

MARK SCHEME for the October/November 2010 question paper

for the guidance of teachers

4037 ADDITIONAL MATHEMATICS

4037/12

Paper 1, maximum raw mark 80

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes must be read in conjunction with the question papers and the report on the examination.

• CIE will not enter into discussions or correspondence in connection with these mark schemes.

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Mark Scheme Notes

Marks are of the following three types:

- M Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the M mark and in some cases an M mark can be implied from a correct answer.
- A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).
- B Accuracy mark for a correct result or statement independent of method marks.
- When a part of a question has two or more "method" steps, the M marks are generally independent unless the scheme specifically says otherwise; and similarly when there are several B marks allocated. The notation DM or DB (or dep*) is used to indicate that a particular M or B mark is dependent on an earlier M or B (asterisked) mark in the scheme. When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.
- The symbol √ implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A or B marks are given for correct work only. A and B marks are not given for fortuitously "correct" answers or results obtained from incorrect working.
- Note: B2 or A2 means that the candidate can earn 2 or 0.
 B2, 1, 0 means that the candidate can earn anything from 0 to 2.

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The follo	wing abbreviations may be used in a mark scheme or use	ed on the scripts:	12 Iscioud.com
AG	Answer Given on the question paper (so extra checkin	g is needed to e	ensure that

- AG Answer Given on the question paper (so extra checking is needed to ensure that the detailed working leading to the result is valid)
- BOD Benefit of Doubt (allowed when the validity of a solution may not be absolutely clear)
- CAO Correct Answer Only (emphasising that no "follow through" from a previous error is allowed)
- ISW Ignore Subsequent Working
- MR Misread
- PA Premature Approximation (resulting in basically correct work that is insufficiently accurate)
- SOS See Other Solution (the candidate makes a better attempt at the same question)

Penalties

- MR –1 A penalty of MR –1 is deducted from A or B marks when the data of a question or part question are genuinely misread and the object and difficulty of the question remain unaltered. In this case all A and B marks then become "follow through $\sqrt{$ ". marks. MR is not applied when the candidate misreads his own figures - this is regarded as an error in accuracy.
- OW –1,2 This is deducted from A or B marks when essential working is omitted.
- PA –1 This is deducted from A or B marks in the case of premature approximation.
- S –1 Occasionally used for persistent slackness – usually discussed at a meeting.
- EX –1 Applied to A or B marks when extra solutions are offered to a particular equation. Again, this is usually discussed at the meeting.

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(i) $a = -12$,		=-4	B1, B1 [2]	B1 for each		Mun My	
	(ii) -4		√ B1 [1]	Follow t	through on their y	value	
2	(i) Graphs		B1 B1 [2]	B1 for a	one correct curve a second correct cu e first curve	rve consistent	
	(ii) 3		√ B1 [1]	Follow through on number of clear point of intersection			
;	$\frac{\cos x (1 + \sin x)}{1 - s}$ $\frac{2 \cos x}{\cos^2 x}$ $2 \sec x$	$\frac{+\cos x(1-\sin x)}{\sin^2 x}$	M1 DM1 M1 A1 [4]	M1 for attempt to get in terms of a sin fraction DM1 simplifying numerator M1 simplifying denominator 4]			
•	Either (x or (x or (2	$(x-7)(2x^{2}+3x+1) (2x+1)(x^{2}-6x-7)$		DM1 for factor A1 corre	attempt to find a ro r attempt to obtain ect quadratic facto tempt to factorise o	ı quadratic r	
;	(i) $a = \pi + \frac{\pi}{3}$	$a = \frac{4\pi}{3}$	B1 [1]				
	(ii) $\frac{\mathrm{d}y}{\mathrm{d}x} = 2x\mathrm{c}$		M1, A1	M1 for a	attempt to differen	tiate a product	
	uл	$= 2, \Rightarrow \text{grad of normal} = -\frac{1}{2}$ $= -\frac{4\pi}{3} = -\frac{1}{2} \left(x - \frac{\pi}{2} \right)$	M1	M1 for <i>i</i> different	$m_1m_2 = -1$, must h tiation	ave used	
	$\left(2y = \frac{19\pi}{6}\right)$	$\left(\frac{\tau}{2}-x\right)$	M1, A1 [5]		attempt at a norma ed differentiation, ified		

