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## **CAMBRIDGE INTERNATIONAL EXAMINATIONS**

**Cambridge Ordinary Level** 

## MARK SCHEME for the October/November 2014 series

## **4037 ADDITIONAL MATHEMATICS**

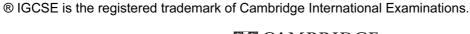
**4037/23** Paper 2, maximum raw mark 80

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge will not enter into discussions about these mark schemes.

Cambridge is publishing the mark schemes for the October/November 2014 series for most Cambridge IGCSE<sup>®</sup>, Cambridge International A and AS Level components and some Cambridge O Level components.





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1	(i) (ii)	f(2)=0 $\rightarrow$ 3(2) <sup>3</sup> +8(2) <sup>2</sup> -33(2)+ p=0 correct working to p = 10 AG method for quadratic factor f(x) = (x-2)(3x <sup>2</sup> +14x-5) f(x) = (x-2)(3x-1)(x+5)	M1 A1 M1 A1	factorise or solve quadratic factor = 0
		$f(x)=0 \rightarrow x=2, -5, \frac{1}{3}$	<b>A1</b>	
2	(i)	$^{12}C_{4} = 495$	B1	
	(ii)	${}^{7}C_{2} \times {}^{5}C_{2} = 21 \times 10$ = 210	M1 A1	
	(iii)	not K and B = ${}^{6}C_{2} \times {}^{4}C_{1} = 15 \times 4 = 60$ K and not B = ${}^{6}C_{1} \times {}^{4}C_{2} = 6 \times 6 = 36$ 60 + 36 96	B1 B1 M1 A1	
		OR K and B = ${}^{6}C_{1} \times {}^{4}C_{1} = 6 \times 4 = 24$ not K and not B = ${}^{6}C_{2} \times {}^{4}C_{2} = 15 \times 6 = 90$ $210 - 90 - 24$ $96$	B1 B1 M1 A1	
3	(i)	C is $(1, 6)D$ is $(1, 6)+(12, 9)= (13, 15)$	B1 M1 A1ft	
	(ii)	gradient of $CD = \frac{15-6}{13-1} \left( = \frac{3}{4} \right)$	B1ft	
		gradient of $AB = \frac{10-2}{-2-4} \left( = \frac{8}{-6} = \frac{-4}{3} \right)$	B1	
		$\frac{3}{4} \times \frac{-4}{3} = -1$ lines are perpendicular	B1	correct completion www
	(iii)	$area = \frac{1}{2} \times AB \times CD = \frac{1}{2} \times 10 \times 15$	M1	good attempt at two relevant lengths for $\frac{1}{2}$ base × height method
		=75 or array method	<b>A1</b>	

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4 (i)	$2000 = 1000e^{a+b} \rightarrow a+b = \ln 2$	B1			AD.COM
( <del>;;</del> )	2207 1000 2a-b	M1	substitution of	2 2205	

4	(i)	$2000 = 1000e^{a+b}  \to  a+b = \ln 2$	B1	
	(ii)	$3297 = 1000e^{2a-b} \rightarrow 2a+b$	M1	substitution of 2, 3297 and
		$= \ln 3.297$ oe	<b>A1</b>	rearrange
	(iii)	Solve for one value $a = 0.5$ and $b = 0.193$ or $0.19$	M1 A1	
	(iv)		M1 A1	
5	(i)	$\overrightarrow{OX} = \mu(a+b)$	B1	
	(ii)	$\overrightarrow{RP} = b - 3a$ or $\overrightarrow{RX} = \lambda(b - 3a)$ oe	B1	
		$\overrightarrow{OX} = 3a + \lambda (b - 3a)$	B1	
	(iii)	$\overrightarrow{OX} = \overrightarrow{OX}$ and equate both coefficients		
		$\mu = 3 - 3\lambda \qquad \mu = \lambda$ $\mu = \lambda = 0.75$	M1	
			<b>A1</b>	2
		$\frac{RX}{XP} = 3 \text{ or } 3:1$	A1ft	$\frac{\lambda}{1-\lambda}$
6	(i)	m=4	B1	
		equation of line is $\frac{\ln y - 39}{3^x - 9} = \frac{39 - 19}{9 - 4}$	M1	forms equation of line
		$ \ln y = 4(3^x) + 3 $	A1ft	ft only on their gradient
	(ii)	$x = 0.5 \rightarrow \ln y = 4\sqrt{3} + 3 = 9.928$	M1	correct expression for lny
		y = 20500	<b>A1</b>	
	(iii)	Substitutes y and rearrange for $3^x$ Solve $3^x = 1.150$ x = 0.127	M1 M1 A1	

