

	VERSITY OF CAMBRIDGE INTER rnational General Certificate of Sec	NATIONAL EXAMINATIONS ondary Education	WW. MY MATHS
NAME			
CENTRE NUMBER		CANDIDATE NUMBER	
MATHEMATICS			0580/41
Paper 4 (Extended)		October	November 2010
		2 h	ours 30 minutes
Candidates answer of	on the Question Paper.		
Additional Materials:	Electronic calculator Mathematical tables (optional)	Geometrical instruments Tracing paper (optional)	

### **READ THESE INSTRUCTIONS FIRST**

Write your Centre number, candidate number and name on all the work you hand in. Write in dark blue or black pen. You may use a pencil for any diagrams or graphs. Do not use staples, paper clips, highlighters, glue or correction fluid. DO NOT WRITE IN ANY BARCODES.

Answer all questions.

If working is needed for any question it must be shown below that question.

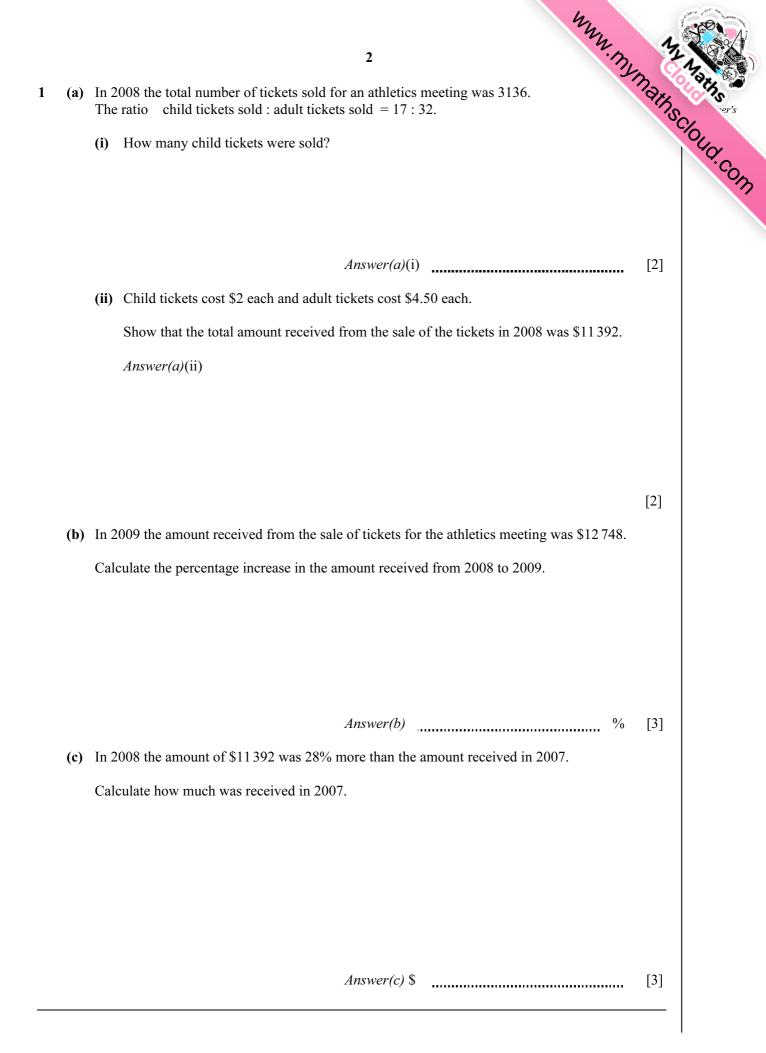
Electronic calculators should be used.

