

**Cambridge International Examinations** Cambridge International General Certificate of Secondary Education

CANDIDATE NAME						
 CENTRE NUMBER	CANDIDATE					
MATHEMATICS	3	0580/41				
Paper 4 (Extend	ded)	May/June 2016				
		2 hours 30 minutes				
Candidates answ	wer on the Question Paper.					
Additional Mater	rials: Electronic calculator Geometrical instrume Tracing paper (optional).	nts				

## READ THESE INSTRUCTIONS FIRST

Write your Centre number, candidate number and name on all the work you hand in.

Write in dark blue or black pen.

You may use an HB pencil for any diagrams or graphs.

Do not use staples, paper clips, glue or correction fluid.

DO NOT WRITE IN ANY BARCODES.

Answer all questions.

If working is needed for any question it must be shown below that question.

Electronic calculators should be used.

If the degree of accuracy is not specified in the question, and if the answer is not exact, give the answer to three significant figures. Give answers in degrees to one decimal place.

For  $\pi$ , use either your calculator value or 3.142.

At the end of the examination, fasten all your work securely together.

The number of marks is given in brackets [] at the end of each question or part question. The total of the marks for this paper is 130.

The syllabus is approved for use in England, Wales and Northern Ireland as a Cambridge International Level 1/Level 2 Certificate.

This document consists of **19** printed pages and **1** blank page.



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- 1 (a) Kristian and Stephanie share some money in the ratio 3 : 2. Kristian receives \$72.
  - (i) Work out how much Stephanie receives.

\$		[2]	]
----	--	-----	---

(ii) Kristian spends 45% of his \$72 on a computer game.

Calculate the price of the computer game.

\$ .....[1]

(iii) Kristian also buys a meal for \$8.40.

Calculate the fraction of the \$72 Kristian has left after buying the computer game and the meal. Give your answer in its lowest terms.

.....[2]

(iv) Stephanie buys a book in a sale for \$19.20. This sale price is after a reduction of 20%.

Calculate the original price of the book.

\$ .....[3]

(b) Boris invests \$550 at a rate of 2% per year simple interest.

Calculate the amount Boris has after 10 years.

\$ .....[3]

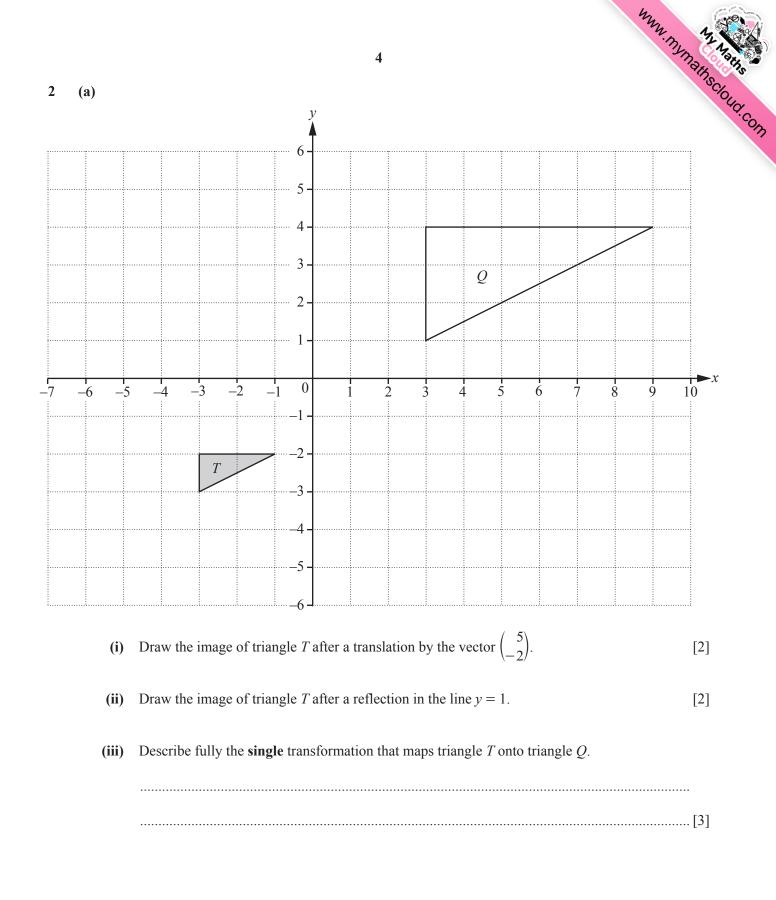
(c) Marlene invests \$550 at a rate of 1.9% per year compound interest.

