

**Cambridge Assessment International Education** Cambridge International General Certificate of Secondary Education

	CANDIDATE NAME		
	CENTRE NUMBER	CANDIDATE NUMBER	
*		0607/52	
л <b></b>	Paper 5 (Core)		May/June 2019
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N			1 hour
ω	Candidates ans		
7566243408*	Additional Mate	rials: Graphics Calculator	
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## **READ THESE INSTRUCTIONS FIRST**

Write your centre number, candidate number and name on all the work you hand in.

Write in dark blue or black pen.

Do not use staples, paper clips, glue or correction fluid.

You may use an HB pencil for any diagrams or graphs.

DO NOT WRITE IN ANY BARCODES.

Answer all the questions.

You must show all relevant working to gain full marks for correct methods, including sketches.

In this paper you will also be assessed on your ability to provide full reasons and communicate your mathematics clearly and precisely.

At the end of the examination, fasten all your work securely together.

The total number of marks for this paper is 24.

This document consists of 8 printed pages.

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Answer **all** the questions.

## SQUARE ROOTS WITHIN SQUARE ROOTS

This investigation looks at sequences of terms with square roots.

You can form a sequence by using square roots within square roots.

$$\sqrt{6}, \sqrt{6+\sqrt{6}}, \sqrt{6+\sqrt{6}+\sqrt{6}}, \sqrt{6+\sqrt{6}+\sqrt{6}}, \dots$$

You can calculate the first four terms of this sequence as follows.

$$\sqrt{6} = 2.4494...$$

$$\sqrt{6+\sqrt{6}} = \sqrt{6+2.4494...} = \sqrt{8.4494...} = 2.9068...$$

$$\sqrt{6+\sqrt{6+\sqrt{6}}} = \sqrt{6+2.9068...} = \sqrt{8.9068...} = 2.9844...$$

$$\sqrt{6+\sqrt{6+\sqrt{6+\sqrt{6}}}} = \sqrt{6+2.9844...} = \sqrt{8.9844...} = 2.9974...$$

1 (a) Complete each part of the calculation below to work out the next term of the sequence, writing each decimal as far as the 4th decimal place.

$$\sqrt{6 + \sqrt{6 + \sqrt{6 + \sqrt{6} + \sqrt{6}}}} = \sqrt{6 + \dots = \sqrt{\dots}} = \dots$$

(b) As the sequence continues, the terms get closer and closer to an integer. This integer is the *integer limit* of the sequence.

Write down the integer limit of this sequence.

.....



2 Here is a similar sequence of square roots.

 $\sqrt{30}, \sqrt{30+\sqrt{30}}, \sqrt{30+\sqrt{30+\sqrt{30}}}, \sqrt{30+\sqrt{30+\sqrt{30}}}, \dots$ 

(a) Calculate the first three terms, writing each decimal as far as the 4th decimal place.

3

.....

(b) Write down the integer limit of this sequence.



3 (a) Complete this table for sequences similar to those in question 1(a) and question 2.

1 <sup>st</sup> term	Integer limit
$\sqrt{2}$	
$\sqrt{6}$	
√ <u>12</u>	4
$\sqrt{20}$	
$\sqrt{30}$	
$\sqrt{42}$	7

(b) (i) Use part (a) to find the first term of the sequence that has an integer limit of 8.

.....

(ii) Calculate the 2nd term of the sequence in **part** (i), writing the decimal as far as the 4th decimal place.

.....



5

For such sequences, k = N(N-a), where *a* is a constant.

(a) Use the last row of the table in question 3(a) to find the value of a.

.....

(b) Use k = N(N-a) to show that

$$\sqrt{90}$$
,  $\sqrt{90 + \sqrt{90}}$ ,  $\sqrt{90 + \sqrt{90 + \sqrt{90}}}$ ,  $\sqrt{90 + \sqrt{90 + \sqrt{90}}}$ , ...

has an integer limit of N = 10.

(c) Find the first three terms, in square root form, of the sequence that has an integer limit of N = 26.

······ , ····· , ·····

5 Here is the general form of another sequence of square roots with integer limit *N*.

$$\sqrt{k}$$
,  $\sqrt{k+2\sqrt{k}}$ ,  $\sqrt{k+2\sqrt{k+2\sqrt{k}}}$ ,  $\sqrt{k+2\sqrt{k+2\sqrt{k}}}$ , ...

For such sequences, k = N(N-a), where *a* is a constant.

When k = 24 the integer limit of the sequence is N = 6.

(a) Find the value of the constant *a*.

(b) (i) Find the value of k when the integer limit is N = 5.

(ii) Write down the 3rd term of the sequence in part (i) in square root form.

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(iii) Calculate the 3rd term, writing the decimal as far as the 4th decimal place.

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6 Here is the general form of another sequence of square roots with integer limit *N*.

$$\sqrt{k}$$
,  $\sqrt{k+5\sqrt{k}}$ ,  $\sqrt{k+5\sqrt{k+5\sqrt{k}}}$ ,  $\sqrt{k+5\sqrt{k+5\sqrt{k}}}$ , ...

For this sequence, k = N(N-a), where *a* is a constant.

The sequence  $\sqrt{14}$ ,  $\sqrt{14+5\sqrt{14}}$ ,  $\sqrt{14+5\sqrt{14}}$ ,  $\sqrt{14+5\sqrt{14}+5\sqrt{14}}$ ,  $\sqrt{14+5\sqrt{14+5\sqrt{14}}}$ , ... has an integer limit of N = 7.

Find the value of the constant *a*.

.....

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Question 7 is printed on the next page.



7 Here is the general sequence with integer limit *N*.

$$\sqrt{k}$$
,  $\sqrt{k+x\sqrt{k}}$ ,  $\sqrt{k+x\sqrt{k+x\sqrt{k}}}$ ,  $\sqrt{k+x\sqrt{k+x\sqrt{k}}}$ , ...

For all such sequences, k = N(N-a), where *a* is a constant that depends on the value of *x*.

## (a) (i) Use question 4, question 5 and question 6 to complete the table.

	x	а
Question 4	1	
Question 5		
Question 6	5	

(ii) Write down an expression for k in terms of N and x.

.....

(b) Find the integer limit, N, of this sequence.

 $\sqrt{7}, \sqrt{7+6\sqrt{7}}, \sqrt{7+6\sqrt{7+6\sqrt{7}}}, \sqrt{7+6\sqrt{7+6\sqrt{7}}}, \dots$ 

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