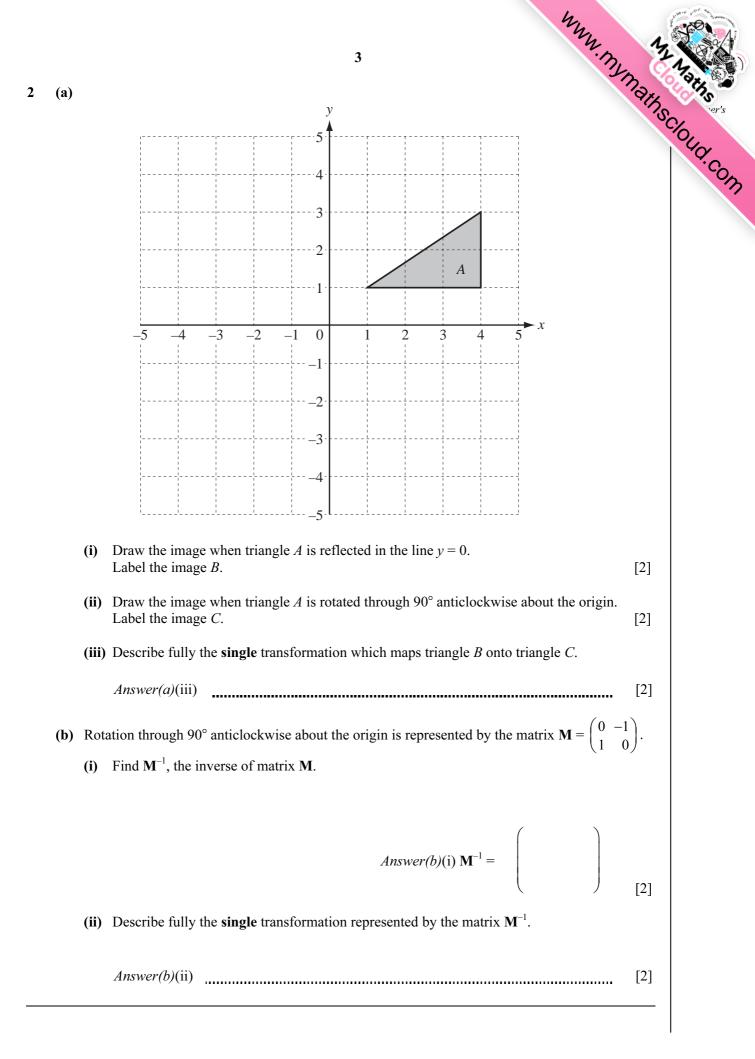
If the degree of accuracy is not specified in the question, and if the answer is not exact, give the answer to three significant figures. Give answers in degrees to one decimal place. For  $\pi$  use either your calculator value or 3.142.

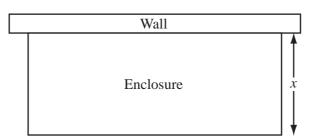
At the end of the examination, fasten all your work securely together. The number of marks is given in brackets [] at the end of each question or part question. The total of the marks for this paper is 130.

This document consists of 16 printed pages.









NOT TO SCALE

A farmer makes a rectangular enclosure for his animals.

He uses a wall for one side and a total of 72 metres of fencing for the other three sides.

The enclosure has width x metres and area A square metres.

(a) Show that  $A = 72x - 2x^2$ .

Answer (a)

**(b)** Factorise completely  $72x - 2x^2$ .

# Answer(b) [2]

(c) Complete the table for  $A = 72x - 2x^2$ .

