



## 1. ALGEBRA

### Quadratic Equation

For the equation  $ax^2 + bx + c = 0$ ,

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} .$$

### Binomial Theorem

$$(a + b)^n = a^n + \binom{n}{1} a^{n-1} b + \binom{n}{2} a^{n-2} b^2 + \dots + \binom{n}{r} a^{n-r} b^r + \dots + b^n,$$

where  $n$  is a positive integer and  $\binom{n}{r} = \frac{n!}{(n-r)!r!}$ .

## 2. TRIGONOMETRY

### Identities

$$\sin^2 A + \cos^2 A = 1$$

$$\sec^2 A = 1 + \tan^2 A$$

$$\operatorname{cosec}^2 A = 1 + \cot^2 A$$

### Formulae for $\Delta ABC$

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$a^2 = b^2 + c^2 - 2bc \cos A$$

$$\Delta = \frac{1}{2} bc \sin A$$

- 1 Show that  $\sec x - \cos x = \sin x \tan x$ . [3]
- 2 A 4-digit number is formed by using four of the seven digits 2, 3, 4, 5, 6, 7 and 8. No digit can be used more than once in any one number. Find how many different 4-digit numbers can be formed if
- (i) there are no restrictions, [2]
- (ii) the number is even. [2]
- 3 The line  $y = mx + 2$  is a tangent to the curve  $y = x^2 + 12x + 18$ . Find the possible values of  $m$ . [4]
- 4 The remainder when the expression  $x^3 + kx^2 - 5x - 3$  is divided by  $x - 2$  is 5 times the remainder when the expression is divided by  $x + 1$ . Find the value of  $k$ . [4]
- 5 Solve the simultaneous equations
- $$\log_3 a = 2 \log_3 b,$$
- $$\log_3 (2a - b) = 1. \quad [5]$$
- 6 Solve the equation  $3x^3 + 7x^2 - 22x - 8 = 0$ . [6]
- 7 (i) Sketch the graph of  $y = |3x - 5|$ , for  $-2 \leq x \leq 3$ , showing the coordinates of the points where the graph meets the axes. [3]
- (ii) On the same diagram, sketch the graph of  $y = 8x$ . [1]
- (iii) Solve the equation  $8x = |3x - 5|$ . [3]
- 8 (a) A function  $f$  is defined, for  $x \in \mathbb{R}$ , by
- $$f(x) = x^2 + 4x - 6.$$
- (i) Find the least value of  $f(x)$  and the value of  $x$  for which it occurs. [2]
- (ii) Hence write down a suitable domain for  $f(x)$  in order that  $f^{-1}(x)$  exists. [1]
- (b) Functions  $g$  and  $h$  are defined, for  $x \in \mathbb{R}$ , by
- $$g(x) = \frac{x}{2} - 1,$$
- $$h(x) = x^2 - x.$$
- (i) Find  $g^{-1}(x)$ . [2]
- (ii) Solve  $gh(x) = g^{-1}(x)$ . [3]

- 9 (a) Find  $\int (x^{\frac{1}{3}} - 3)^2 dx$ . [3]
- (b) (i) Given that  $y = x \sqrt{x^2 + 6}$ , find  $\frac{dy}{dx}$ . [3]
- (ii) Hence find  $\int \frac{x^2 + 3}{\sqrt{x^2 + 6}} dx$ . [2]

10 A particle travels in a straight line so that,  $t$  s after passing through a fixed point  $O$ , its displacement  $s$  m from  $O$  is given by  $s = \ln(t^2 + 1)$ .

- (i) Find the value of  $t$  when  $s = 5$ . [2]
- (ii) Find the distance travelled by the particle during the third second. [2]
- (iii) Show that, when  $t = 2$ , the velocity of the particle is  $0.8 \text{ ms}^{-1}$ . [2]
- (iv) Find the acceleration of the particle when  $t = 2$ . [3]

11 Solve the equation

- (i)  $3 \sin x - 4 \cos x = 0$ , for  $0^\circ \leq x \leq 360^\circ$ , [3]
- (ii)  $11 \sin y + 1 = 4 \cos^2 y$ , for  $0^\circ \leq y \leq 360^\circ$ , [4]
- (iii)  $\sec\left(2z + \frac{\pi}{3}\right) = -2$ , for  $0 \leq z \leq \pi$  radians. [4]

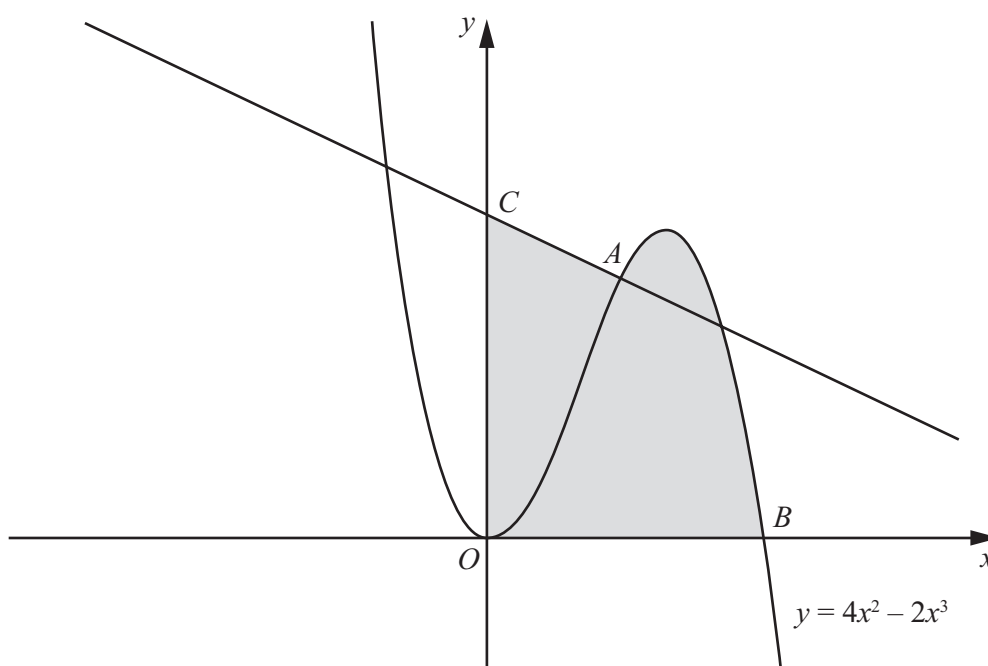
12 Answer only **one** of the following two alternatives.

**EITHER**

A curve has the equation  $y = A \sin 2x + B \cos 3x$ . The curve passes through the point with coordinates  $\left(\frac{\pi}{12}, 3\right)$  and has a gradient of  $-4$  when  $x = \frac{\pi}{3}$ .

- (i) Show that  $A = 4$  and find the value of  $B$ . [6]
- (ii) Given that, for  $0 \leq x \leq \frac{\pi}{3}$ , the curve lies above the  $x$ -axis, find the area of the region enclosed by the curve, the  $y$ -axis and the line  $x = \frac{\pi}{3}$ . [5]

**OR**



The diagram shows the curve  $y = 4x^2 - 2x^3$ . The point  $A$  lies on the curve and the  $x$ -coordinate of  $A$  is 1. The curve crosses the  $x$ -axis at the point  $B$ . The normal to the curve at the point  $A$  crosses the  $y$ -axis at the point  $C$ .

- (i) Show that the coordinates of  $C$  are  $(0, 2.5)$ . [5]
- (ii) Find the area of the shaded region. [6]





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