

Cambridge International Examinations Cambridge Ordinary Level



4037/22 October/November 2016

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Paper 2 MARK SCHEME Maximum Mark: 80

Published

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Abbrevi			Cloud.cc
awrt cao	answers which round to correct answer only		UN,
dep	dependent		

## Abbreviations

awrt	answers which round to
cao	correct answer only
dep	dependent
FT	follow through after error
isw	ignore subsequent working
oe	or equivalent
rot	rounded or truncated
SC	Special Case
soi	seen or implied
WWW	without wrong working

Question	Answer	Marks	Part Marks
1	$4x - 3 = x \rightarrow x = 1$ 4x - 3 = -x x = 0.6	B1 M1 A1	www use of $-x$ or $-(4x-3)$ but not both.
	<b>OR</b> $(4x-3)^2 = x^2$ $15x^2 - 24x + 9 = 0$	B1	
	3(x-1)(5x-3) = 0 x = 1 and x = 0.6	M1 A1	solve correct 3 term quadratic www
2	$a\left(\sqrt{3}-1\right)+b\left(\sqrt{3}+1\right)$	M1	Common denominator or
	$= \left(\sqrt{3} - 3\right)\left(\sqrt{3} - 1\right)\left(\sqrt{3} + 1\right)$ $= 2\left(\sqrt{3} - 3\right) \text{ oe}$		$\times \left(\sqrt{3} - 1\right) \left(\sqrt{3} + 1\right)$
	a+b=2-a+b=-6	DM1 A1 DM1	equate constant terms and $\sqrt{3}$ terms. both correct solve two <b>linear</b> equations to obtain $a = $ or
	b = -2 and $a = 4$	A1	<i>b</i> = both correct
3	$2\lg x = \lg x^{2}$ 1 = lg10	B1 B1	soi anywhere soi anywhere
	$\lg x^2 - \lg \left(\frac{x+10}{2}\right) = \lg \left(\frac{2x^2}{x+10}\right) \text{ oe}$	<b>B</b> 1	soi division; logs may be removed
	$2x^{2} - 10x - 100 = 0 \rightarrow 2(x+5)(x-10) = 0$	M1	obtain correct 3 term quadratic equation and attempt to solve
	x = 10 only	A1	x = -5 must not remain.

## Mark Scheme Cambridge O Level – October/November 2016

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Question	Answer	Marks	Munu Marks
4 (i)	$t = 10 \rightarrow N = 7000 + 2000e^{-0.5}$ = 8213 or 8210	B1	Do not accept non integer responses.
(ii)	$N = 7500 \rightarrow 7500 = 7000 + 2000e^{-0.05t}$ $e^{-0.05t} = \frac{500}{2000}$	M1	insert and make e <sup>-0.05t</sup> subject
	2000 -0.05t = ln0.25 $\rightarrow t = \frac{\ln 0.25}{-0.05}$ = 27.7 (days)	M1 A1	take logs and make <i>t</i> the subject awrt 27.7
(iii)	$\frac{\mathrm{d}N}{\mathrm{d}t} = -100\mathrm{e}^{-0.05t}$ $t = 8 \longrightarrow \frac{\mathrm{d}N}{\mathrm{d}t} = \pm 67 \ (.0)$	M1 A1 A1	$ke^{-0.05t}$ where k is a constant $k = -100$ or $-0.05 \times 2000$ awrt $\pm 67$ mark final answer
5 (i)	$\frac{\mathrm{d}y}{\mathrm{d}x} = 3x^2 + 4x - 7$	B1	
	$x = -2 \rightarrow \frac{\mathrm{d}y}{\mathrm{d}x} = 12 - 8 - 7 = -3$	M1	insert $x = -2$ into <i>their</i> gradient and use $(-2, 16)$ and <i>their</i> gradient of tangent in
	Equation of tangent : $\frac{y-16}{x+2} = -3 \rightarrow y = -3x+10$	A1	equation of line.
(ii)	Tangent cuts curve again $x^{3} + 2x^{2} - 7x + 2 = -3x + 10$	M1 A1	equate curve and <i>their</i> linear answer from (i).
	$x^{3} + 2x^{2} - 4x - 8 = 0$ (x+2)(x+2)(x-2) = 0	M1	factorise: $(x \pm 2)$ and a two or three term
	x = 2,  y = 4	A1A1	quadratic is sufficient. Allow long division withhold final $A1$ if (2, 4) not clearly identified as their sole answer.
6 (i)	$\frac{\cos x}{1+\tan x} - \frac{\sin x}{1+\cot x} = \frac{\cos x}{1+\frac{\sin x}{1+\frac{\cos x}{1+\cos x$	M1	$\tan x = \frac{\sin x}{\cos x}$ and $\cot x = \frac{\cos x}{\sin x}$
	$=\frac{\cos^2 x}{\cos x + \sin x} - \frac{\sin^2 x}{\cos x + \sin x}$	M1 A1	Attempt to multiply by cosx and sinx
	$=\frac{(\cos x - \sin x)(\cos x + \sin x)}{(\cos x + \sin x)}$	A1	AG
(ii)	$-\sin x + \cos x = 3\sin x - 4\cos x$ $5\cos x = 4\sin x$	M1	equate and collect sinx and cosx oe
	$\tan x = \frac{5}{4}$	A1	
	$x = 51.3^{\circ}, -128.7^{\circ}$	A1A1	<b>FT</b> from tan $x = k$