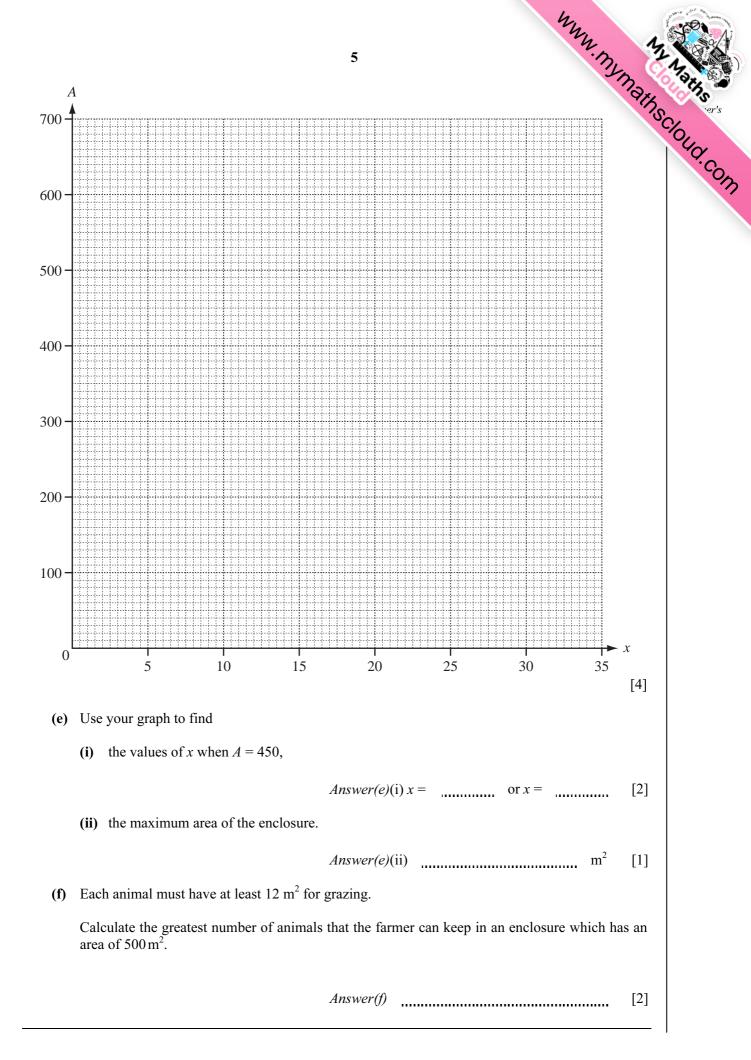
x	0	5	10	15	20	25	30	35
A	0	310	520			550	360	

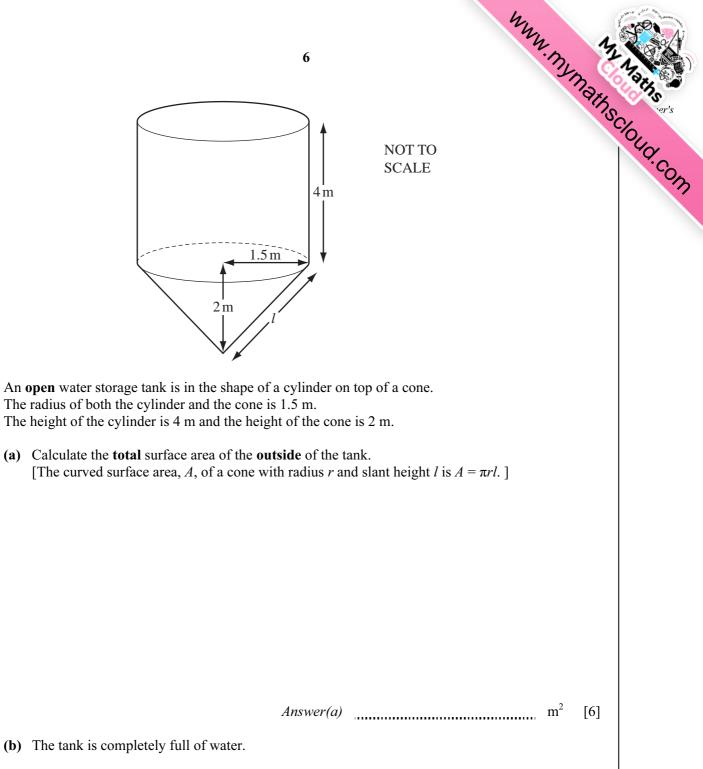
[3]

[2]

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(d) Draw the graph of  $A = 72x - 2x^2$  for  $0 \le x \le 35$  on the grid opposite.