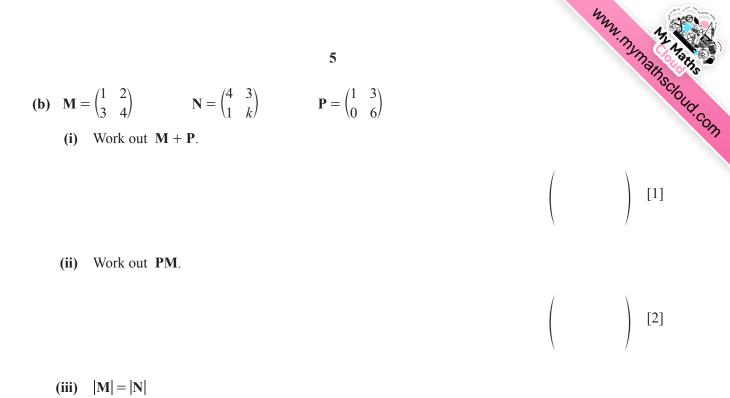
Calculate the amount Marlene has after 10 years.

\$ .....[2]

(d) Hans invests \$550 at a rate of x% per year compound interest.At the end of 10 years he has a total amount of \$638.30, correct to the nearest cent.

Find the value of *x*.





Find the value of *k*.

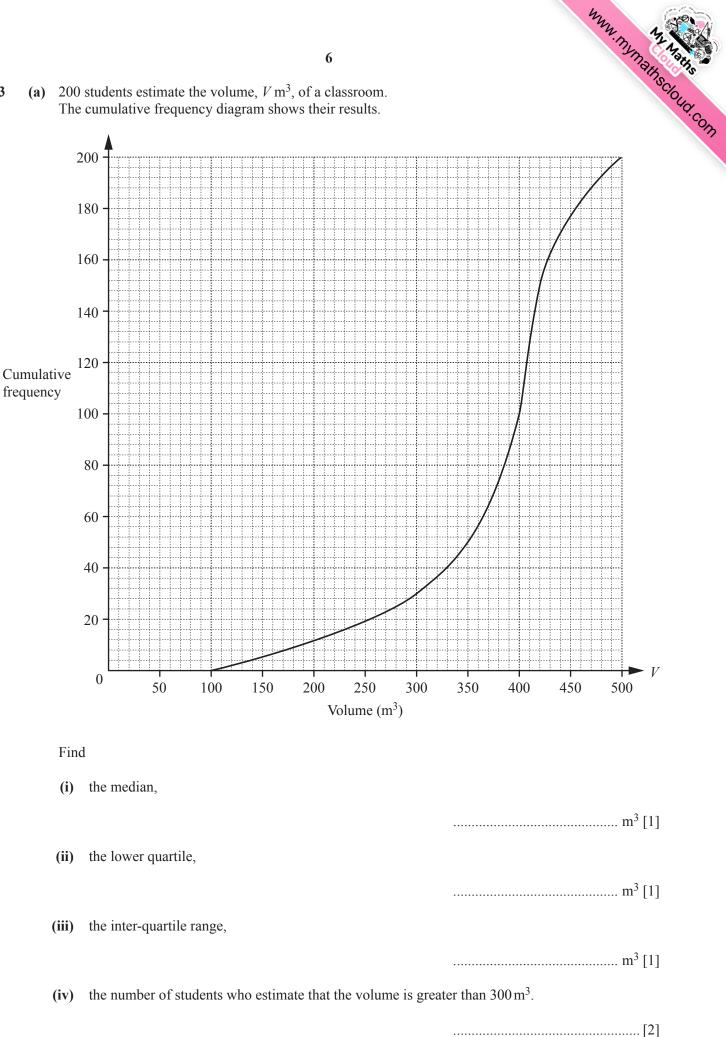
*k* = .....[3]

(c) (i) Describe fully the single transformation represented by the matrix  $\begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix}$ .

