



Cambridge International Examinations

Cambridge International General Certificate of Secondary Education

ADDITIONAL MATHEMATICS Paper 1 MARK SCHEME Maximum Mark: 80 Published

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Page 2	Mark Scheme	Syllabus	Pulman
	Cambridge IGCSE – May/June 2016	0606	12 4/70 %
Abbreviations			SCIOUD.COD
awrt	answers which round to		.)

Abbreviations

answers which round to awrt cao correct answer only

dependent dep

follow through after error FTignore subsequent working isw

oe or equivalent

rounded or truncated rot

SC Special Case seen or implied soi

without wrong working www

	Question	Answer	Marks	Guidance
1	(a)	$Y \subset X$ or $Y \subseteq X$ only $Y \cap Z = \emptyset$ or $\{\}$ only	B1 B1	
	(b)	(i) (ii)	B1 B1	
2	(i)	$32 - \frac{20}{x} + \frac{5}{x^2}$	В3	B1 for each correct term – must be integers
	(ii)	$(3\times32) + \left(-\frac{20}{x}\times4x\right) = 16$ Accept $16x^{\circ}$	M1 A1	for $(3 \times their 32) + \left(\frac{their(-20)}{x} \times 4x\right)$
3	(i)	$\mathbf{b} - \mathbf{c} = \begin{pmatrix} 6 \\ -2 \end{pmatrix}$ $4 + y^2 = 36 + 4$ $y = \pm 6$	B1 M1 A1	may be implied by further correct working for one correct attempt at using the modulus
	(ii)	$\mu + 4 = 2\lambda \text{or} -4\mu + 24 = 7\lambda$ $\mu - 4 = -\lambda \text{or} 8\mu - 8 = \lambda$ leading to $\mu = \frac{4}{3}$, $\lambda = \frac{8}{3}$ oe allow 1.33 and 2.67 or better	B1 B1 DB1	for one correct equation in μ and λ for a second correct equation in μ and λ for both, must have both previous B marks

			3, 3
Page 3	Mark Scheme	Syllabus	P. J.Mark
	Cambridge IGCSE – May/June 2016	0606	12 %

Question	Answer	Marks	Guidance
4	$(4+\sqrt{5})x^2+(2-\sqrt{5})x-1=0$		You must be convinced that a calculator is not being used.
	$(4+\sqrt{5})x^{2} + (2-\sqrt{5})x - 1 = 0$ $x = \frac{-(2-\sqrt{5}) \pm \sqrt{(2-\sqrt{5})^{2} - 4(4+\sqrt{5})(-1)}}{2(4+\sqrt{5})}$	M1	for use of quadratic formula (allow one sign error), allow $b^2 = 9 - 4\sqrt{5}$ all correct
	$x = \frac{-(2-\sqrt{5}) \pm \sqrt{9-4\sqrt{5}+16+4\sqrt{5}}}{2(4+\sqrt{5})}$	DM1	for attempt to simplify the discriminant (minimum of 4 terms must be seen in discriminant, 2 terms involving $\sqrt{5}$ and 2 constant terms)
	$= \frac{-\left(2 - \sqrt{5}\right) + 5}{2\left(4 + \sqrt{5}\right)}$ $= \frac{3 + \sqrt{5}}{2\left(4 + \sqrt{5}\right)}$	A1	for $\frac{3+\sqrt{5}}{2(4+\sqrt{5})}$ or $\frac{3+\sqrt{5}}{8+2\sqrt{5}}$, ignore negative
	$= \frac{(3+\sqrt{5})(4-\sqrt{5})}{2(4+\sqrt{5})(4-\sqrt{5})}$	M1	solution if included for attempt to rationalise an expression of the form $\frac{a \pm b\sqrt{5}}{c \pm d\sqrt{5}}$ as part of their solution of the
	$=\frac{7+\sqrt{5}}{22}$	A1	quadratic Must obtain an integer denominator Final A1 can only be awarded if all previous marks have been obtained
5 (i)	$(1 - \cos \theta)(1 + \sec \theta)$ $= 1 - \cos \theta + \frac{1}{\cos \theta} - \frac{\cos \theta}{\cos \theta}$ $= \sec \theta - \cos \theta$ $= \frac{1}{\cos \theta} - \cos \theta$	M1	M1 for expansion and use of $\sec \theta = \frac{1}{\cos \theta}$ consistently, allow one sign error
	$=\frac{1-\cos^2\theta}{\cos\theta}$	DM1	for attempt at a single fraction, dependent on first M1
	$=\frac{\sin^2\theta}{\cos\theta}$	A1	
	$= \sin \theta \tan \theta$ www	A1	

			3, 32
Page 4	Mark Scheme	Syllabus	P. Jan
	Cambridge IGCSE – May/June 2016	0606	12 Paths

