



# Cambridge IGCSE™

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**ADDITIONAL MATHEMATICS**

**0606/12**

Paper 1

**May/June 2021**

**2 hours**

You must answer on the question paper.

No additional materials are needed.

## INSTRUCTIONS

- Answer **all** questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do **not** use an erasable pen or correction fluid.
- Do **not** write on any bar codes.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.

## INFORMATION

- The total mark for this paper is 80.
- The number of marks for each question or part question is shown in brackets [ ].

This document has **16** pages.

**Mathematical Formulae****1. ALGEBRA***Quadratic Equation*

For the equation  $ax^2 + bx + c = 0$ ,

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

*Binomial Theorem*

$$(a + b)^n = a^n + \binom{n}{1}a^{n-1}b + \binom{n}{2}a^{n-2}b^2 + \dots + \binom{n}{r}a^{n-r}b^r + \dots + b^n$$

where  $n$  is a positive integer and  $\binom{n}{r} = \frac{n!}{(n-r)!r!}$

*Arithmetic series*      $u_n = a + (n-1)d$

$$S_n = \frac{1}{2}n(a+l) = \frac{1}{2}n\{2a + (n-1)d\}$$

*Geometric series*      $u_n = ar^{n-1}$

$$S_n = \frac{a(1-r^n)}{1-r} \quad (r \neq 1)$$

$$S_\infty = \frac{a}{1-r} \quad (|r| < 1)$$

**2. TRIGONOMETRY***Identities*

$$\begin{aligned} \sin^2 A + \cos^2 A &= 1 \\ \sec^2 A &= 1 + \tan^2 A \\ \operatorname{cosec}^2 A &= 1 + \cot^2 A \end{aligned}$$

*Formulae for  $\triangle ABC$* 

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

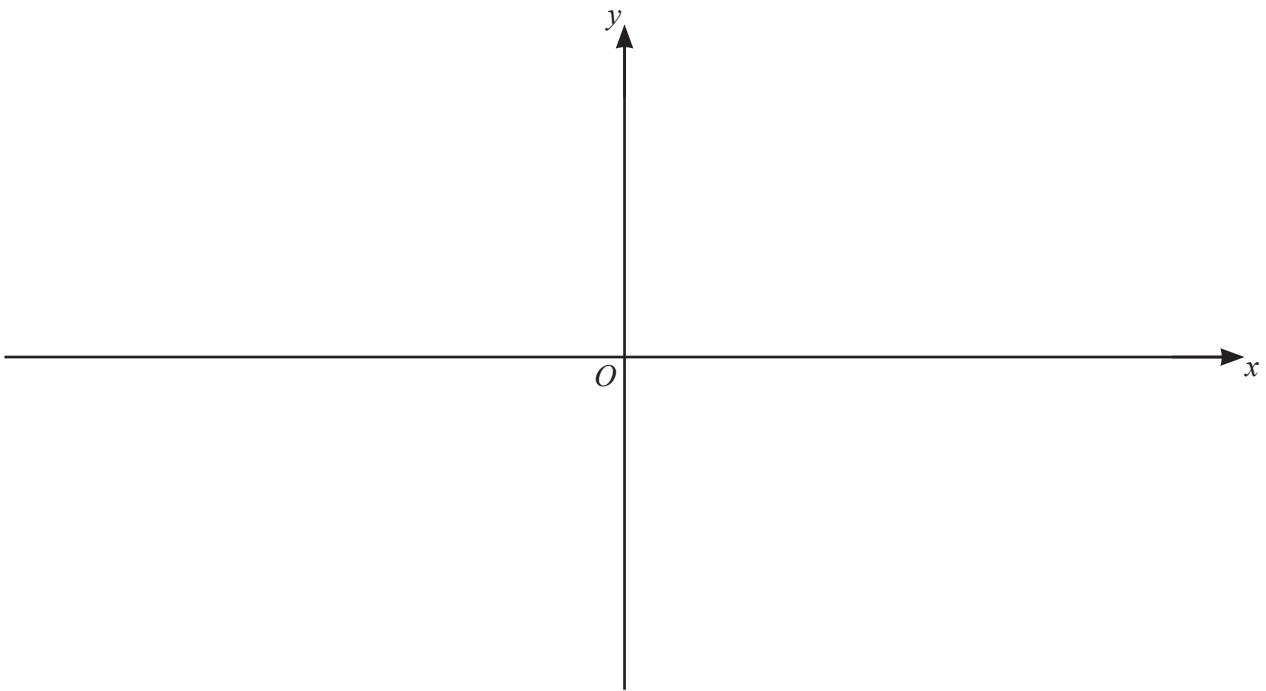
$$a^2 = b^2 + c^2 - 2bc \cos A$$

$$\Delta = \frac{1}{2}bc \sin A$$

1 Write  $\frac{(pqr)^{-2}r^{\frac{1}{3}}}{(p^2r)^{-1}q^3}$  in the form  $p^a q^b r^c$ , where  $a$ ,  $b$  and  $c$  are constants.