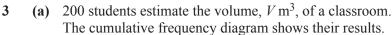
.....[3]

(ii) Find the matrix which represents a reflection in the line y = x.

[2]



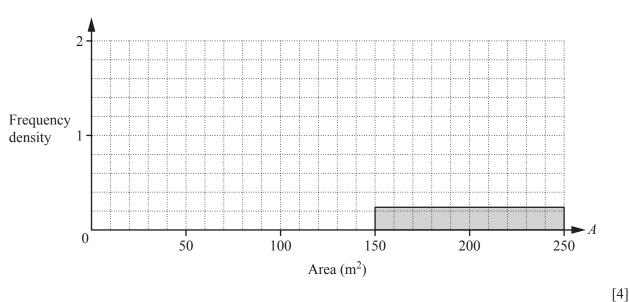
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	7 200 students also estimate the total area, $A \mathrm{m}^2$ , of the windows in the classroom. results are shown in the table.						
Area $(A \mathrm{m}^2)$	$20 < A \le 60$	$60 < A \le 100$	$100 < A \le 150$	$150 < A \le 250$			
Frequency	32	64	80	24			

Calculate an estimate of the mean. (i) Show all your working.

..... m<sup>2</sup> [4]



(ii) Complete the histogram to show the information in the table.

## (iii) Two of the 200 students are chosen at random.

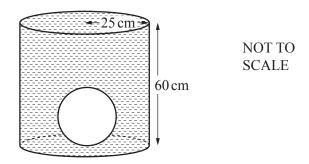
Find the probability that they both estimate that the area is greater than  $100 \text{ m}^2$ .

.....[2]

8

[2]

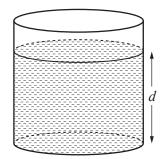
(b) (i) The sphere is placed inside an empty cylindrical tank of radius 25 cm and height 60 cm. The tank is filled with water.



Calculate the volume of water required to fill the tank.

..... cm<sup>3</sup> [3]

The sphere is removed from the tank. (ii)



NOT TO SCALE

Calculate the depth, *d*, of water in the tank.

*d* = ..... cm [2]



- (c) The sphere is melted down and the metal is made into a solid cone of height 54 cm.
  - (i) Calculate the radius of the cone. [The volume, V, of a cone with radius r and height h is  $V = \frac{1}{3}\pi r^2 h$ .]

..... cm [3]

(ii) Calculate the total surface area of the cone. [The curved surface area, A, of a cone with radius r and slant height l is  $A = \pi r l$ .]

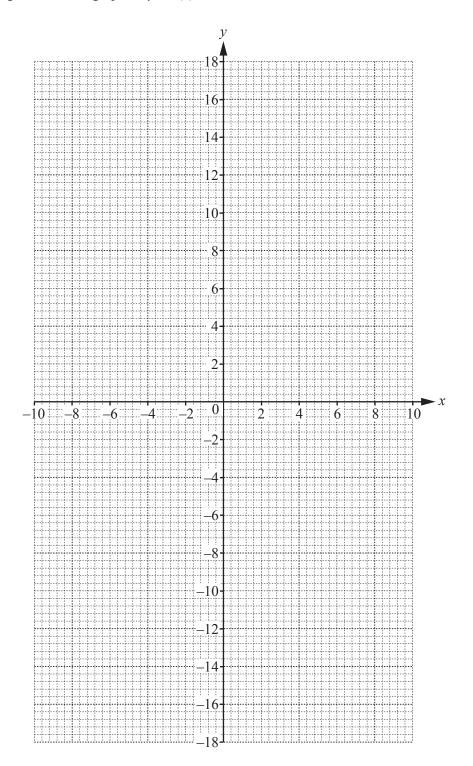
5 
$$f(x) = \frac{20}{x} + x, \quad x \neq 0$$

(a) Complete the table.

x	-10	-8	-5	-2	-1.6	1.6	2	5	8	10
f( <i>x</i> )	-12	-10.5	-9	-12	-14.1	14.1	12			12

10

(b) On the grid, draw the graph of y = f(x) for  $-10 \le x \le -1.6$  and  $1.6 \le x \le 10$ .



