

MARK SCHEME for the October/November 2015 series

4037 ADDITIONAL MATHEMATICS

4037/22

Paper 2, maximum raw mark 80

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Page 2	Mark Scheme	Syllabus	P. M. Mary
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Abbrevi	ations		SCIOUD.
awrt	answers which round to		CON.
cao	correct answer only		
den	dependent		

Abbreviations

awrt	answers which round to
cao	correct answer only
dep	dependent
FT	follow through after error
isw	ignore subsequent working
nfww	not from wrong working
oe	or equivalent
rot	rounded or truncated
SC	Special Case
soi	seen or implied
WWW	without wrong working

1	(i)	f(-2) = -32 - 16 + 30 + 18 = 0	B1	All four evaluated terms must be seen. Allow if correct long division used
	(ii)	$f(x) = (x+2)(4x^2 - 12x + 9)$	M1 A1	Coefficients 4 and 9 Coefficient –12
		=(x+2)(2x-3)(2x-3)	A1	All three factors together
		$f(x) = 0 \rightarrow x = -2, 1.5$ nfww	A1	Allow 1.5 mentioned just once
2	(i)	$(2-3x)^6 = 64 - 576x + 2160x^2$ isw	B1B1B1	
	(ii)	$2160 - 2 \times 576 = 1008$	M1 A1	<i>their</i> final $2160 + 2 \times their$ final -576
3	(i)	$\overrightarrow{AB} = \begin{pmatrix} -15\\ 8 \end{pmatrix}$	B1	Allow \overrightarrow{BA} May be implied by later work.
		$ AB = \sqrt{15^2 + 8^2} (=17)$	M1	Use of Pythagoras on <i>their AB</i>
		Speed = $17 \times 3 = 51$ km/hr	A1	Must be exact
	(ii)	$\overrightarrow{BC} = \begin{pmatrix} 16\\ -30 \end{pmatrix}$	B1	Allow \overrightarrow{CB}
		$ BC = \sqrt{16^2 + 30^2} (= 34)$	M1	Use of Pythagoras on <i>their BC</i>
		Time taken = $\frac{34}{51} \times 60 = 40$ mins (or $\frac{2}{3}$ hrs)	A1	Allow answers which round to 40 to 2sf. Accept 0.66 or 0.67 hrs. Mark final answer.

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Pa	age 3	Mark Scheme		Syllabus P. 472
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4	(a)	$2\mathbf{B}\mathbf{A} = 2 \begin{pmatrix} 1 & -2 & 4 \\ -2 & 3 & 0 \end{pmatrix} \begin{pmatrix} 2 & -1 \\ 3 & 5 \\ 7 & 4 \end{pmatrix}$	B3,2,1,0	-1 each error in 2 × 2 result. Failure to multiply by 2 is one error
	(b) (i)	$= 2 \begin{pmatrix} 24 & 5\\ 5 & 17 \end{pmatrix} = \begin{pmatrix} 48 & 10\\ 10 & 34 \end{pmatrix}$ $\mathbf{C}^{-1} = \frac{1}{8} \begin{pmatrix} 6 & -2\\ 1 & 1 \end{pmatrix} \text{ isw}$	B1	$\frac{1}{8}$
			B1	o Matrix
	(ii)	$\mathbf{I} - \mathbf{D} = \begin{pmatrix} -2 & 2\\ -1 & -3 \end{pmatrix}$	B1	
		$\mathbf{X} = \mathbf{C}^{-1} \left(\mathbf{I} - \mathbf{D} \right) = \frac{1}{8} \begin{pmatrix} 6 & -2 \\ 1 & 1 \end{pmatrix} \begin{pmatrix} -2 & 2 \\ -1 & -3 \end{pmatrix}$ $1 \begin{pmatrix} -10 & 18 \end{pmatrix} .$	M1	Pre multiply <i>their</i> $\mathbf{I} - \mathbf{D}$ with <i>their</i> \mathbf{C}^{-1}
		$=\frac{1}{8}\begin{pmatrix} -10 & 18\\ -3 & -1 \end{pmatrix}$ isw	A1	
5	(a)	$2^{3(q-1)} \times 2^{2p+1} = 2^{14}$	B1	Correct powers of 2 allow unsimplified isw
		$3^{2(p-4)} \times 3^q = 3^4$	B1	Correct powers of 3 allow unsimplified isw
		Solve $3q + 2p = 16$ q + 2p = 12	M1	Attempt to solve <i>their</i> linear equations by eliminating one variable
		p=5, q=2	A1	Both correct
	(b)	(3x-2)(x+1)	M1	LHS oe isw
		= 50	A1	50 from correct processing of $2 - \lg 2$
		$3x^2 + x - 52 = 0 \rightarrow (3x + 13)(x - 4)$	M1	Solution of <i>their</i> three term quadratic Roots must be obtained from correct
		x = 4	A1	quadratic
		$x = -\frac{13}{3}$ discarded	A1	

