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## **CAMBRIDGE INTERNATIONAL EXAMINATIONS**

**Cambridge Ordinary Level** 

## MARK SCHEME for the October/November 2014 series

## **4037 ADDITIONAL MATHEMATICS**

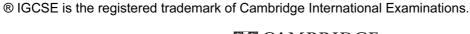
4037/22 Paper 2, maximum raw mark 80

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

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1 (a)		B1	
		B1	
(b)	No.in H only = $50 - x$ ; No in F only = $60 - x$ Sum: $50 - x + 60 - x + x + 30 - 2x = 98$ x = 14	B1 M1 A1	Both written or on diagram Add at least 3 terms each with <i>x</i> involved and equate to 98 soi
2	$9x^{2} + 2x - 1 < (x + 1)^{2}$ $8x^{2} < 2 \text{ oe isw}$ $-\frac{1}{2} < x < \frac{1}{2}$	M1 A1 A1	Expand and collect terms
3	$\log_2(x+3) = \log_2 y + 2 \rightarrow x + 3 = 4y$ $\log_2(x+y) = 3 \rightarrow x + y = 8$ $x+3 = 4(8-x)$ $5x = 29 \rightarrow x = 5.8, \text{ oe}$ $y = 2.2 \text{ oe}$	B1 B1 M1 A1 A1	Eliminate y or x from two linear three term equations

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4 (i)	$f(37) = 3 \text{ or } gf(x) = \frac{\sqrt{x-1} - 3 - 2}{2(\sqrt{x-1} - 3) - 3}$	B1		
	$gf(37) = \frac{3-2}{6-3} = \frac{1}{3}$	B1		
(ii)	$y = \sqrt{x-1} - 3 \rightarrow (y+3)^2 = x-1$	M1	Rearrange and square in any order	
	$(x+3)^2 + 1 = f^{-1}(x)$ oe isw	A1	Interchange <i>x</i> and <i>y</i> and complete	
(iii)	$y = \frac{x-2}{2x-3}$			
	$2xy - 3y = x - 2  \rightarrow  2xy - x = 3y - 2$	M1	Multiply and collect like terms	
	$\frac{3x-2}{2x-1} = g^{-1}(x)$ oe	A1	Interchange and complete Mark final answer	
5 (i)	B = 900	B1		
(ii)	$B = 500 + 400e^2 = 3455$ or 3456 or 3460	B1	3455.6 scores <b>B0</b>	
(iii)	$\left(\frac{\mathrm{d}B}{\mathrm{d}t} = \right)80\mathrm{e}^{0.2t}$	B1		
	$t = 10 \rightarrow \frac{\mathrm{d}B}{\mathrm{d}t} = 80\mathrm{e}^2 = 591(\mathrm{/day})$	B1	awrt	
(iv)	$10000 = 500 + 400e^{0.2t} \rightarrow e^{0.2t} = (23.75)$	M1	$e^{0.2t} = k$	
	$0.2t = \ln 23.75$	DM1	take logs: $0.2t = \ln k$	
	t = 15.8  (days)	A1	awrt	

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6 (i)	$(x+2)^2 + x^2 = 10$	B1	
	$x^{2} + 2x - 3 = 0 \rightarrow (x+3)(x-1) = 0$	M1	3 term quadratic with attempt to solve
	Points $(1, 3), (-3, -1)$ isw	A1	both x or a pair
	or elimination of x leads to $y^2 - 2y - 3 = 0$ , then as above	A1	both y or second pair
(ii)	$m^2x^2 + 10mx + 25 + x^2 = 10$	B1	
	$(m^2+1)x^2+10mx+15=0$		
	$b^2 - 4ac = (0) \rightarrow 100m^2 - 60(m^2 + 1) = 0$	M1 A1	attempt to use discriminant on three term quadratic. Allow unsimplified
	$m = \pm \sqrt{\frac{3}{2}}$ oe isw	<b>A1</b>	cao $\pm$ is required
	Alternative solution: $\frac{dy}{dx} = \frac{-x}{\sqrt{10 - x^2}} \text{ or } \frac{dy}{dx} = -\frac{x}{y}$	B1	allow unsimplified
	Result:		•
	$y^2 = x^2 + 5y$ after inserted in $y = mx + 5$ Attempt to solve with $x^2 + y^2 = 10$	M1	Eliminata
	Attempt to solve with $x + y = 10$ $y = 2, x = \pm \sqrt{6}$	A1	Eliminate <i>x</i> or <i>y</i> both
		A1	Cotti
	$m = \pm \frac{3}{\sqrt{6}}$ oe		
7 (i)	$v = 2\cos t + 1$	B1	mark final answer
(ii)	$2\cos t + 1 = 0$	M1	equate their <i>v</i> to zero (must be a differential) and attempt to solve to find
	$t = \frac{2\pi}{3} \text{ or } 2.09$	A1	an <b>angle</b> awrt
(iii)	$t = \frac{2\pi}{3} \rightarrow x = 2\sin\left(\frac{2\pi}{3}\right) + \frac{2\pi}{3} = 3.83 \mathrm{m}$	B1	awrt
	$a = -2\sin t$	B1ft	ft <i>their</i> v (2 <sup>nd</sup> differential)
	$t = \frac{2\pi}{3}a = -\sqrt{3} = -\frac{1.73}{4} \text{ms}^{-2}$	DB1ft	ft using their <b>angle</b> t in correct a awrt
8 (i)	$\frac{dy}{dx} = \frac{(2+x^2) \times 2x - x^2 \times 2x}{(2+x^2)^2} = \frac{4x}{(2+x^2)^2}$	M1 A1	apply quotient or product rule unsimplified
	k=4	<b>A1</b>	k=4 does not need to be specifically
(ii)	$\int \frac{x}{(2+x^2)^2} dx = \frac{1}{4} \times \frac{x^2}{2+x^2} + (c) \text{ isw}$	B1 B1	identified $\frac{1}{their  k} \times \text{ original function}$

