



## **Cambridge International Examinations**

Cambridge International General Certificate of Secondary Education

## ADDITIONAL MATHEMATICS Paper 2 MARK SCHEME Maximum Mark: 80

**Published** 

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			°C/6,
Abbrevia	tions		AD
awrt	answers which round to		COM
cao	correct answer only		

## **Abbreviations**

dep dependent

follow through after error ignore subsequent working FΤ isw

or equivalent oe

rounded or truncated rot

Special Case SC seen or implied soi

without wrong working www

Question	Answer	Marks	Part Marks
1	$4x - 3 = x \rightarrow x = 1$ $4x - 3 = -x$ $x = 0.6$	B1 M1 A1	www use of $-x$ or $-(4x-3)$ but not both.
	OR $(4x-3)^2 = x^2$ $15x^2 - 24x + 9 = 0$ 3(x-1)(5x-3) = 0 x = 1 and $x = 0.6$	B1 M1 A1	solve correct 3 term quadratic www
2	$a(\sqrt{3}-1)+b(\sqrt{3}+1)$ $=(\sqrt{3}-3)(\sqrt{3}-1)(\sqrt{3}+1)$ $=2(\sqrt{3}-3) \text{ oe}$	M1	Common denominator or $\times (\sqrt{3} - 1)(\sqrt{3} + 1)$
	a+b=2 $-a+b=-6$ $b=-2  and  a=4$	DM1 A1 DM1	equate constant terms and $\sqrt{3}$ terms. both correct solve two <b>linear</b> equations to obtain $a = \text{ or } b = \text{ both correct}$
3	$2\lg x = \lg x^{2}$ $1 = \lg 10$ $\lg x^{2} - \lg \left(\frac{x+10}{2}\right) = \lg \left(\frac{2x^{2}}{x+10}\right) \text{ oe}$	B1 B1 B1	soi anywhere soi anywhere soi division; logs may be removed
	$2x^{2} - 10x - 100 = 0 \rightarrow 2(x+5)(x-10) = 0$ $x = 10 \text{ only}$	M1 A1	obtain correct 3 term quadratic equation and attempt to solve $x = -5$ must not remain.

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Question	Answer	Marks	Part Marks
4 (i)	$t = 10 \rightarrow N = 7000 + 2000e^{-0.5}$ = 8213 or 8210	B1	Do not accept non integer responses.
(ii)	$N = 7500 \rightarrow 7500 = 7000 + 2000e^{-0.05t}$ $e^{-0.05t} = \frac{500}{2000}$	M1	insert and make e <sup>-0.05t</sup> subject
	$-0.05t = \ln 0.25 \rightarrow t = \frac{\ln 0.25}{-0.05}$ $= 27.7 \text{ (days)}$	M1 A1	take logs and make t the subject awrt 27.7
(iii)	$\frac{dN}{dt} = -100e^{-0.05t}$ $t = 8 \rightarrow \frac{dN}{dt} = \pm 67  (.0)$	M1 A1 A1	$ke^{-0.05t}$ where $k$ is a constant $k = -100$ or $-0.05 \times 2000$ awrt $\pm 67$ mark final answer
5 (i)	$\frac{dy}{dx} = 3x^2 + 4x - 7$ $x = -2 \rightarrow \frac{dy}{dx} = 12 - 8 - 7 = -3$	B1	
	$x = -2 \rightarrow \frac{dy}{dx} = 12 - 8 - 7 = -3$	M1	insert $x = -2$ into <i>their</i> gradient and use $(-2, 16)$ and <i>their</i> gradient of tangent in
	Equation of tangent: $\frac{y-16}{x+2} = -3 \rightarrow y = -3x + 10$	A1	equation of line.
(ii)	Tangent cuts curve again $x^{3} + 2x^{2} - 7x + 2 = -3x + 10$ $x^{3} + 2x^{2} - 4x - 8 = 0$	M1 A1	equate curve and <i>their</i> linear answer from (i).
	(x+2)(x+2)(x-2) = 0	M1	factorise: $(x \pm 2)$ and a two or three term
	x=2,  y=4	A1A1	quadratic is sufficient. Allow long division withhold final <b>A1</b> if (2, 4) not clearly identified as their sole answer.
6 (i)	$\frac{\cos x}{1+\tan x} - \frac{\sin x}{1+\cot x} = \frac{\cos x}{1+\frac{\sin x}{1+\frac{\cos x}{1+\cos x$	M1	$\tan x = \frac{\sin x}{\cos x} \text{ and } \cot x = \frac{\cos x}{\sin x}$
	$= \frac{\cos^2 x}{\cos x + \sin x} - \frac{\sin^2 x}{\cos x + \sin x}$	M1 A1	Attempt to multiply by cosx and sinx
	$=\frac{(\cos x - \sin x)(\cos x + \sin x)}{(\cos x + \sin x)}$	A1	AG
(ii)	$-\sin x + \cos x = 3\sin x - 4\cos x$ $5\cos x = 4\sin x$	M1	equate and collect sinx and cosx oe
	$\tan x = \frac{5}{4}$	A1	
	$x = 51.3^{\circ}, -128.7^{\circ}$	A1A1	FT from tan $x = k$

