		www.myn
	OF CAMBRIDGE INTERNATIONA	
MATHEMATICS (4024/02
Paper 2	C	October/November 2004
Additional Materials:	Answer Booklet/Paper Electronic calculator Geometrical instruments Graph paper (2 sheets) Mathematical tables (optional)	2 hours 30 minutes

READ THESE INSTRUCTIONS FIRST

Write your answers and working on the separate Answer Booklet/Paper provided. Write your Centre number, candidate number and name on all the work you hand in. Write in dark blue or black pen on both sides of the paper. You may use a pencil for any diagrams or graphs. Do not use staples, paper clips, highlighters, glue or correction fluid.

Section A

Answer **all** questions.

Section B Answer any four questions.

At the end of the examination, fasten all your work securely together. The number of marks is given in brackets [] at the end of each question or part question.

Show all your working on the same page as the rest of the answer.

Omission of essential working will result in loss of marks.

The total of the marks for this paper is 100.

You are expected to use an electronic calculator to evaluate explicit numerical expressions. You may use mathematical tables as well if necessary.

If the degree of accuracy is not specified in the question, and if the answer is not exact, give the answer to three significant figures. Give answers in degrees to one decimal place.

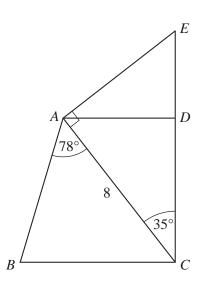
For π , use either your calculator value or 3.142, unless the question requires the answer in terms of π .

This document consists of **10** printed pages and **2** blank pages.



Section A [52 marks]

Answer **all** the questions in this section.



The diagram represents some beams which support part of a roof.

AD and BC are horizontal and CDE is vertical.

$$AC = 8$$
 metres, $B\hat{A}C = 78^\circ$, $A\hat{C}D = 35^\circ$ and $C\hat{A}E = 90^\circ$.

Calculate the length of the beam

1

(a) A	[2]
(b) C	[2]
(c) A	[3]

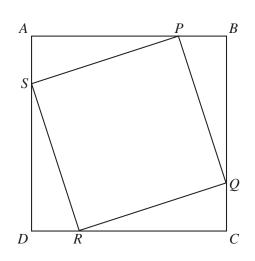
2	3 The points A R and C are $(0, 8)$ (12, 4) and $(4, -2)$ respectively.	WWW. MY MAINS CIOUD. COM
2	The points A, B and C are $(9, 8)$, $(12, 4)$ and $(4, -2)$ respectively.	-1040 ·
	(a) Find	·com
	(i) the gradient of the line through <i>A</i> and <i>B</i> ,	[1]
	(ii) the equation of the line through C which is parallel to AB .	[2]
	(b) Calculate the length of the line segment	
	(i) AB ,	[1]
	(ii) <i>BC</i> .	[1]
	(c) Show that AB is perpendicular to BC .	[1]
	(d) Calculate the area of triangle <i>ABC</i> .	[1]

3	Mr	Smit	h bought three companies, Alpha, Beta and Gamma, for a total of \$80 000 000.	
	The	amo	bunts he paid for these companies were in the ratio $4:5:7$.	
	(a)	Cal	culate how much he paid for each company.	[2]
	(b)	Wh	en he sold the companies, he made a profit of 12% on the \$80000000 he paid for them.	
		Cal	culate the profit he made on the sale of the three companies.	[1]
	(c)	Wh	en he sold the companies, he made a profit of 25% on Alpha and a loss of 10% on Beta.	
		Cal	culate	
		(i)	the profit he made on Alpha,	[1]
		(ii)	the percentage profit that he made on Gamma.	[3]

(d) When the previous owner, Mr Jones, sold the companies to Mr Smith for \$80,000, he made a profit of 60%.

Calculate the total amount Mr Jones had paid for the companies. [2]





4

In the diagram, ABCD is a square.

Points P, Q, R and S lie on AB, BC, CD and DA so that AP = BQ = CR = DS.

(a) Giving all your reasons, show that

(i)	PB = QC,	[2]
(ii)	triangle BPQ is congruent to triangle CQR ,	[3]
(iii)	PQR is a right angle.	[2]
(b) Wri	te down two reasons to show that PQRS is a square.	[2]

5 (a) It is given that $S = \frac{n(a+l)}{2}$.