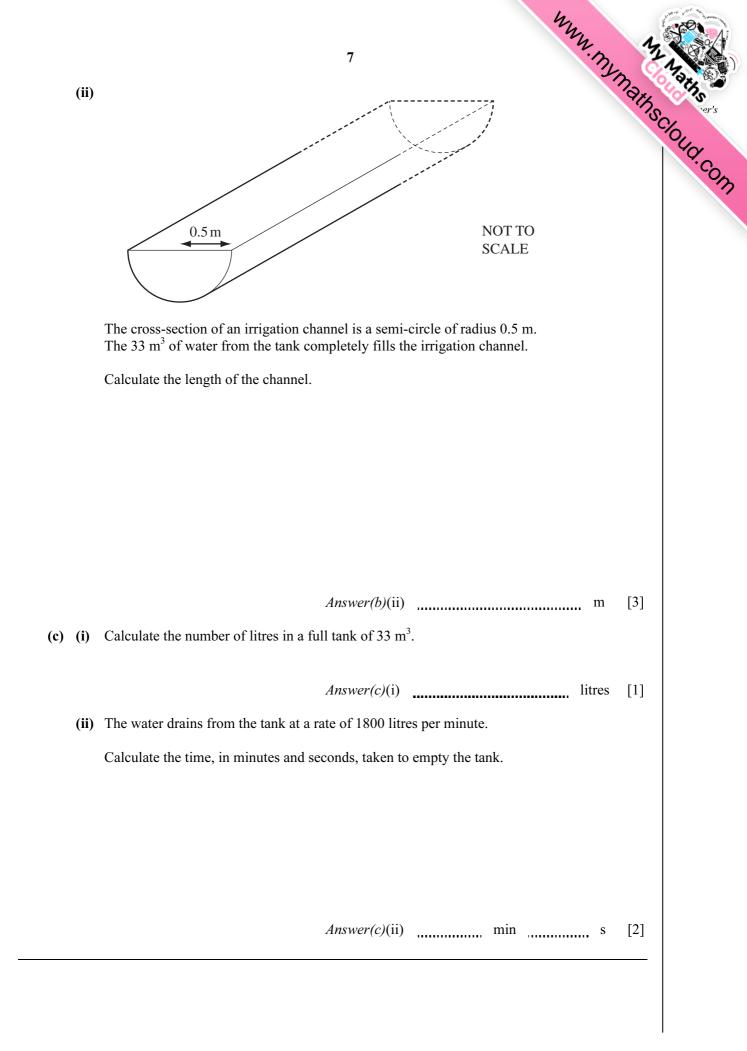


(i) Calculate the volume of water in the tank and show that it rounds to 33 m<sup>3</sup>, correct to the nearest whole number.

[The volume, V, of a cone with radius r and height h is  $V = \frac{1}{3}\pi r^2 h$ .]

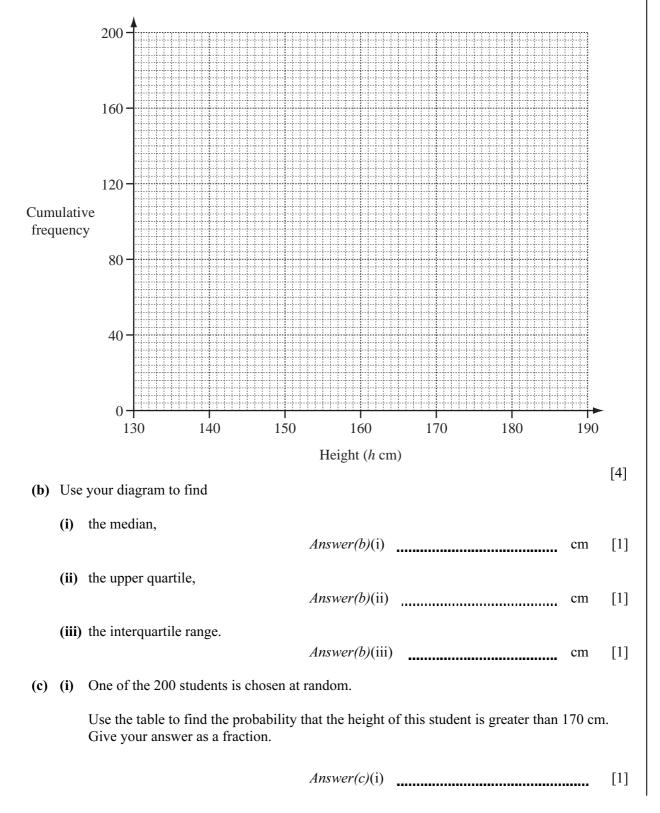
Answer(b)(i)

[4]



- MMM. MYMathscioud.com Height (h cm) ≤130 ≤140 ≤150 ≤160 ≤165 ≤170 ≤180 Cumulative frequency 0 10 50 95 115 145 180
- 5 The cumulative frequency table shows the distribution of heights, h centimetres, of 200 students

(a) Draw a cumulative frequency diagram to show the information in the table.