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Question	Answer	Marks	Part Marks
7 (i)	$h = \sqrt{9 - x^2}$ $A = \frac{\sqrt{9 - x^2}}{2} (14 + x + x) = \sqrt{9 - x^2} (7 + x)$	B2/1/0	Must be clear that $\sqrt{9-x^2}$ is the height of the trapezium. $14+2x$ oe must be seen AG
(ii)	$\frac{dA}{dx} = \sqrt{9 - x^2} + (7 + x)\frac{1}{2}(9 - x^2)^{-0.5} \times -2x$	M1 A2/1/0	product rule on correct function minus 1 each error, allow unsimplified.
	$\frac{dA}{dx} = 0 \rightarrow 9 - x^2 = 7x + x^2$ $2x^2 + 7x - 9 = 0$	M1 A1	equate to 0 and simplify to a linear or quadratic equation. correct three term quadratic obtained
	x=1 $A=16\sqrt{2} \text{ or } 8\sqrt{8} \text{ or } \sqrt{512} \text{ or } 22.6$	A1 A1	Extra positive answer loses penultimate <b>A1</b> . ignore negative solution.
8 (i)	$f'(x) = \frac{(x^3 + 1)9x^2 - (3x^3 - 1)3x^2}{(x^3 + 1)^2}$	M1 A1	quotient rule or product rule all correct
	$=\frac{12x^2}{\left(x^3+1\right)^2}$	A1	www beware $9x^6 - 9x^6$ gets <b>A0</b>
(ii)	$\int_{1}^{2} \frac{x^{2}}{\left(x^{3}+1\right)^{2}} dx = \frac{1}{12} \left[ \frac{3x^{3}-1}{x^{3}+1} \right]_{1}^{2}$	M1	$c \times \frac{3x^3 - 1}{x^3 + 1}$
		A1	$\mathbf{FT} \ c = \frac{1}{their12}$
	$= \frac{1}{12} \left[ \frac{23}{9} - \frac{2}{2} \right]$	DM1	top limit – bottom limit in <i>their</i> integral.
	$=\frac{7}{54}$	A1	or 0.130 or 0.1296 or 0.12
(iii)	$y^3 = \frac{1}{2}$	B1	make $y^3$ or $x^3$ the subject
	$f^{-1}(x) = \sqrt[3]{\frac{x+1}{3-x}}$ Domain: $-1 \le x \le 2\frac{6}{7}$	В1	FT take cube root (as long as $y^3$ or $x^3$ equals a fraction with terms in $x$ or $y$ only) oe
	Domain: $-1 \leqslant x \leqslant 2\frac{6}{7}$	B1 B1	FT change $x$ and $y$ – can be done at any time Allow upper limit of 2.86. Do not isw

