

CAMBRIDGE INTERNATIONAL EXAMINATIONS

Cambridge International General Certificate of Secondary Education

MARK SCHEME for the October/November 2015 series

0606 ADDITIONAL MATHEMATICS

0606/13

Paper 1, maximum raw mark 80

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge will not enter into discussions about these mark schemes.

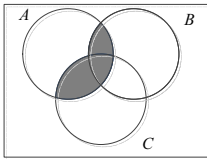
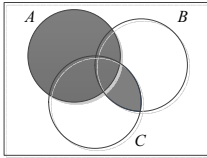
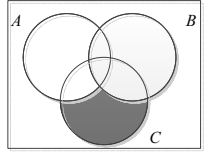
Cambridge is publishing the mark schemes for the October/November 2015 series for most Cambridge IGCSE[®], Cambridge International A and AS Level components and some Cambridge O Level components.

® IGCSE is the registered trademark of Cambridge International Examinations.

Page 2	Mark Scheme	Syllabus	Page 13
	Cambridge IGCSE – October/November 2015	0606	

Abbreviations

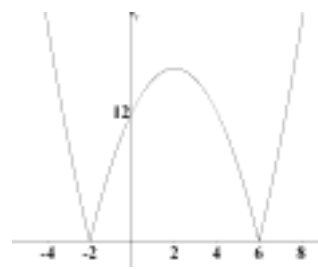
Awrt	answers which round to
Cao	correct answer only
dep	dependent
FT	follow through after error
isw	ignore subsequent working
oe	or equivalent
rot	rounded or truncated
SC	Special Case
soi	seen or implied
www	without wrong working

1	(i)		B1	
	(ii)		B1	
	(iii)		B1	
2	$\cos\left(3x - \frac{\pi}{4}\right) = (\pm)\frac{1}{\sqrt{2}} \text{ oe}$ $3x - \frac{\pi}{4} = -\frac{\pi}{4}, \frac{\pi}{4}, \frac{3\pi}{4}$ $x = \left(-\frac{\pi}{4} + \frac{\pi}{4}\right) \div 3, \left(\frac{\pi}{4} + \frac{\pi}{4}\right) \div 3, \left(\frac{3\pi}{4} + \frac{\pi}{4}\right) \div 3 \text{ oe}$ $x = 0 \text{ and } \frac{\pi}{6} \text{ (or 0 and 0.524)}$ $x = \frac{\pi}{3} \text{ (or 1.05)}$	<p>M1</p> <p>DM1</p> <p>A2/1/0</p>	<p>division by 2 and square root</p> <p>correct order of operations in order to obtain a solution</p> <p>A2 for 3 solutions and no extras in the range</p> <p>A1 for 2 solutions</p> <p>A0 for one solution or no solutions</p>	

Page 3	Mark Scheme	Syllabus	Paper 13
	Cambridge IGCSE – October/November 2015	0606	

3	(a)	$\begin{pmatrix} 12 & 16 & 4 \\ 30 & 32 & 10 \end{pmatrix}$	B2,1,0	B2 for 6 elements correct, B1 for 5 elements correct
	(b)	$\begin{pmatrix} 28 & -24 \\ -8 & 76 \end{pmatrix} = m \begin{pmatrix} 4 & 6 \\ 2 & -8 \end{pmatrix} + n \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$ $-24 = 6m$ or $-8 = 2m$ giving $m = -4$ $28 = 4m + n$ or $76 = -8m + n$ $n = 44$	B2,1,0 B1 M1 A1	B2 for 4 correct elements in X^2 B1 for 3 correct elements in X^2 For $m = -4$ using correct I complete method to obtain n
	(c)	$a^2 - 6 = 0$ so $a = \pm\sqrt{6}$	B2,1,0	B2 for $a = \pm\sqrt{6}$ or $a = \pm 2.45$, with no incorrect statements seen or B1 for $a = \pm\sqrt{6}$ or $a = \pm 2.45$ seen or B1 for $a = \sqrt{6}$ and no incorrect working
4	(i)	$\frac{1}{2}(4\sqrt{3}+1) \times BC = \frac{47}{2}$ $BC = \frac{47}{(4\sqrt{3}+1)} \times \frac{(4\sqrt{3}-1)}{(4\sqrt{3}-1)}$ $BC = 4\sqrt{3}-1$	B1 M1 A1	correct use of the area correct rationalisation Dependent on all method being seen
		Alternative method $\frac{1}{2}(4\sqrt{3}+1) \times BC = \frac{47}{2}$ $(4\sqrt{3}+1)(a\sqrt{3}+b) = 47$ Leading to $12a + b = 47$ and $a + 4b = 0$ Solution of simultaneous equations $BC = 4\sqrt{3}-1$	B1 M1 A1	Dependent on all method seen including solution of simultaneous equations
	(ii)	$(4\sqrt{3}+1)^2 + (4\sqrt{3}-1)^2$ $= (48 + 8\sqrt{3} + 1) + (48 - 8\sqrt{3} + 1)$ $AC^2 = 98$ $AC = 7\sqrt{2}$ or $p = 7$	B1FT B1cao	6 correct FT terms seen 98 and $7\sqrt{2}$ or 98 and $p = 7$