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Question	Answer	Marks	Part Marks
7 (i)	$h = \sqrt{9 - x^2}$ $A = \frac{\sqrt{9 - x^2}}{2} (14 + x + x) = \sqrt{9 - x^2} (7 + x)$	B2/1/0	Must be clear that $\sqrt{9-x^2}$ is the height of the trapezium. $14+2x$ oe must be seen AG
(ii)	$\frac{dA}{dx} = \sqrt{9 - x^2} + (7 + x)\frac{1}{2}(9 - x^2)^{-0.5} \times -2x$	M1 A2/1/0	product rule on correct function minus 1 each error, allow unsimplified.
	$\frac{\mathrm{d}A}{\mathrm{d}x} = 0 \longrightarrow 9 - x^2 = 7x + x^2$	M1	equate to 0 and simplify to a linear or quadratic equation.
	$2x^2 + 7x - 9 = 0$	A1	correct three term quadratic obtained
	x=1 $A=16\sqrt{2} \text{ or } 8\sqrt{8} \text{ or } \sqrt{512} \text{ or } 22.6$	A1 A1	Extra positive answer loses penultimate A1. ignore negative solution.
3 (i)	$f'(x) = \frac{(x^3 + 1)9x^2 - (3x^3 - 1)3x^2}{(x^3 + 1)^2}$	M1 A1	quotient rule or product rule all correct
	$=\frac{12x^2}{\left(x^3+1\right)^2}$	A1	www beware $9x^6 - 9x^6$ gets <b>A0</b>
(ii)	$\int_{1}^{2} \frac{x^{2}}{\left(x^{3}+1\right)^{2}} dx = \frac{1}{12} \left[\frac{3x^{3}-1}{x^{3}+1}\right]_{1}^{2}$	M1	$c \times \frac{3x^3 - 1}{x^3 + 1}$
		A1	<b>FT</b> $c = \frac{1}{their 12}$
	$=\frac{1}{12}\left[\frac{23}{9}-\frac{2}{2}\right]$	DM1	top limit – bottom limit in <i>their</i> integral.
	$=\frac{7}{54}$	A1	or 0.130 or 0.1296 or 0.12
(iii)	$x = \frac{3y^3 - 1}{y^3 + 1}$		
	$y^{3} + 1$ $y^{3} = \frac{x+1}{3-x}$	B1	make $y^3$ or $x^3$ the subject
	$f^{-1}(x) = \sqrt[3]{\frac{x+1}{3-x}}$	B1	<b>FT</b> take cube root (as long as $y^3$ or $x^3$ equals fraction with terms in <i>x</i> or <i>y</i> only) oe
	6	B1	<b>FT</b> change $x$ and $y$ – can be done at any time
	Domain : $-1 \leq x \leq 2\frac{6}{7}$	<b>B</b> 1	Allow upper limit of 2.86 . Do not isw