(i) Find the value of S when $n = 20$, $a = -5$ and $l = 17$. [[1]
---	-----

- (ii) Express l in terms of S, n and a. [2]
- (**b**) Solve the equations

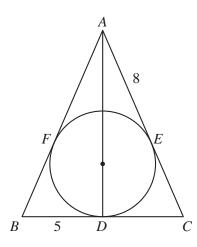
(i)
$$5t^2 = 12t$$
, [2]
(ii) $y = 1$ 2

(ii)
$$\frac{y-1}{8} = \frac{2}{y-1}$$
. [3]

(c) Solve the equation $3x^2 + 9x + 5 = 0$, giving both answers correct to two decimal places. [4]



6 (a)



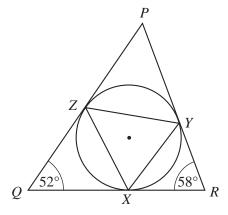
The diagram shows a circle which passes through *D*, *E* and *F*. *AFB*, *BDC* and *CEA* are tangents to the circle. *D* is the midpoint of *BC*.

Given that BD = 5 cm and AE = 8 cm, find

(i)
$$EC$$
,
[1]

(ii) $C\hat{A}D$.
[2]

(b)



The diagram shows a circle which passes through *X*, *Y* and *Z*. *PZQ*, *QXR* and *RYP* are tangents to the circle.

Given that $P\hat{Q}R = 52^{\circ}$ and $Q\hat{R}P = 58^{\circ}$, calculate

(i)	QPR,	[1]
(ii)	QŹX,	[2]
(iii)	ΖÂΥ.	[2]

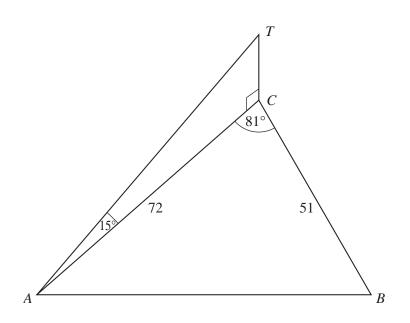


Section B [48 marks]

Answer **four** questions in this section.

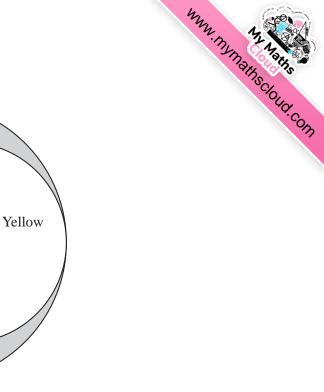
Each question in this section carries 12 marks.





Three paths, *AB*, *BC* and *CA*, run along the edges of a horizontal triangular field *ABC*. BC = 51 m, AC = 72 m and angle $ACB = 81^{\circ}$.

(a)	Calculate the length of <i>AB</i> .	[4]
(b)	Calculate the area of the field <i>ABC</i> .	[2]
(c)	Calculate the shortest distance from <i>C</i> to <i>AB</i> .	[2]
(d)	A vertical tree, <i>CT</i> , has its base at <i>C</i> . The angle of elevation of the top of the tree from <i>A</i> is 15° .	
	Calculate the height of the tree.	[2]
(e)	John measured the largest angle of elevation of the top of the tree as seen from the path AB .	
	Calculate this angle of elevation.	[2]



The diagram shows the design of a company symbol.

It consists of three circles.

The smallest circle has centre O and radius 2x centimetres.

Green

The largest circle has centre *O* and radius 2*y* centimetres.

The third circle touches both the other two circles as shown.

The three regions formed are coloured red, yellow and green as shown.

(a) Explain fully why the radius of the third circle is (x + y) centimetres. [2]

7

Red

0

(b) Write down, in terms of π , x and y, expressions for the area of the region that is coloured

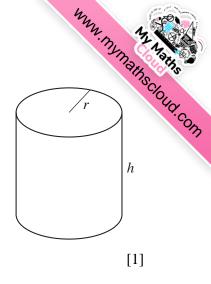
(i) yellow,	[1]
-------------	-----

- (ii) green. [1]
- (c) The area of the green region is twice the area of the yellow region. Use this information to write down an equation involving *x* and *y*, and show that it simplifies to

$$y^2 - 6xy + 5x^2 = 0.$$
 [3]

(d) (i) Factorise $y^2 - 6xy + 5x^2$.	[1]
(ii) Solve the equation $y^2 - 6xy + 5x^2 = 0$, expressing y in terms of x.	[2]
(e) Calculate the fraction of the design that is coloured yellow.	[2]