Page 4	Mark Scheme	Syllabus	Paper 13
	Cambridge IGCSE – October/November 2015	0606	

5	<p>When $x = \frac{\pi}{4}, y = 2$</p> <p>$\frac{dy}{dx} = 5\sec^2 x$</p> <p>When $x = \frac{\pi}{4}, \frac{dy}{dx} = 10$</p> <p>Equation of normal $y - 2 = -\frac{1}{10}\left(x - \frac{\pi}{4}\right)$</p> <p>$10y + x - 20 - \frac{\pi}{4} = 0$ or $10y + x - 20.8 = 0$ oe</p>	<p>B1</p> <p>B1</p> <p>B1</p> <p>M1</p> <p>A1</p>	<p>$y = 2$</p> <p>$5\sec^2 x$</p> <p>10 from differentiation</p> <p>$y - 2 = -\frac{1}{10}\left(x - \frac{\pi}{4}\right)$</p> <p>allow unsimplified</p>
6 (i)		<p>B1</p> <p>B1</p> <p>B1</p> <p>M1</p> <p>A1</p> <p>B1</p> <p>B1</p>	<p>shape</p> <p>intercepts on x-axis</p> <p>intercept on y-axis for a curve with a maximum and two arms</p> <p>$(2, \pm 16)$ seen or $(2, k)$ where $k > 0$</p> <p>$(2, 16)$ or $x = 2$ and $y = 16$ only</p>
(ii)	$(2, 16)$		
(iii)	<p>$k = 0$</p> <p>$k > 16$</p>	<p>B1</p> <p>B1</p>	

Page 5	Mark Scheme	Syllabus	Paper 13
	Cambridge IGCSE – October/November 2015	0606	

7	$\frac{dy}{dx} = 2 \sin 3x \quad (+c)$ $4\sqrt{3} = 2 \frac{\sqrt{3}}{2} + c$ $\frac{dy}{dx} = 2 \sin 3x + 3\sqrt{3}$ $y = -\frac{2}{3} \cos 3x + 3\sqrt{3}x \quad (+d)$ $-\frac{1}{3} = -\frac{2}{3} \cos \frac{\pi}{3} + 3\sqrt{3} \left(\frac{\pi}{9} \right) + d$ $y = -\frac{2}{3} \cos 3x + 3\sqrt{3}x - \frac{\sqrt{3}}{3} \pi$	<p>B1</p> <p>M1</p> <p>A1</p> <p>B1FT</p> <p>M1</p> <p>A1</p>	<p>2 sin 3x</p> <p>finding constant using $\frac{dy}{dx} = k \sin 3x + c$ making use of $\frac{dy}{dx} = 4\sqrt{3}$ and $x = \frac{\pi}{9}$</p> <p>Allow with $c = 5.20$ or $\sqrt{27}$</p> <p>FT integration of <i>their</i> $k \sin 3x$</p> <p>finding constant d for $k \cos 3x + cx + d$</p> <p>Allow $y = -0.667 \cos 3x + 5.20x - 0.577\pi$ or better</p>
8	<p>(a)</p> $(2 + kx)^8 = 256 + 1024kx + 1792k^2x^2 + 1792k^3x^3$ $k = \frac{1}{4}$ $p = 112$ $q = 28$ <p>(b)</p> ${}^9C_3 x^6 \left(-\frac{2}{x^2} \right)^3$ $84x^6 \left(-\frac{8}{x^6} \right) \text{ leading to } -672$	<p>B1</p> <p>B1FT</p> <p>B1FT</p> <p>M1</p> <p>DM1</p> <p>A1</p>	<p>FT 1792 multiplied by <i>their</i> k^2</p> <p>FT 1792 multiplied by <i>their</i> k^3</p> <p>correct term seen</p> <p>Term selected and 2^3 and 9C_3 correctly evaluated</p>

Page 6	Mark Scheme	Syllabus	Paper 13
	Cambridge IGCSE – October/November 2015	0606	

9	(a) (i)	Number of arrangements with Maths books as one item = $4!$ or $4 \times 3!$	M1	$4!(\times 2)$ or $4 \times 3!(\times 2)$ oe
		or Maths books can be arranged 2! ways and History 3! ways = $2! \times 3!$		$2! \times 3!(\times 4)$ or $2 \times 3!(\times 4)$ oe
		$2 \times 4!$ or $2 \times 4 \times 3!$ or $4 \times 2 \times 3! = 48$	A1	A1 for 48
	(ii)	$5! - 48$ or $6 \times 2 \times 3!$	M1	$5!$ – <i>their</i> answer to (i)
		72	A1	or for $6 \times 2 \times 3$
	(b) (i)	3003	B1	
	(ii) $3003 - 6 - 135$	M1	<i>their</i> answer to (i) – $6 - {}^6C_4 \times 9$	
	2862	B1	135 subtracted	
	or			
	$2M\ 3W = 720$	M1	complete correct method using 4 cases, may be implied by working. Must have at least one correct	
	$3M\ 2W = 1260$			
	$4M\ 1W = 756$			
	$5M = 126$	B1	any 3 correct	
	2862	A1		