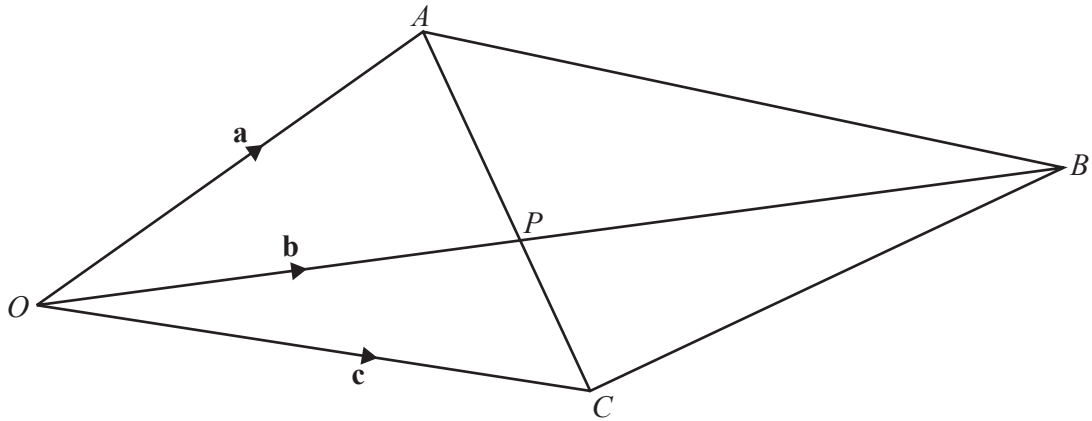
[3]

- 2 (a) On the axes, sketch the graph of  $y = |4 - 3x|$ , stating the intercepts with the coordinate axes. [2]



- (b) Solve the inequality  $|4 - 3x| \geq 7$ . [3]

3



The diagram shows the quadrilateral  $OABC$  such that  $\vec{OA} = \mathbf{a}$ ,  $\vec{OB} = \mathbf{b}$  and  $\vec{OC} = \mathbf{c}$ . The lines  $OB$  and  $AC$  intersect at the point  $P$ , such that  $AP : PC = 3 : 2$ .

(a) Find  $\vec{OP}$  in terms of  $\mathbf{a}$  and  $\mathbf{c}$ . [3]

(b) Given also that  $OP : PB = 2 : 3$ , show that  $2\mathbf{b} = 3\mathbf{c} + 2\mathbf{a}$ . [2]

- 4 A curve is such that  $\frac{d^2y}{dx^2} = (3x + 2)^{-\frac{1}{3}}$ . The curve has gradient 4 at the point (2, 6.2). Find the equation of the curve. [6]

5 (a) Given that  $\log_a p + \log_a 5 - \log_a 4 = \log_a 20$ , find the value of  $p$ . [2]

(b) Solve the equation  $3^{2x+1} + 8(3^x) - 3 = 0$ . [3]

(c) Solve the equation  $4\log_y 2 + \log_2 y = 4$ . [3]

**6 DO NOT USE A CALCULATOR IN THIS QUESTION.**

A curve has equation  $y = (3 + \sqrt{5})x^2 - 8\sqrt{5}x + 60$ .

- (a) Find the  $x$ -coordinate of the stationary point on the curve, giving your answer in the form  $a + b\sqrt{5}$ , where  $a$  and  $b$  are integers. [4]



- (b) Hence find the  $y$ -coordinate of this stationary point, giving your answer in the form  $c\sqrt{5}$ , where  $c$  is an integer. [3]

- 7 (a) A six-character password is to be made from the following eight characters.

Digits	1	3	5	8	9
Symbols	*	\$	#		

No character may be used more than once in a password.

Find the number of different passwords that can be chosen if

- (i) there are no restrictions, [1]
- (ii) the password starts with a digit and finishes with a digit, [2]
- (iii) the password starts with three symbols. [2]
- (b) The number of combinations of 5 objects selected from  $n$  objects is six times the number of combinations of 4 objects selected from  $n - 1$  objects. Find the value of  $n$ . [3]

- 8 Variables  $x$  and  $y$  are such that  $y = Ax^b$ , where  $A$  and  $b$  are constants. When  $\lg y$  is plotted against  $\lg x$ , a straight line graph passing through the points  $(0.61, 0.57)$  and  $(5.36, 4.37)$  is obtained.
- (a) Find the value of  $A$  and of  $b$ . [5]

Using your values of  $A$  and  $b$ , find

- (b) the value of  $y$  when  $x = 3$ , [2]

- (c) the value of  $x$  when  $y = 3$ . [2]

- 9 (a) The first three terms of an arithmetic progression are  $-4, 8, 20$ . Find the smallest number of terms for which the sum of this arithmetic progression is greater than 2000. [4]

(b) The 7th and 9th terms of a geometric progression are 27 and 243 respectively. Given that the geometric progression has a positive common ratio, find

(i) this common ratio, [2]

(ii) the 30th term, giving your answer as a power of 3. [2]

(c) Explain why the geometric progression  $1, \sin \theta, \sin^2 \theta, \dots$  for  $-\frac{\pi}{2} < \theta < \frac{\pi}{2}$ , where  $\theta$  is in radians, has a sum to infinity. [2]

- 10 (a) Solve the equation  $\sin \alpha \operatorname{cosec}^2 \alpha + \cos \alpha \sec^2 \alpha = 0$  for  $-\pi < \alpha < \pi$ , where  $\alpha$  is in radians. [4]

(b) (i) Show that  $\frac{\cos \theta}{1 - \sin \theta} + \frac{1 - \sin \theta}{\cos \theta} = 2 \sec \theta$ . [4]

(ii) Hence solve the equation  $\frac{\cos 3\phi}{1 - \sin 3\phi} + \frac{1 - \sin 3\phi}{\cos 3\phi} = 4$  for  $0^\circ \leq \phi \leq 180^\circ$ . [4]

**Question 11 is printed on the next page.**

- 11 The normal to the curve  $y = \frac{\ln(x^2 + 2)}{2x - 3}$  at the point where  $x = 2$  meets the  $y$ -axis at the point  $P$ .

Find the coordinates of  $P$ .

[7]

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