Question	Answer	Marks	Guidance
	Alternative method: $(1 - \cos \theta) \left(\frac{\cos \theta + 1}{\cos \theta} \right)$ $1 - \cos^2 \theta$	M1	for attempt at a single fraction for second factor and use of $\sec \theta = \frac{1}{\cos \theta}$
	$= \frac{1 - \cos^2 \theta}{\cos \theta}$ $= \frac{\sin^2 \theta}{\cos \theta}$	DM1 A1	for expansion
	$= \sin \theta \tan \theta$ www	A1	
(ii)	$\sin \theta \tan \theta = \sin \theta$ $\sin \theta (\tan \theta - 1) = 0$		
	$\tan \theta = 1$, $\theta = \frac{\pi}{4}$, allow 0.785 or better	B1	for $\theta = \frac{\pi}{4}$ from $\tan \theta = 1$
	$\sin \theta = 0$, $\theta = 0$, π or 3.14 or better	B1 B1	for $\theta = 0$ from $\sin \theta = 0$ for $\theta = \pi$ from $\sin \theta = 0$
6	$\frac{\mathrm{d}}{\mathrm{d}x}\left(\mathrm{e}^{3x}\left(4x+1\right)^{\frac{1}{2}}\right)$		
	$= e^{3x} \frac{1}{2} \times 4(4x+1)^{-\frac{1}{2}} + 3e^{3x} (4x+1)^{\frac{1}{2}}$	B1	for $re^{3x} (4x+1)^{-\frac{1}{2}}$ must be part of a sum, $r = \frac{1}{2}$ or 2 or $\frac{1}{2} \times 4$
		B1	for $se^{3x} (4x+1)^{\frac{1}{2}}$ must be part of a sum, s is 1 or 3
	$= \frac{2e^{3x}}{(4x+1)^{\frac{1}{2}}} + 3e^{3x} (4x+1)^{\frac{1}{2}}$	B1	for all correct, allow unsimplified
	$=\frac{e^{3x}}{(4x+1)^{\frac{1}{2}}}(2+12x+3)$	DM1	for $\frac{e^{3x}}{(4x+1)^{\frac{1}{2}}}(a+bx)$, dependent on first 2 B marks, must be using a correct method,
	$=\frac{e^{3x}}{(4x+1)^{\frac{1}{2}}}(12x+5)$	A1	collecting terms in the numerator correctly
7 (i)	$\cos 3x = \frac{1}{2}$, $x = \frac{\pi}{9}$ or 0.349, 20°, allow 0.35	M1 A1	for correct attempt to solve the trigonometric equation
(ii)	$B\left(\frac{\pi}{3}, 3\right)$ or $(1.05, 3), (60^{\circ}, 3)$	B1B1	B1 for each, must be in correct position or in terms of $x = \text{ and } y =$

			7,7, 32
Page 5	Mark Scheme	Syllabus	PLAN
	Cambridge IGCSE – May/June 2016	0606	12 Paths

Question	Answer	Marks	Guidance
(iii)	$\int_{\frac{\pi}{9}}^{\frac{\pi}{3}} 1 - 2\cos 3x dx = \left[x - \frac{2}{3}\sin 3x \right]_{\frac{\pi}{9}}^{\frac{\pi}{3}}$ $= \frac{\pi}{3} - \left(\frac{\pi}{9} - \left(\frac{2}{3} \times \frac{\sqrt{3}}{2} \right) \right)$ $= \frac{2\pi}{9} + \frac{\sqrt{3}}{3} \text{ oe or } 1.28$	M1 A1 DM1	for $x \pm a \sin 3x$ attempt to integrate at least one term for correct integration for correct use of limits from (i) and (ii), must be in radians
8 (i)	$\lg y = x^{2} \lg b + \lg A$ $\lg b = \pm 0.21$ $b = 0.617 \text{ allow } 0.62, 10^{-0.21}$ $\lg A = 0.94 \text{ allow } 0.93 \text{ to } 0.95$ $A = 8.71 \text{ allow awrt } 8.5 \text{ to } 8.9$	B1 B1 B1 B1	for $\lg b = \pm 0.21$ may be implied
	Alternative method $5.37 \text{ or } 10^{0.73} = Ab$ $1.259 \text{ or } 10^{0.1} = Ab^4$ $b^3 = 10^{-0.63}$ $b = 0.617 \text{ allow } 0.62, 10^{-0.21}$ A = 8.71 allow awrt 8.5 to 8.9	B1 B1 B1 B1	for both equations, allow correct to 2 sf
(ii)	$x = 1.5$, $x^2 = 2.25$ y = 2.93, allow awrt 2.9 or 3.0	M1 A1	for correct use of graph $y = theirA \times theirb^{1.5^2}$ or $\lg y = \lg theirA + \left(1.5^2 \lg theirb\right)$
(iii)	$\lg y = 0.301$, or $2 = 8.71(0.617)^{x^2}$, $x = 1.74$, allow $\sqrt{3}$ or awrt 1.7, 1.8	M1	for correct use of graph to read off x^2 $2 = theirA(theirb)^{x^2}$ or $\lg 2 = (\lg theirb)x^2 + \lg(theirA)$
9 (i)	$y = \frac{2}{3}(3x+10)^{\frac{1}{2}} (+c)$ passes through $\left(2, -\frac{4}{3}\right)$, so $c = -4$ $y = \frac{2}{3}(3x+10)^{\frac{1}{2}} - 4 \text{ oe}$	B1 B1 M1	for $p(3x+10)^{\frac{1}{2}}$ where p is a constant for $\frac{2}{3}(3x+10)^{\frac{1}{2}}$ oe unsimplified for attempt to find c , must have attempt to integrate, must have the first B1
	$y = \frac{1}{3}(3x + 10)^2 - 4$ oe	AI	