Page 7	Mark Scheme	Syllabus	Paper
	Cambridge IGCSE – October/November 2015	0606	13

10	(i)	$10^2 = 6^2 + 6^2 - 2 \times 6 \times 6 \times \cos ABC$ or $\sin\left(\frac{ABC}{2}\right) = \frac{5}{6}$ or $ABC = \pi - \sin^{-1} \frac{10\sqrt{11}}{36}$ $ABC = 1.9702$	M1	correct cosine rule statement or correct statement for $\sin \frac{ABC}{2}$ or equating areas oe
	(ii)	$XY = 2$ Arc length $6\left(\frac{\pi - 1.970}{2}\right)$ oe Perimeter = $2 + 2\left(6\left(\frac{\pi - 1.970}{2}\right)\right)$ = 9.03	B1 B1 M1 A1	for XY (may be implied by later work, allow on diagram) correct arc length (unsimplified) <i>their</i> $2 + 2 \times 6 \times$ <i>their</i> angle C
	(iii)	$\left(\frac{1}{2} \times 6^2 \left(\frac{\pi - 1.970}{2}\right) - \frac{1}{2} \times 5 \times \sqrt{11}\right) \times 2$ = 4.50 or 4.51 or better	M1 M1 A1	sector area using <i>their</i> C area of $\triangle ABM$ where M is the midpoint of AC , or (\triangle s ABY and BXY) or $\triangle ABC$ Answers to 3sf or better

Page 8	Mark Scheme	Syllabus	Paper 13
	Cambridge IGCSE – October/November 2015	0606	

11	$x^2 - 2x - 3 = 0$ or $y^2 - 6y + 5 = 0$	M1	substitution and simplification to obtain a three term quadratic equation in one variable
	leading to (3, 5) and (-1, 1)	A1,A1	A1 for each 'pair' from a correct quadratic equation, correctly obtained.
	Midpoint (1, 3)	B1cao	midpoint
	(Gradient - 1) Perpendicular bisector $y = 4 - x$	M1	perpendicular bisector, must be using <i>their</i> perpendicular gradient and <i>their</i> midpoint
	Meets the curve again if $x^2 + 10x - 15 = 0$ or $y^2 - 18y + 41 = 0$	M1	substitution and simplification to obtain a three term quadratic equation in one variable.
	leading to $x = -5 \pm 2\sqrt{10}$, $y = 9 \mp 2\sqrt{10}$	A1,A1	A1 for each 'pair'
	$CD^2 = (4\sqrt{10})^2 + (4\sqrt{10})^2$	M1	Pythagoras using <i>their</i> coordinates from solution of second quadratic. $(x_1 - x_2)^2 + (y_1 - y_2)^2$ must be seen if not using correct coordinates.
$CD = 8\sqrt{5}$	A1	A1 for $8\sqrt{5}$ from $\sqrt{320}$ and all correct so far.	

Page 9	Mark Scheme	Syllabus	Paper 13
	Cambridge IGCSE – October/November 2015	0606	

12 (a)	$2^{2x-1} \times 2^{2(x+y)} = 2^7$ and $\frac{3^{2(2y-x)}}{3^{3(y-4)}} = 1$ $2x - 1 + 2(x + y) = 7$ oe $2(2y - x) = 3(y - 4)$ oe leading to $x = 4, y = -4$ <u>Example of Alternative method</u> Method mark as above $2x - 1 + 2(x + y) = 7$ leading to $y = \frac{(8 - 4x)}{2}$ Correctly substituted in $\frac{3^{2(2y-x)}}{3^{3(y-4)}} = 1$ Leading to $2\left(\frac{2(8 - 4x)}{2} - x\right) = 3\left(\frac{(8 - 4x)}{2} - 4\right)$ Leading to $x = 4$ and $y = -4$	M1	expressing 4^{x+y} , 128 as powers of 2 and 9^{2y-x} , 27^{y-4} as powers of 3
		A1 A1 A1	Correct equation from correct working Correct equation from correct working for both
		M1 A1	As before One of the correct equations in x and y
		A1 A1	Correct, unsimplified, equation in x or y only Both answers
(b)	$(2(5^z) - 1)(5^z + 1) = 0$ leading to $2.5^z = 1$ ($5^z = -1$) $5^z = 0.5$	M1	solution of quadratic
		A1	correct solution
		DM1	correct attempt to solve $2.5^z = k$, where k is positive
	$z = \frac{\log 0.5}{\log 5}$ or $z = -0.431$ or better	A1	must have one solution only