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9	$(a+3\sqrt{5})^2 = a^2 + 3\sqrt{5}a + 3\sqrt{5}a + 45$ oe	B1	anywhere
	Equate: $a^2 + a + 45 = 51$	B1	
	and $6a - b = 0$	B1	
	(a+3)(a-2)=0	M1	Attempt to solve three term quadratic with integer coefficients obtained by
	a = -3, 2 b = -18, 12	A1 A1	equating coeffs Both as correct or one correct pair Both bs correct
10 (i)	$\sec x \csc x = \frac{1}{\cos x \sin x}$	B1	anywhere
	$\cot x = \frac{\cos x}{\sin x}$	<b>B</b> 1	anywhere
	LHS = $\frac{1 - \cos^2 x}{\cos x \sin x}$ oe	B1ft	correct addition of their terms
	$= \frac{\sin^2 x}{\cos x \sin x} = \tan x \qquad \text{AG}$	B1	use of identity and cancel
(ii)	$3\cot x - \cot x = \tan x  \to  2\cot x = \tan x$	M1	equate and collect like terms, allow sign errors
	$\tan^2 x = 2$ oe x = 54.7, 125.3, 234.7, 305.3	A1 A1 A1	2 values only 2 more values. awrt
11 (i)	Area of sector = $\frac{1}{2} \times x^2 \times 0.8 = 0.4x^2 \text{ cm}^2$	B1	anywhere
	$SR = 5\sin 0.8 (= 3.59)$ or	<b>B</b> 1	SR may be seen in stated $\frac{1}{2}ab\sin C$
	$OR = 5\cos 0.8 (= 3.48)$		2
	Area of triangle =		
	$\frac{1}{2}5\cos 0.8 \times 5\sin 0.8 = 6.247 \text{cm}^2$	M1 A1	insert correct terms into correct area formulae
	$0.08x^2 = 6.247$		Tormulae
	x = 8.837 cm AG	A1	
(ii)	SQ = 8.84 - 5 (= 3.84  cm)		
()	$PR = 8.84 - 5\cos 0.8 (= 5.35 \text{ or } 5.36\text{cm})$	B1	two lengths from SQ, PR, PQ awrt
	$PQ = 8.84 \times 0.8 (= 7.07 \text{ cm})$	B1	third length awrt
	Perimeter = 19.84 to 19.86 cm or rounded to 19.8 or 19.9	B1	sum
(iii)	Area $PQSR = 4 \times 6.247$	M1	
	$= 25 \mathrm{cm}^2$	A1	24.95 to 25
			13 = 2

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12 (i)	$f(2) = 3(2^3) - 14(2^2) + 32 = 0$ Or complete long division	B1	
(ii)	$f(x) = (x-2)(3x^2 - 8x - 16)$ $f(x) = (x-2)(x-4)(3x+4)$	M1 A1 M1 A1	$3x^2$ and 16 8x and correct signs Factorise three term quadratic
(iii)	x = 2, 4	B1	
(iv)	$\int 3x - 14 + \frac{32}{x^2} dx = 1.5x^2 - 14x - \frac{32}{x} (+ c)$ $Area = \left[ 1.5x^2 - 14x - \frac{32}{x} \right]_2^4$ $= (-) 2$	B1 B1 M1 A1	first 2 terms third term correct unsimplified  Limits of 2 and 4 and subtract