(ii) One of the 200 students is chosen at random and then a second student is chosen at ra. from the remaining students.

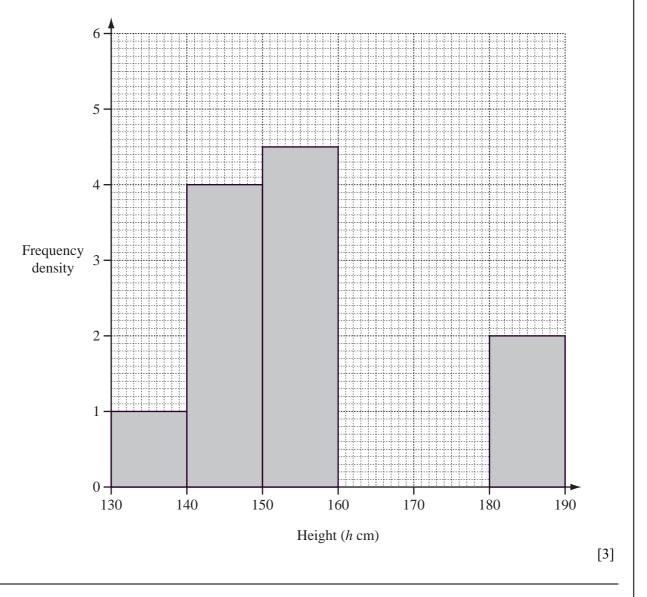
MMM. Mymathscious. 29's Calculate the probability that one has a height greater than 170 cm and the other has a height of 140 cm or less. Give your answer as a fraction.

#### Answer(c)(ii) [3]

Complete this frequency table which shows the distribution of the heights of the 200 (d) (i) students.

Height (h cm)	130< <i>h</i> ≤140	140< <i>h</i> ≤150	150< <i>h</i> ≤160	160< <i>h</i> ≤165	165< <i>h</i> ≤170	170< <i>h</i> ≤180	180< <i>h</i> ≤190
Frequency	10	40	45	20			

## (ii) Complete this histogram to show the distribution of the heights of the 200 students.



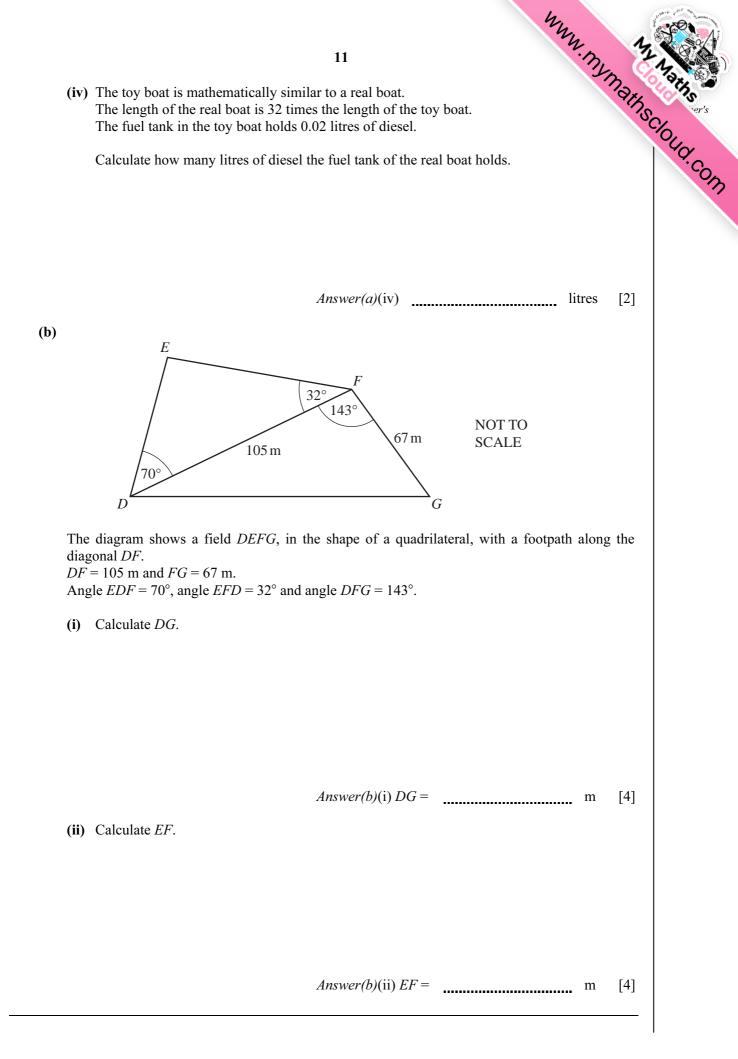
[2]