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[2]

- (c) Using your graph, solve the equation f(x) = 11.
- (d) k is a prime number and f(x) = k has no solutions.Find the possible values of k.

(e) The gradient of the graph of y = f(x) at the point (2, 12) is -4.Write down the co-ordinates of the other point on the graph of y = f(x) where the gradient is -4.

(.....)[1]

.....[2]

 $x = \dots$  or  $x = \dots$  [2]

(f) (i) The equation  $f(x) = x^2$  can be written as  $x^3 + px^2 + q = 0$ . Show that p = -1 and q = -20.

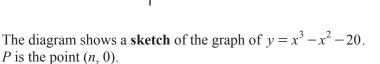
[2]

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(ii) On the grid opposite, draw the graph of 
$$y = x^2$$
 for  $-4 \le x \le 4$ . [2]

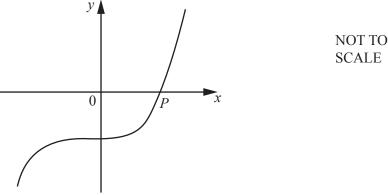
(iii) Using your graphs, solve the equation  $x^3 - x^2 - 20 = 0$ .

(iv)



Write down the value of *n*.

<i>n</i> =	[1]
[Turn	over



0580/41/M/J/16



[3]

The perimeter of the rectangle is 80 cm. The area of the rectangle is  $A \text{ cm}^2$ .

(i) Show that  $x^2 - 40x + A = 0$ .

(ii) When A = 300, solve, by factorising, the equation  $x^2 - 40x + A = 0$ .

12

xcm

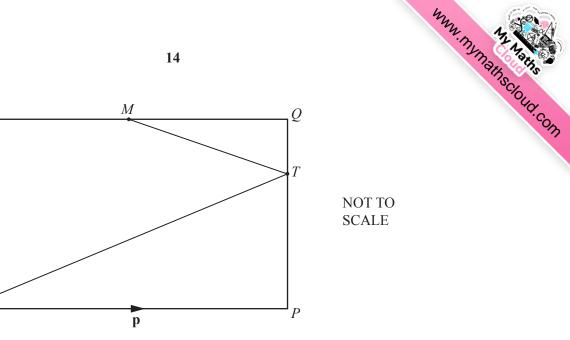
(iii) When A = 200, solve, by using the quadratic formula, the equation  $x^2 - 40x + A = 0$ . Show all your working and give your answers correct to 2 decimal places.

 $x = \dots$  or  $x = \dots$ [4]

- (b) A car completes a 200 km journey with an average speed of x km/h. The car completes the return journey of 200 km with an average speed of (x + 10) km/h.
- www.mymathscloud.com Show that the difference between the time taken for each of the two journeys is  $\frac{2000}{x(x+10)}$  hours. (i)

- [3]
- (ii) Find the difference between the time taken for each of the two journeys when x = 80. Give your answer in **minutes** and **seconds**.

..... min ...... s [3]



*OPQR* is a rectangle and *O* is the origin. *M* is the midpoint of *RQ* and *PT* : TQ = 2 : 1.  $\overrightarrow{OP} = \mathbf{p}$  and  $\overrightarrow{OR} = \mathbf{r}$ .

- (a) Find, in terms of **p** and/or **r**, in its simplest form
  - (i)  $\overrightarrow{MQ}$ ,

R

r

0

- (ii)  $\overrightarrow{MT}$ ,
- (iii)  $\overrightarrow{OT}$ .
- (b) RQ and OT are extended to meet at U.

Find the position vector of U in terms of **p** and **r**. Give your answer in its simplest form.