			my north
		8	Munail and
9	Three in The thre	tegers, <i>a</i> , <i>b</i> and <i>c</i> , are such that $a < b < c$. e integers are said to form a Pythagorean Triple if $c^2 = a^2 + b^2$ or $c^2 - b^2 = a^2$.	WWW. MY MAINS CIOLID COM
	For exam 3, 4 and 5, 1	nple , 5 form a Pythagorean Triple because $5^2 - 4^2 = (5 - 4)(5 + 4) = 1 \times 9 = 9 = 3^2$ 2, 13 form a Pythagorean Triple because $13^2 - 12^2 = (13 - 12)(13 + 12) = 1 \times 25 = 12^2$	
	(a) In t	he same way, show that 7, 24 and 25 form a Pythagorean Triple.	[1]
	(b) For	m a Pythagorean Triple	
	(i)	in which the last two integers are 40 and 41,	[1]
	(ii)	in which the first integer is 11.	[1]
	(c) (i)	Simplify $(n + 1)^2 - n^2$.	[1]
	(ii)	Hence form a Pythagorean Triple in which the first integer is 101.	[2]
	(d) It is	also possible to form Pythagorean Triples in which the last two integers differ by	2.
	For 8, 1	example 5, 17 form a Pythagorean Triple because $17^2 - 15^2 = (17 - 15)(17 + 15) = 2 \times 32 =$	$64 = 8^2$.
	(i)	Copy and complete the following statements:	
		, 35, 37 form a Pythagorean Triple because $37^2 - 35^2 = ()() = \dots \times \dots =$	= = [1]
		16,, form a Pythagorean Triple because – = ()() = $2 \times =$	$ = 16^2.[2]$
	(ii)	Simplify $(4n^2 + 1)^2 - (4n^2 - 1)^2$ and hence express it as a perfect square.	[2]
	(iii)	Form a Pythagorean Triple in which the first integer is 400 and the other t differ by 2.	wo integers [1]



10 Answer the whole of this question on a sheet of graph paper.

A solid cylinder of radius *r* centimetres and height *h* centimetres has a volume of $100 \,\pi \,\mathrm{cm}^3$.

- (a) (i) Show that $h = \frac{100}{r^2}$.
 - (ii) The cylinder has a total surface area of πy square centimetres.

Show that
$$y = 2r^2 + \frac{200}{r}$$
. [1]

(b) The table below shows some values of r and the corresponding values of y, correct to the nearest whole number.

r	1	1.5	2	3	4	5	6
у	202	138	108	85	82	90	р

9

(i) Find the value of *p*. [1] (ii) Using a scale of 2 cm to represent 1 cm, draw a horizontal *r*-axis for $1 \le r \le 6$. Using a scale of 2 cm to represent 20 cm², draw a vertical y-axis for $70 \le y \le 220$. On your axes, plot the points given in the table and join them with a smooth curve. [3] (c) Use your graph to find the values of r for which y = 100. [2] (d) By drawing a tangent, find the gradient of the graph at the point where r = 2. [2] (e) Use your graph to find the value of *r* for which *y* is least, [1] **(i)** the smallest possible value of the total surface area of the cylinder. (ii) [1]

4024/02/O/N/04

11 Answer the whole of this question on a sheet of graph paper.

www.mymathscloud.com The table below shows the marks obtained in tests of English and Mathematics by 140 students.

Mark (<i>x</i>)	Number of candidates		
	English	Mathematics	
$0 < x \le 20$	4	10	
$20 < x \le 40$	26	20	
$40 < x \le 60$	50	30	
$60 < x \le 80$	56	55	
$80 < x \le 100$	4	25	

(a) Copy and complete the cumulative frequency table below.

Mark (<i>x</i>)	Number of candidates		
	English	Mathematics	
x = 0	0	0	
$x \le 20$	4		
$x \le 40$			
$x \le 60$			
$x \le 80$			
$x \le 100$	140		

- (b) Using a scale of 2 cm to represent 20 marks, draw a horizontal x-axis for $0 \le x \le 100$. Using a scale of 2 cm to represent 20 pupils, draw a vertical axis for values from 0 to 140. On your axes, draw and label both smooth cumulative frequency curves to illustrate this information. [3]
- (c) Use your curves to find

	(i)	the upper quartile mark for English,	[1]		
	(ii)	the interquartile range for English,	[1]		
	(iii)	the median mark for English and the median mark for Mathematics.	[1]		
(d)	Stat	e, with a reason, which you think is the easier test.	[1]		
(e)		One student is chosen at random. It may be assumed that the marks gained in the two subjects are independent.			
	Expressing each answer as a fraction in its lowest terms, calculate the probability that the student gains				
	(i)	more than 60 marks on both papers,	[1]		
	(ii)	more than 80 marks on one paper, but not on the other.	[2]		

© UCLES 2004

[2]



BLANK PAGE



BLANK PAGE

Every reasonable effort has been made to trace all copyright holders where the publishers (i.e. UCLES) are aware that third-party material has been reproduced. The publishers would be pleased to hear from anyone whose rights they have unwittingly infringed.

University of Cambridge International Examinations is part of the University of Cambridge Local Examinations Syndicate (UCLES), which is itself a department of the University of Cambridge.