MMM. Mymathscious. er's 10 6 **(a)** A NOT TO 19.5 cm 16.5 cm **SCALE** 11 cm Q R B С The diagram shows a toy boat. AC = 16.5 cm, AB = 19.5 cm and PR = 11 cm. Triangles *ABC* and *PQR* are **similar**. (i) Calculate PQ. Answer(a)(i) PQ = cm [2] (ii) Calculate BC.

Answer(a)(ii) BC = cm [3]

(iii) Calculate angle ABC.

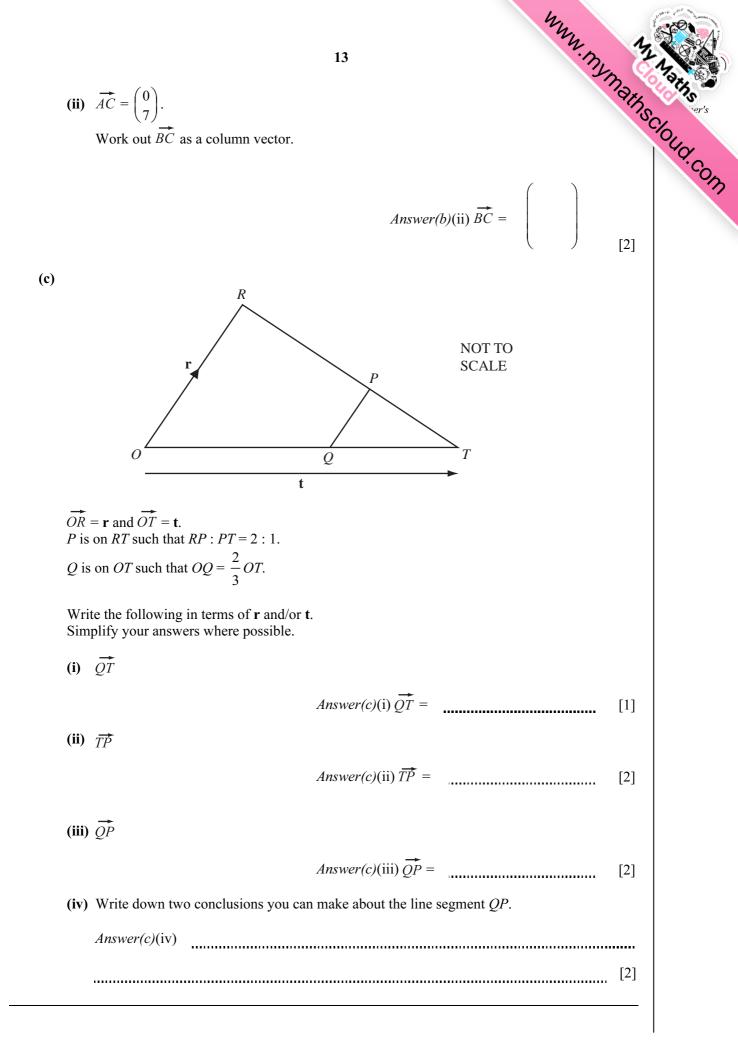
Answer(a)(iii) Angle ABC =[2]



MMM. MYMathscious ser's 12 **(a)** A V NOT TO SCALE В D 62° w 0 Z С A, B, C and D are points on the circumference of a circle centre O. AC is a diameter. BD = BC and angle  $DBC = 62^{\circ}$ . Work out the values of *w*, *x*, *y* and *z*. Give a reason for each of your answers. w =because [2] ..... x =[2] because ..... ..... *y* = [2] because ..... [2] Z =because ..... **(b)** y • *B* (4,4) NOT TO SCALE • A (2,1) **x** 0

(i) Write down  $\overrightarrow{AB}$  as a column vector.