			.7, 2
Page 6	Mark Scheme	Syllabus	Perna
_	Cambridge IGCSE – May/June 2016	0606	12 Aths 145

Question	Answer	Marks	Guidance
(ii)	When $x = 5$,		
	$y = -\frac{2}{3}$	B1	
	perpendicular gradient = -5	B1	
		M1	for attempt at the normal using <i>their</i> perpendicular gradient and <i>their y</i> value (but not 4 5.
	Equation of normal: $y + \frac{2}{3} = -5(x - 5)$	A1	$y = -\frac{4}{3} \text{ or } -\frac{5}{3}$).
	When $y = -\frac{5}{3}$,	DM1	for use of $y = -\frac{5}{3}$ in their normal equation to
	x = 5.2 oe	A1	get as far as $x =$
10 (i)	Area: $20 = \pi x^2 + xy$	B1	
	$y = \frac{20 - \pi x^2}{x}$	B1	
	$P = 2\pi x + 2x + 2y$ $= 2\pi x + 2x + 2\left(\frac{20}{x} - \pi x\right)$	M1	for attempt to use perimeter and obtain in terms of x only
	$=2x+\frac{40}{x}$	A1	all steps seen, www AG
	Alternative method: $20 = \pi x^2 + xy$ $P = 2\pi x + 2y + 2x$	B1	
	$=\frac{2}{x}(\pi x^2 + xy) + 2x$	M1	for attempt to use perimeter and write in $\frac{\pi x^2 + xy}{x}$
	$= \frac{2}{x}(20) + 2x$ $= 2x + \frac{40}{x}$	B1	for replacing $\pi x^2 + xy$ with 20
	$=2x+\frac{40}{x}$	A1	all steps seen, www AG

			3, 3
Page 7	Mark Scheme	Syllabus	Punding
	Cambridge IGCSE – May/June 2016	0606	12
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Question	Answer	Marks	Guidance
(ii)	$\frac{\mathrm{d}P}{\mathrm{d}x} = 2 - \frac{40}{x^2}$	M1	for attempt to differentiate
	When $\frac{\mathrm{d}P}{\mathrm{d}x} = 0$,	DM1	for equating to zero and attempt to solve at least as far as $x^2 =$
	$x = 2\sqrt{5}$ allow 4.47, $\sqrt{20}$	A1	
	leading to $P = 8\sqrt{5}$, allow 17.9	A1	
	$\frac{d^2 P}{dx^2} = \frac{80}{x^3}$, always positive so a minimum	A1	for this statement or use of gradient inspection either side of correct x
11 (a) (i)	Distance = area under graph	M1	for attempt to find the area, one correct area seen (triangle, rectangle or trapezium) as part of a sum.
	= 1275	A1	a sum.
(ii)	deceleration is 1.5 oe	B1	
(b)		B 1	for a straight line between (0,0) and (10,60)
		B1FT	FT a straight line between (10, 60) and
			$(20, 90)$, a displacement vector $\begin{pmatrix} 10\\30 \end{pmatrix}$ from their
			(10, their60)
(c) (i)	e ^{2t} is always positive or oe	B1	
(ii)	$a = 8e^{2t}$	M1	for attempt to differentiate, must be of the form
	$e^{2t} = \frac{3}{2}$		pe^{2t} , equate to 12 and solve.
	$t = \frac{1}{2} \ln \frac{3}{2}$, $\ln \sqrt{\frac{3}{2}}$ or $\frac{1}{2} \ln 1.5$	A1	Allow fractions equivalent to $\frac{3}{2}$
(iii)	$s = \left[2e^{2t} + 6t\right]_{0.4}^{0.5}$	M1	for attempt to integrate to get $qe^{2t} + 6t$
		A1	all correct
	$= (2e+3) - (2e^{0.8} + 2.4)$ $(= 8.436 - 6.851)$	DM1	for correct use of limits or considering distances separately, ignore attempts at <i>c</i>
	=1.59, allow 1.58	A1	