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6 (i)	a = 3, b = 2, c = 4	B1B1B1	40.0
(ii)	$\frac{\mathrm{d}y}{\mathrm{d}x} = 8\cos 4x \text{ isw}$	M1 A1FT	$\pm k \cos cx$ and no other term in $x c \neq 1$ $bc \times \cos cx$ and no other term
(iii)	$x = \frac{\pi}{2} \to \frac{\mathrm{d}y}{\mathrm{d}x} = 8\cos 2\pi = 8$	DM1	Find <i>their</i> correct numerical $\frac{dy}{dx}$
	Eqn: $\frac{y-3}{x-\frac{\pi}{2}} = -\frac{1}{8} \qquad \left(\rightarrow y = -\frac{1}{8}x + 3.20 \right)$	M1	Find equation with <i>their</i> numerical normal gradient ie $\frac{-1}{\frac{dy}{dt}}$ and point
		A1	$ \begin{pmatrix} \frac{\pi}{2}, 3 \\ \text{All correct isw} \end{pmatrix} $
7 (i)	$\frac{h}{8} = \frac{6-r}{6} \to h = \frac{4}{3}(6-r)$	M1 A1	Uses correct ratio. Cannot be implied
(ii)	$V = \pi r^{2} h = \pi r^{2} \times \frac{4}{3} (6 - r)$ $= 8\pi r^{2} - \frac{4}{3} \pi r^{3}$	B1	AG all steps must be seen Penalise missing brackets at any point in working
(iii)	$\frac{\mathrm{d}V}{\mathrm{d}r} = 16\pi r - 4\pi r^2$	M1 A1	Differentiate at least one power reduced by one
	$\frac{\mathrm{d}V}{\mathrm{d}r} = 0 \to r = 4$	M1 A1	Attempt to solve – must get $r =$ Correct value of r . Ignore $r = 0$
	$V = \frac{128}{3}\pi \qquad (= 42.7\pi)$	A1	Correct value of V. Condone 134. $\frac{d^2V}{dr^2}$ must be correct and some
	$\frac{\mathrm{d}^2 V}{\mathrm{d}r^2} = 16\pi - 8\pi r < 0 \text{ when } r = 4 \rightarrow \max$	B1	dr^2 indication of a negative value seen plus maximum stated