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7	(i)	$x = \frac{2}{y} + 1  \to  y = \frac{2}{x - 1}$	M1	any valid method
		$f^{-1}(x) = \frac{2}{x - 1}$	A1	
	(ii)	$x = \frac{2}{y} + 1 \rightarrow y = \frac{2}{x - 1}$ $f^{-1}(x) = \frac{2}{x - 1}$ $gf(x) = \left(\frac{2}{x} + 1\right)^2 + 2$	B2/1/0	-1 each error
(ii	ii)	$fg(x) = \frac{2}{x^2 + 2} + 1$	B2/1/0	−1 each error
(i	iv)	$fg(x) = \frac{2}{x^2 + 2} + 1$ $ff(x) = \frac{2}{\frac{2}{x} + 1} + 1 = \frac{2x}{x + 2} + 1$ $= \frac{3x + 2}{x + 2}$ $\frac{3x + 2}{x + 2} = x \rightarrow x^2 - x - 2 = 0$	M1	correct starting expression
		$=\frac{3x+2}{x+2}$	A1	correct algebra to given answer
		$\frac{3x+2}{x+2} = x  \rightarrow  x^2 - x - 2 = 0$	M1	form and solve 3 term quadratic
		(x-2)(x+1) = 0 x = 2 only	A1	
8 (	(i)	$v = C + K\sin 2t \qquad C \neq 0$	M1	
		$v = 5 + 6\sin 2t$ $a = 12\cos 2t$	A1 A1ft	
(i	(ii)	$a = 0 \rightarrow \cos 2t = 0$ and solve	M1	set $a = 0$ and solve for $t$
		$t = \frac{\pi}{4}$ or 0.785 or 0.79	<b>A1</b>	
		$v = 5 + 6\sin\frac{\pi}{2} = 11$	A1ft	ft only on K
(ii		$v = 2 \rightarrow \sin 2t = -\frac{1}{2}$ and solve	M1	set $v = 2$ and solve for $t$
		$t = \frac{7\pi}{12}$ or $1.83 - 1.84$	<b>A1</b>	
		$t = \frac{7\pi}{12}$ or $1.83 - 1.84$ $a = 12\cos\frac{7\pi}{6} = -6\sqrt{3}$ or $-10.4$	<b>A1</b>	

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9 (i)	$\frac{\mathrm{d}y}{\mathrm{d}x} = 4 - \frac{1}{(x-2)^2}$	B1			od.com

9	(i)	$\frac{\mathrm{d}y}{\mathrm{d}x} = 4 - \frac{1}{\left(x - 2\right)^2}$	B1	
		$\frac{dy}{dx} = 0 \rightarrow (x-2)^2 = \frac{1}{4}$ $(4x^2 - 16x + 15 = 0)$	M1	solve 3 term quadratic from $\frac{dy}{dx} = 0$
		x = 2.5  or  1.5 y = 12  or  4	A1 A1	x values or 1 pair y values or 1 pair
		$\frac{d^2 y}{dx^2} = 2(x-2)^{-3}$	M1	use $\frac{d^2y}{dx^2}$ with solution from
		$x = 2.5 \rightarrow \frac{d^2 y}{dx^2} > 0 \rightarrow \text{minimum}$ $x = 1.5 \rightarrow \frac{d^2 y}{dx^2} < 0 \rightarrow \text{maximum}$	A1	$\frac{dy}{dx} = 0$ both identified www
	(ii)	$x=3 \rightarrow \frac{dy}{dx} = 3$ Use $m_1m_2 = -1$ for gradient normal from gradient tangent	B1 M1	must use numerical values
		Eqn of normal: $\frac{y-13}{x-3} = -\frac{1}{3}$	A1ft	
		Intersection of norm and curve $14 - \frac{x}{3} = 4x + \frac{1}{x-2}$	M1	equation and attempt to simplify
		$3x^{2} - 68x + 87 = 0$ $x = \frac{29}{13} \text{ or } 2.23$	DM1 A1	attempt to solve 3 term quadratic
		$x - \frac{13}{13}$ or 2.25	711	
10	(i)	LHS = $\frac{1 + \cos x + 1 - \cos x}{(1 - \cos x)(1 + \cos x)}$	B1	correct fraction
		$=\frac{2}{1-\cos^2 x}$	B1	correct evaluation
		$=\frac{2}{\sin^2 x} = RHS$	B1	use of $1-\cos^2 x = \sin^2 x$ and completion of fully correct proof
	(ii)	$2\csc^2 x = 8$	M1	identity used
		$\sin^2 x = \frac{1}{4}$	<b>A1</b>	
		$\sin x = \pm \frac{1}{2}$	<b>A1</b>	
		$x = 30^{\circ}, 150^{\circ}, 210^{\circ}, 330^{\circ}$	A1	