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Question	Answer	Marks	Part Marks
9 (i)	tangent touches circle $x^{2} + (kx - 4)^{2} - 2(kx - 4) = 8$	M1	eliminate $y$ or $x$ allow unsimplified
	$k^2x^2 + x^2 - 8kx - 2kx + 16 = 0$ or better	A1	
	Equal roots as tangent touches circle: $b^2 = 4ac$	DM1	use of discriminant on 3 term quadratic soi
	$(-10k)^2 = 4(k^2 + 1) \times 16$	<b>A1</b>	
	$36k^2 = 64$ $k = +\frac{4}{3} \text{ only}$	A1	oe any inequality loses last A1
(ii)	$x = \frac{-b}{2a} \rightarrow x = \frac{\frac{4}{3} \times 10}{\frac{25}{9}}$	M1	use $x = \frac{-b}{2a}$
	$x = \frac{12}{5} \qquad y = -\frac{4}{5}$	A1A1	
	<b>OR</b> tangent $y = \frac{4}{3}x - 4$ cuts radius	M1	find equation of radius and attempt to solve with tangent
	$y = -\frac{3}{4}x + 1$		
	$at x = \frac{12}{5}$	A1	
	$y = -\frac{4}{5}$	<b>A1</b>	
	<b>OR</b> Obtain $25x^2 - 120x + 144 = 0$ oe	M1	obtain any 3 term quadratic using <i>their</i> non zero $k$ and reach $x =$
	$(5x-12)(5x-12) = 0$ $x = \frac{12}{5} \to y = -\frac{4}{5}$		
	$x = \frac{12}{5} \rightarrow y = -\frac{4}{5}$	A1A1	
(iii)	$TP = \sqrt{(0-2.4)^2 + (-4+0.8)^2} = 4$	M1A1	M1 for using their $T$ and $(0,-4)$ . Signs must be correct.

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Question	Answer	Marks	Part Marks
10 (i)	$r_{j} = {5000 \choose 1000 p} + {-2\cos 40 \choose 2\cos 50} t$	B1 B1	x coordinate oe y coordinate oe
(ii)	$2.5t\cos 70 = 5000 - 2t\cos 40$	M1	equate <i>their x</i> values (must be 3 terms)
	$t = \frac{5000}{2.5\cos 70 + 2\cos 40}$	DM1	make $t$ the subject allow one sign error
	= 2095 awrt or 2090 or 2100 $(2.5\cos 20 - 2\cos 50) \times 2095 = 1000 p$	A1 M1	equate <i>their y</i> values(must be 3 terms) and insert <i>their t</i> or $ t $ .
	p = 2.23  awrt	A1	
11 (i)	Free choice: no. of ways ${}^{6}C_{4} \times {}^{5}C_{2} = 15 \times 10$ $= 150$	B1 B1	${}^{6}C_{4} \times \text{another } {}^{n}C_{r} \text{ term only}$ $\times {}^{5}C_{2}$ and answer or vice versa
(ii)	Both Mr and Mrs Coldicott ${}^{5}C_{3} \times {}^{4}C_{1} = 10 \times 4$ $= 40$	B1 B1	${}^{5}C_{3} \times \text{ another } {}^{n}C_{r} \text{ term only}$ $\times {}^{4}C_{1} \text{ and answer or vice versa}$
(iii)	Mr C and not Mrs C ${}^5C_3 \times {}^4C_2 (= 60)$ Not Mr C and Mrs C ${}^5C_4 \times {}^4C_1 (= 20)$ Total = 80	B1 B1 B1	An incorrect final answer does not affect the awarding of the first two <b>B1</b> marks.  www
	OR Total = (i) – (ii) – neither Neither = ${}^{5}C_{4} \times {}^{4}C_{2} = 30$ Total = $150 - 40 - 30 = 80$	M1 A1 A1	