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(i)) 64-960	$0x + 6000x^2$	B1, B1, B1 [3]	B1 for ea	ach correct term, a	Pap nymath 12 allow 2 ⁶
(ii	i) 1 × (their	$x \text{ term}$) + $\frac{10}{2}$ × (their 64)	M1	M1 for 2		
	-960 + 3 = -640	20	B1 A1 [3]	B1 for $\frac{1}{2}$	$\frac{0}{2}$ or 5	
(a	a) (i) $x = 2$	30°, 150°	B1, B1 [2]	B1 for ea	ach	
	x = 1	30° = 120°, 240° 150°, 270° B = {30°, 150°, 270°}	B1 √B1		= 150° , 270° only hrough on their A	
			[2]			
(b	,	± 1 or $\tan 3x = 0$	M1	M1 for d	lealing with sec as	nd $3x$
		180°, 360°, 540°)°, 120°, 180°	A1 √B1 [3]		ll solutions correc hrough on their n s	
(i)	Use of rails $\ln y = 6.8$	$n x + \ln A$	M1 M1 A1 B1 M1 A1, A1 [7]	M1 for a A1 for ln B1 for ln M1 for u	$\int y = b \ln x + \ln A$	
(i)	$A = x^2,$	$\Rightarrow \frac{\mathrm{d}A}{\mathrm{d}x} = 2x$	B1 [1]			
(ii		$=5, \frac{\mathrm{d}A}{\mathrm{d}x}=10$	$\sqrt{B1}$	Follow t	hrough on their $\frac{c}{c}$	$\frac{ A }{ x }$
	$\frac{\mathrm{d}x}{\mathrm{d}t} = \frac{0.0}{1}$	$\frac{100}{0}$	M1	M1 for 0	0.003 ÷ their 10	
	= 0.0003		A1 [3]			
(ii	$V = 4x^3,$		B1, B1	B1 for ea	ach	
	$\frac{\mathrm{d}v}{\mathrm{d}t} = 12.$	$x^2 \times 0.0003$	M1			
	= 0.09		A1			
			[4]			

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10	(i)	0 1	$\frac{4}{P_A}$, $PA = 4\sqrt{3}$	B1	B1 for P	A (answer given)	WWW. MUM Pap 12	- TOUD COM
		$PB = \frac{4}{\sin^2}$	$\frac{\pi}{6}$ + 4, <i>PB</i> = 12	B1	B1 for <i>P</i>	B (answer given)		
			o ivalent methods	[2]				
			$ea = \frac{1}{2}12^2 \times \frac{\pi}{3}$	$\sqrt{\mathbf{B}1}$	$\sqrt{B1}$ sec	etor area, ft on the	eir PB	
		Area of k	ite = $2 \times \frac{1}{2} \times 4\sqrt{3} \times 4$	M1, A1		ttempt to find are ate triangle	ea of kite or	
		Shaded an	rea = 47.7	A1 [4]	TT T			
	(iii)	$P = \left(12 \times \right)$	$\left(\frac{\pi}{3}\right) + 2\left(12 - 4\sqrt{3}\right) + 2(4)$	B1, B1, B1	B1 for each	ach of the 3 terms	8	
		= 30.7		B1 [4]	B1 for fi	nal answer		
11	(i)	$2(1+x)^{\frac{1}{2}}($	(+c)	M1, A1 [2]	M1 for	$(1+x)^{\frac{1}{2}}$, A1 for 2		
	(ii)	$\frac{\mathrm{d}y}{\mathrm{d}x} = \frac{2\sqrt{1}}{2}$	$\frac{1}{1+x} - 2x \frac{1}{2} (1+x)^{-\frac{1}{2}}}{1+x}$	M1 A2, 1, 0	M1 atter -1 each	npt at differentiat error	ion	
		$=\frac{2}{\left(\sqrt{1+y}\right)}$	$\left(\overline{x}\right)^{-} \overline{\left(\sqrt{1+x}\right)^{3}}$	A1 [4]	A1 all co	orrect		
	(iii)	($\int_{3}^{3} dx = \int \frac{2}{\left(\sqrt{1+x}\right)} dx - \frac{2x}{\sqrt{1+x}}$	M1	M1 for i	dea of using (ii) '	in reverse'	
		$=4\sqrt{1+x}$	$\frac{1}{\sqrt{1+x}}(+c)$	A1	A1 all co	orrect		
		$\int_0^3 \frac{x}{\left(\sqrt{1+x}\right)^3}$	$\frac{1}{\sqrt{x}} dx = (8-3) - (4), = 1$	M1, A1	M1 for a	ttempt evaluation	1	
		·		[4]				

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	-9x(+c) = 3, y = 1, so c = -8 0, leads to x = ±1.5	M1, A1 M1, A1 [4] M1	M1 for a	attempt to integrate the definition of the defi	
(iii) Midpoin Gradient	.5, -17), (-1.5, 1) t AB: (0, -8) of AB = -6, perp grad = $\frac{1}{6}$: $x - 6y = 48$	A1, A1 [3] M1 M1 M1, A1 [4]	M1 for a	ach pair attempt to find mic attempt to find gra t be working with	d of perp
-20 = 2A	$4e^{2x} - Be^{-x}$	B1 M1 A1 DM1 A1 [5]	A1 all co	attempt to differen orrect r attempt to solve	
$e^{3x} = 2$	$e^{2x} - 40e^{-x}$, $20e^{2x} = 40e^{-x}$ 2 or 0.231	M1 M1 M1 A1 [4]	solution M1 for c	equating to zero ar lealing with expor attempt to obtain <i>x</i> oth	nentials
<u>u</u> n	$40e^{2x} + 40e^{-x}$ +ve, so min	M1 A1 [2]	other va	attempt at second o lid method correct conclusio	