answer both part A (Questions 1 to 4) and part B (Questions 5 to 8).
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do **not** use an erasable pen or correction fluid.
- Do **not** write on any bar codes.
- You should use a graphic display calculator where appropriate.
- You may use tracing paper.
- You must show all necessary working clearly, including sketches, to gain full marks for correct methods.
- In this paper you will be awarded marks for providing full reasons, examples and steps in your working to communicate your mathematics clearly and precisely.

#### INFORMATION

- The total mark for this paper is 60.
- The number of marks for each question or part question is shown in brackets [].



#### A INVESTIGATION (QUESTIONS 1 TO 4)

#### AREAS OF POLYGONS INSIDE AND OUTSIDE A CIRCLE (30 marks)

You are advised to spend no more than 50 minutes on this part.

This investigation looks at the areas of polygons drawn inside and outside a circle of radius 10 cm.

An inscribed polygon is a polygon in which all the vertices lie on a circle. This is an inscribed square.



A circumscribed polygon is a polygon in which each side is a tangent to a circle. This is a circumscribed square.



You may find some of these formulas useful.  
Area, A, of circle, radius 
$$r$$
  $A = \pi r^2$   
Area, A, of triangle, base b, height  $h$   $A = \frac{1}{2}bh$   
In a right-angled triangle,  
 $\sin \theta = \frac{\text{opposite}}{\text{hypotenuse}},$   
 $\cos \theta = \frac{\text{adjacent}}{\text{hypotenuse}},$   
 $\tan \theta = \frac{\text{opposite}}{\text{adjacent}}.$ 

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A square circumscribes a circle, centre *O*, radius 10 cm.

Work out the area of the square.





A regular hexagon is inscribed in a circle, centre O, radius 10 cm.

Find the area of the hexagon.

.....[3]



(b) (i)



6

An equilateral triangle has height 10 cm.

Find the area of the triangle.





A regular hexagon circumscribes a circle, centre O, radius 10 cm.

Using your answer to **part (i)**, find the area of the hexagon.

www.mymainscloud.com (c) (i) Use Question 1(c), Question 2(a) and Question 2(b)(ii) to complete the inequality.

7

#### $\ldots$ < $\pi$ < $\ldots$ [1]

(ii) Give a geometric reason why the range in the inequality in Question 2(c)(i) is smaller than the range in the inequality in **Question 1(d)**.

..... ......[1]



A regular 12-sided polygon is inscribed in a circle, centre *O*, radius 10 cm. Find the area of this polygon.

.....[2]



A regular 12-sided polygon circumscribes a circle, centre *O*, radius 10 cm. Find the area of this polygon.

.....[3]

(c) Use the answers to part (a) and part (b) to complete the inequality.

www.mymainscloud.com (a) (i) Show that a formula for the area,  $A \operatorname{cm}^2$ , of a regular polygon with *n* sides inscribed in a 4 circle, radius 10 cm, is

 $A = 50n \sin\left(\frac{360}{n}\right)^\circ.$ 

[2]

[2]

(ii) Show that a formula for the area,  $B \text{ cm}^2$ , of a regular polygon with *n* sides that **circumscribes** a circle, radius 10 cm, is

$$B = 100n \tan\left(\frac{180}{n}\right)^\circ.$$

www.mymathscloud.com 11 Work out the area of a regular polygon with 100 sides that is inscribed in a circle, radius 10 cm (b) (i) Give your answer correct to 4 significant figures. Work out the area of a regular polygon with 100 sides that circumscribes a circle, (ii) radius 10 cm. Give your answer correct to 4 significant figures. (c) Use your answers to part (b) to explain how you can find the value of  $\pi$  correct to 3 significant figures.

.....[1]



#### **B** MODELLING (QUESTIONS 5 TO 8)

#### MODELLING CONTAINERS (30 marks)

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You are advised to spend no more than 50 minutes on this part.

Olivia wants to design a closed container with a volume of 1000 cm<sup>3</sup> and minimum surface area.

5 Olivia uses a square-based cuboid to model the container.



(a) (i) Write down a formula for the volume of the cuboid,  $V \text{ cm}^3$ , in terms of x and h.

......[1]

(ii) Find a formula for the surface area,  $S \text{ cm}^2$ , of the cuboid, in terms of x and h. Give your answer in its simplest form.

......[2]

**(b)** (i) V = 1000.

Write h in terms of x.

......[1]

(ii) Show that 
$$S = 2x^2 + \frac{4000}{x}$$
.



[Turn over

		`	1
	Volume, V, of a cylinder of radius r, height h	$V = \pi r^2 h$	
	Curved surface area, $A$ , of a cylinder of radius $r$ , height $h$	$A = 2\pi rh$	
< · · ·			/

Olivia now uses a cylinder to model the container.



The total surface area of this model is  $T \text{ cm}^2$ .

(a) V = 1000.

Show that  $T = 2\pi r^2 + \frac{2000}{r}$ .

[3]

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(b) (i) Find the minimum surface area of the cylinder.

.....[2]

14

6



*r* = .....  $h = \dots [2]$ 

# Volume, *V*, of a pyramid, base area *A*, height *h* $V = \frac{1}{3}Ah$

Olivia now uses a square-based pyramid to model the container.

7



The pyramid, OABCD, has a square base of side x cm and height h cm. The vertex of the pyramid, O, is directly above the centre of the square base. E is the mid-point of BC.

(a) Find an expression for *OE* in terms of *h* and *x*.

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(b) The total surface area of this model is  $P \text{ cm}^2$ .

V = 1000.Show that  $P = x^2 + \frac{\sqrt{x^6 + 36000000}}{x}$ 

[4]



.....[2]

(ii) Find the dimensions of the pyramid with the minimum surface area.

18

 $x = \dots$  $h = \dots$  [2]

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	19
8	Olivia recommends the container with the smallest surface area to a company.
	Give a geometric reason why the company might not accept Olivia's recommendation.
	Olivia recommends the
	Geometric reason



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