 $\overrightarrow{MQ}$  = .....[1]



.....[2]

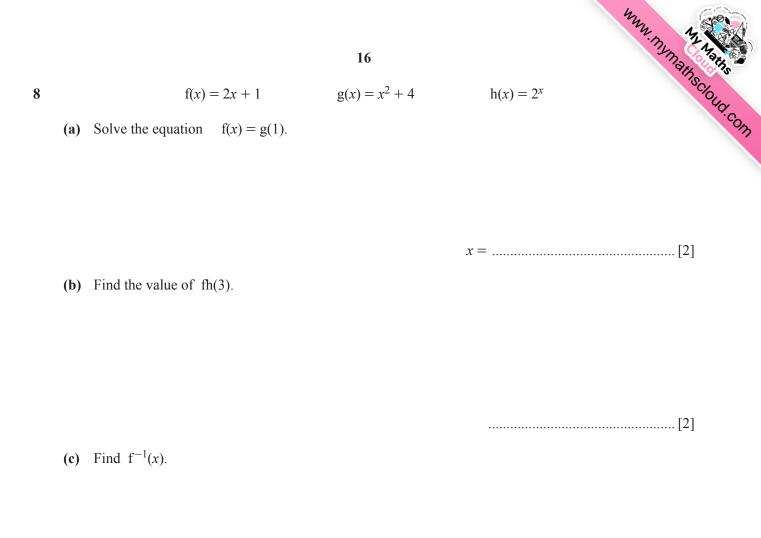
*k* = .....[3]

(c) 
$$\overrightarrow{MT} = \begin{pmatrix} 2k \\ -k \end{pmatrix}$$
 and  $|\overrightarrow{MT}| = \sqrt{180}$ 

Find the positive value of *k*.

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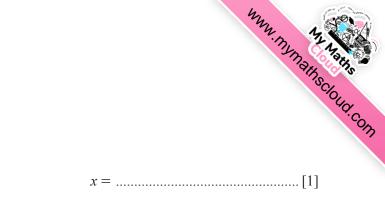
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(d) Find gf(x) in its simplest form.

.....[3]

 $f^{-1}(x) = \dots [2]$ 

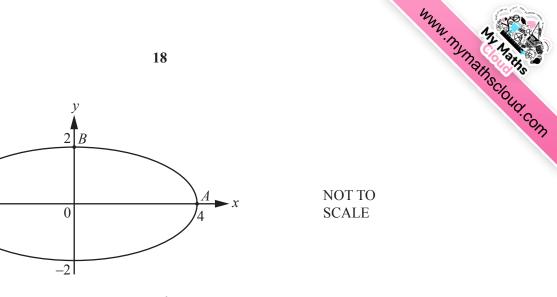


(f)  $\frac{1}{h(x)} = 2^{kx}$ 

Write down the value of *k*.

(e) Solve the equation  $h^{-1}(x) = 0.5$ .

 $k = \dots [1]$ 



The diagram shows a curve with equation  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1.$ 

(a) A is the point (4, 0) and B is the point (0, 2).

Δ

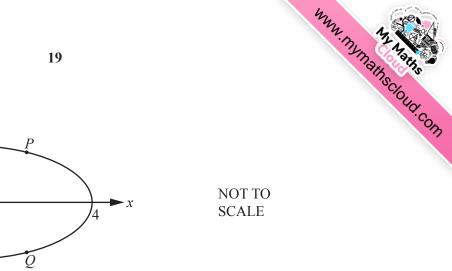
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(i) Find the equation of the straight line that passes through *A* and *B*. Give your answer in the form y = mx + c.

*y* = .....[3]

(ii) Show that  $a^2 = 16$  and  $b^2 = 4$ .

[2]



-2| Q P(2, k) and Q(2, -k) are points on the curve  $\frac{x^2}{16} + \frac{y^2}{4} = 1.$ 

0

(i) Find the value of k.

(ii) Calculate angle *POQ*.

Angle *POQ* = .....[3]

(c) The area enclosed by a curve with equation  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$  is  $\pi ab$ .

(i) Find the area enclosed by the curve  $\frac{x^2}{16} + \frac{y^2}{4} = 1$ .

Give your answer as a multiple of  $\pi$ .

.....[1]

.....[2]

(ii) A curve, mathematically similar to the one in the diagrams, intersects the x-axis at (12, 0) and (-12, 0).

Work out the area enclosed by this curve, giving your answer as a multiple of  $\pi$ .

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**(b)** 



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