Answer(b)(i) 
$$\overrightarrow{AB} =$$
 [1]



8	(a)	f(x) = 2x - 1	$g(x) = x^2$	14 Winny	III
		Work out			SCIO ver's
		(i) f(2),		Answer(a)(i)	[1]
		(ii) g(-2),		Answer(a)(ii)	[1]
		(iii) ff(x) in its simple	est form,		
		(iv) $f^{-1}(x)$ , the invers	se of $f(x)$ ,	Answer(a)(iii) ff(x) =	[2]
		(v) $x$ when $gf(x) = 4$	4.	Answer(a)(iv) $f^{-1}(x) =$	[2]
	(b)	<i>y</i> is <b>inversely</b> proport Find,		or $x =$	[4]
		(i) an equation conn	ecting <i>y</i> and <i>x</i> ,		
		(ii) <i>y</i> when $x = \frac{1}{2}$ .		Answer(b)(i)	[2]
				Answer(b)(ii) $y =$	[1]
					I

9	(a)	The first five terms P	1, P <sub>2</sub> ,	P <sub>3</sub> , P	$_4$ and P <sub>5</sub> c	of a sequence are	e given below.
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1	$= 1 = P_1$
1 + 2	$= 3 = P_2$
1 + 2 + 3	$= 6 = P_3$
1 + 2 + 3 + 4	$= 10 = P_4$
1 + 2 + 3 + 4 + 5	$= 15 = P_5$

(i) Write down the next term,  $P_6$ , in the sequence 1, 3, 6, 10, 15...

Answer(a)(i) [1]

(ii) The formula for the *n*th term of this sequence is

$$\mathbf{P}_n = \frac{1}{2}n(n+1).$$

Show this formula is true when n = 6.

Answer (a)(ii)

(iii) Use the formula to find  $P_{50}$ , the 50th term of this sequence.

(iv) Use your answer to part (iii) to find  $3 + 6 + 9 + 12 + 15 + \dots + 150$ . [1]

Answer(a)(iv) [1]

(v) Find  $1 + 2 + 3 + 4 + 5 + \dots + 150$ .

Answer(a)(v)[1]

(vi) Use your answers to **parts** (iv) and (v) to find the sum of the numbers less than 150 which are **not** multiples of 3.

Answer(a)(vi) [1]

### This question continues on the next page.

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[1]

MMM. Mymathscious. (b) The first five terms,  $S_1$ ,  $S_2$ ,  $S_3$ ,  $S_4$  and  $S_5$  of a different sequence are given below.

 $(1 \times 1)$  $= 1 = S_1$  $(1 \times 2) + (2 \times 1)$  $= 4 = S_2$  $(1 \times 3) + (2 \times 2) + (3 \times 1)$  $= 10 = S_3$  $(1 \times 4) + (2 \times 3) + (3 \times 2) + (4 \times 1)$  $= 20 = S_4$  $(1 \times 5) + (2 \times 4) + (3 \times 3) + (4 \times 2) + (5 \times 1) = 35 = S_5$ 

(i) Work out the next term,  $S_6$ , in the sequence 1, 4, 10, 20, 35...

Answer(b)(i) [2]

(ii) The formula for the *n*th term of this sequence is

$$S_n = \frac{1}{6}n(n+1)(n+2).$$

Show this formula is true for n = 6.

Answer(b)(ii)

(iii) Find  $(1 \times 20) + (2 \times 19) + (3 \times 18) \dots + (20 \times 1)$ .

Answer(b)(iii) [1]

(c) Show that  $S_6 - S_5 = P_6$ , where  $P_6$  is your answer to part (a)(i).

Answer(c)

(d) Show by algebra that 
$$S_n - S_{n-1} = P_n$$
.  $[P_n = \frac{1}{2}n(n+1)]$   
Answer(d)

[1]

[1]

<sup>[3]</sup> 

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