Page 5	Mark Scheme Cambridge O Level – October/November 2016		Syllabus P.   mber 2016 4037 22   Part Marks
Question	Answer	Marks	Part Marks
9 (i)	tangent touches circle $x^{2} + (kx - 4)^{2} - 2(kx - 4) = 8$	M1	eliminate $y$ or $x$ allow unsimplified
	$k^2 x^2 + x^2 - 8kx - 2kx + 16 = 0$ or better	A1	
	Equal roots as tangent touches circle : $b^2 = 4ac$	DM1	use of discriminant on 3 term quadratic soi
	$(-10k)^2 = 4(k^2 + 1) \times 16$	A1	
	$36k^2 = 64$ $k = +\frac{4}{3}$ only	A1	oe any inequality loses last A1
(ii)	$x = \frac{-b}{2a} \rightarrow x = \frac{\frac{4}{3} \times 10}{\frac{25}{9}}$	M1	use $x = \frac{-b}{2a}$
	$x = \frac{12}{5}$ $y = -\frac{4}{5}$	A1A1	
	<b>OR</b> tangent $y = \frac{4}{3}x - 4$ cuts radius	M1	find equation of radius and attempt to solve with tangent
	$y = -\frac{3}{4}x + 1$		
	at $x = \frac{12}{5}$	A1	
	$y = -\frac{4}{5}$	A1	
	<b>OR</b> Obtain $25x^2 - 120x + 144 = 0$ oe	M1	obtain any 3 term quadratic using <i>their</i> non zero $k$ and reach $x =$
	(5x-12)(5x-12)=0		
	$x = \frac{12}{5} \rightarrow y = -\frac{4}{5}$	A1A1	
(iii)	$TP = \sqrt{\left(0 - 2.4\right)^2 + \left(-4 + 0.8\right)^2} = 4$	M1A1	<b>M1</b> for using <i>their</i> T and $(0, -4)$ . Signs must be correct.

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Syllabus 4037

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Question	Answer	Marks	Part M	larks
10 (i)	$r_j = \begin{pmatrix} 5000\\1000p \end{pmatrix} + \begin{pmatrix} -2\cos 40\\2\cos 50 \end{pmatrix} t$	B1 B1	<i>x</i> coordinate oe <i>y</i> coordinate oe	
(ii)	$2.5t\cos 70 = 5000 - 2t\cos 40$	M1	equate <i>their x</i> values (mu	st be 3 terms)
	$t = \frac{5000}{2.5\cos 70 + 2\cos 40}$	DM1	make <i>t</i> the subject allow	one sign error
	= 2095 awrt or 2090 or 2100	A1		(1.2.) 1
	$(2.5\cos 20 - 2\cos 50) \times 2095 = 1000 p$	M1	equate <i>their</i> y values(must insert <i>their</i> t or $ t $ .	st be 3 terms) and
	p = 2.23 awrt	A1		
11 (i)	Free choice : no. of ways	Dá	60 1 201	1
	${}^{6}C_{4} \times {}^{5}C_{2} = 15 \times 10$	B1 B1	${}^{6}C_{4} \times \text{another } {}^{n}C_{r} \text{ term of}$	
	=150	DI	$\times^5 C_2$ and answer or vic	e versa
(ii)	Both Mr and Mrs Coldicott ${}^{5}C$ ${}^{4}C$ ${}^{1}$ 10 ${}^{4}$	B1	${}^{5}C_{3} \times \text{another } {}^{n}C_{r} \text{ term o}$	nlv
	${}^{5}C_{3} \times {}^{4}C_{1} = 10 \times 4$ = 40	B1	$\times^4 C_1$ and answer or vice	
(iii)	Mr C and not Mrs C ${}^{5}C_{3} \times {}^{4}C_{2} (= 60)$ Not Mr C and Mrs C ${}^{5}C_{4} \times {}^{4}C_{1} (= 20)$	B1 B1 B1	An incorrect final answer awarding of the first two	r does not affect the
	Total = 80	B1	WWW	
	<b>OR</b> Total = $(i) - (ii)$ – neither	M1		
	Neither = ${}^{5}C_{4} \times {}^{4}C_{2} = 30$ Total = 150 - 40 - 30 = 80	A1 A1		