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8 (i)	Gradient $AB = \frac{8-2}{9+3}$ $\left(=\frac{1}{2}\right)$ isw	B1	Syllabus P. M. N. S. N. S. Cloud. Co.
	Equation AB and $x = 0 \rightarrow \frac{y-2}{0+3} = \frac{1}{2} \qquad \left(\rightarrow y = \frac{1}{2}x + 3.5 \right)$	M1	Find equation with <i>their</i> gradient and set $x = 0$
	$\rightarrow y = 3.5$	A1	
(ii)	<i>D</i> is (3, 5)	B1	
(iii)	Gradient perpendicular = -2	M1	Use of $m_1 \times m_2 = -1$ on gradient used
	Equation perpendicular $\frac{y-5}{x-3} = -2$ $\rightarrow (y = -2x + 11)$	A1	for <i>their</i> line in (i)
(iv)	$E ext{ is } (0, 11)$	A1FT	
(v)	Area of $ABE = \frac{1}{2} \begin{vmatrix} -3 & 9 & 0 & -3 \\ 2 & 8 & 11 & 2 \end{vmatrix}$	M1	For area of <i>ABE</i> or <i>ECD</i> . $\frac{1}{2}$ and <i>their</i> correct 8 elements must be seen.
	$=\frac{1}{2} -24+99-18+33 =45$	A1	45 condone from $E(0, -4)$
	Area of $EDC = \frac{1}{2} \begin{vmatrix} 3 & 0 & 0 & 3 \\ 5 & 3.5 & 11 & 5 \end{vmatrix}$		
	$=\frac{1}{2} -10.5+33 =11.25$	A1	11.25 condone from <i>E</i> (0, –4)

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9 (i)	$\tan 2x = -\frac{5}{4}$	M1	Syllabus P. M.
	4 (2x = 128.7, 308.7)		$\tan 2x = \pm \frac{5}{4} \text{ or } \pm \frac{4}{5}$
			4 5resulting in $2x =$
	x = 64.3 awrt	A1	$\tan x = \dots$ gets M0
	154.3 awrt	A1FT	their $64.3^\circ + 90^\circ$
(ii)	$\csc^2 y + 3\csc y - 4 = 0$ or	B1	In any form as a three term quadratic.
	$4\sin^2 y - 3\sin y - 1 = 0$		
	$(\operatorname{cosec} y + 4)(\operatorname{cosec} y - 1) = 0$ or		
	$(4\sin y+1)(\sin y-1)=0$		
	$\sin y = -\frac{1}{4}$ or $\sin y = 1$	M1	Solve three term quadratic in $\operatorname{cosec} y$
			or sin y
	y = 194.5, 345.5, 90	A1A1A1	Answers must be obtained from the correct quadratic
(iii)	$z + \frac{\pi}{4} = \pi - \frac{\pi}{3}$ or	B1	Accept 2.09, 2.10, $\pi - 1.05$, $\pi - 1.04$ on
		B1	RHS. Could be implied by final answer Accept 4.19, 4.18, π +1.05, π +1.04 on
	$z + \frac{\pi}{4} = \pi + \frac{\pi}{3}$	DI	RHS. Could be implied by final answer
	$z = \frac{5\pi}{12}, \frac{13\pi}{12}$	B1B1	Answers must be correct multiples of π .
10 (i)	$s = \frac{1}{2}e^{2t} + 3e^{-2t} - t + (c)$	M1	Integrate : coefficient of $\frac{1}{2}$ or 3 seen
	2		with no change in powers of e. Ignore $-t$
	$t = 0, \ s = 0 \rightarrow c = -3.5$		
	$t = 0, \ s = 0 \to c = -3.5$ $\left(s = \frac{1}{2}e^{2t} + 3e^{-2t} - t - 3.5\right)$	A1 A1	All correct and simplified
(ii)	$v = 0 \rightarrow u^{2} - u - 6 = 0 \text{ oe}$ $(u - 3)(u + 2) = 0$ $\rightarrow u = 3 \rightarrow t = \frac{1}{2} \ln 3 \text{ or } 0.549$	M1	Obtain three term quadratic in u or e^{2t}
			Condone sign errors.
	(u-3)(u+2)=0	DM1	Solve three term quadratic
			-
	$\rightarrow u = s \rightarrow i = -\text{In } s \text{ or } 0.549$	A1	Accept 0.55 No second answer
(iii)	$t = \frac{1}{2} \ln 3 \rightarrow a = 2e^{2t} + 12e^{-2t}$ = 6 + 4 = 10	B1	Correct differentiation
	=6+4=10	B1	Allow awrt 10.0 or 9.99. No second
			answer.