

## MARK SCHEME for the October/November 2010 question paper

### for the guidance of teachers

# **4037 ADDITIONAL MATHEMATICS**

4037/11

Paper 1, maximum raw mark 80

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes must be read in conjunction with the question papers and the report on the examination.

• CIE will not enter into discussions or correspondence in connection with these mark schemes.

CIE is publishing the mark schemes for the October/November 2010 question papers for most IGCSE, GCE Advanced Level and Advanced Subsidiary Level syllabuses and some Ordinary Level syllabuses.



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#### Mark Scheme Notes

Marks are of the following three types:

- M Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the M mark and in some cases an M mark can be implied from a correct answer.
- A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).
- B Accuracy mark for a correct result or statement independent of method marks.
- When a part of a question has two or more "method" steps, the M marks are generally independent unless the scheme specifically says otherwise; and similarly when there are several B marks allocated. The notation DM or DB (or dep\*) is used to indicate that a particular M or B mark is dependent on an earlier M or B (asterisked) mark in the scheme. When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.
- The symbol √ implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A or B marks are given for correct work only. A and B marks are not given for fortuitously "correct" answers or results obtained from incorrect working.
- Note: B2 or A2 means that the candidate can earn 2 or 0.
  B2, 1, 0 means that the candidate can earn anything from 0 to 2.

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The follo	wing abbreviations may be used in a mark scheme or use	ed on the scripts:	II IISCIOUD.COM
AG	Answer Given on the question paper (so extra checkin	g is needed to e	nsure that

- AG Answer Given on the question paper (so extra checking is needed to ensure that the detailed working leading to the result is valid)
- BOD Benefit of Doubt (allowed when the validity of a solution may not be absolutely clear)
- CAO Correct Answer Only (emphasising that no "follow through" from a previous error is allowed)
- ISW Ignore Subsequent Working
- MR Misread
- PA Premature Approximation (resulting in basically correct work that is insufficiently accurate)
- SOS See Other Solution (the candidate makes a better attempt at the same question)

### **Penalties**

- MR –1 A penalty of MR –1 is deducted from A or B marks when the data of a question or part question are genuinely misread and the object and difficulty of the question remain unaltered. In this case all A and B marks then become "follow through  $\sqrt{$ ". marks. MR is not applied when the candidate misreads his own figures - this is regarded as an error in accuracy.
- OW –1,2 This is deducted from A or B marks when essential working is omitted.
- PA –1 This is deducted from A or B marks in the case of premature approximation.
- S –1 Occasionally used for persistent slackness – usually discussed at a meeting.
- EX –1 Applied to A or B marks when extra solutions are offered to a particular equation. Again, this is usually discussed at the meeting.

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	Page 4	Mark Scheme: Tead	chers' version		Syllabus	Papty	
	<b>v</b>	GCE O LEVEL – Octobe		010	4037	11 913	
	(i) $a = -12, b$	<b>i)</b> $a = -12, b = -4$		B1 for each			
	(ii) -4		√B1 [1]	Follow 1	hrough on their y	value	
	(i) Graphs		B1 B1 [2]	B1 for a	ne correct curve second correct cu first curve	rve consistent	
	(ii) 3		√ B1 [1]	Follow through on number of clear point of intersection			
3	$\frac{\cos x(1+\sin x)}{1-s}$ $\frac{2\cos x}{\cos^2 x}$ $2\sec x$	$+\cos x(1-\sin x)$ $\sin^2 x$	M1 M1 for attempt to get in terms of a sin fraction DM1 DM1 simplifying numerator M1 M1 simplifying denominator A1 [4]			tor	
	$x = -1 \text{ or } 7 \text{ or } -\frac{1}{2} \text{ seen}$ Either $(x+1)(2x^2 - 13x - 7)$ or $(x-7)(2x^2 + 3x + 1)$ or $(2x+1)(x^2 - 6x - 7)$ leading to $(x+1)(x-7)(2x+1)$		M1 DM1 A1 DM1, A1 [5]	DM1 fo factor A1 corre	attempt to find a ro r attempt to obtain ect quadratic facto cempt to factorise	ı quadratic r	
5	(i) $a = \pi + \frac{\pi}{3}$	$a = \frac{4\pi}{3}$	B1 [1]	Must be	in terms of $\pi$		
	(ii) $\frac{\mathrm{d}y}{\mathrm{d}x} = 2x\mathrm{co}$	_	M1, A1	M1 for a	attempt to differen	tiate a product	
	uл	$x = 2, \Rightarrow$ grad of normal = $-\frac{1}{2}$ $-\frac{4\pi}{3} = -\frac{1}{2}\left(x - \frac{\pi}{2}\right)$	M1	M1 for $m_1m_2 = -1$ , must have used differentiation			
	$\left(2y = \frac{19\pi}{6}\right)$	$\left(\frac{x}{x}-x\right)$	M1, A1 [5]		attempt at a normated differentiation, ified		

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5 (	(i) 64-960	$0x + 6000x^2$	B1, B1, B1 [3]	B1 for ea	ach correct term, a	May My Math
	(ii) 1 × (their	$r x \text{ term}$ ) + $\frac{10}{2}$ × (their 64)	M1	M1 for 2		
	-960 + 3 = -640	20	B1 A1 [3]	B1 for $\frac{1}{2}$	$\frac{0}{2}$ or 5	
7 (	(a) (i) $x = 2$	30°, 150°	B1, B1 [2]	B1 for ea	ach	
	x = 1	$30^{\circ} = 120^{\circ}, 240^{\circ}$ $150^{\circ}, 270^{\circ}$ $B = \{30^{\circ}, 150^{\circ}, 270^{\circ}\}$	$\begin{array}{c} \mathbf{B1} \\ \sqrt{\mathbf{B1}} \end{array}$		= $150^\circ$ , $270^\circ$ only hrough on their A	
		()	[2]			
(	$3x = 0^{\circ},$	$\pm 1$ or $\tan 3x = 0$ 180°, 360°, 540°	M1		ealing with sec an	
	$x = 0^{\circ}, 60$ $n(C) = 4$	0°, 120°, 180°	A1 √B1 [3]		Il solutions correc hrough on their n	
	Use of raising $\ln y = 6.8$ $\ln y = b \ 1$ $A = e^{(\text{their})}$	n x + ln A	M1 M1 A1 B1 M1 A1, A1 [7]	M1 for a A1 for ln B1 for ln M1 for u	$y = b \ln x + \ln A$	
) (	$(i)  A = x^2,$	$\Rightarrow \frac{\mathrm{d}A}{\mathrm{d}x} = 2x$	B1 [1]			
(	(ii) When $x =$		$\sqrt{B1}$	Follow tl	hrough on their $\frac{d}{d}$	$\frac{A}{ x }$
	$\frac{\mathrm{d}x}{\mathrm{d}t} = \frac{0.0}{1}$ $= 0.0003$		M1 A1 [3]	M1 for 0	.003 ÷ their 10	
	(iii) $V = 4x^3$ ,	$\frac{\mathrm{d}V}{\mathrm{d}x} = 12x^2$	B1, B1	B1 for ea	ach	
	$\frac{\mathrm{d}V}{\mathrm{d}t} = 12$	$x^2 \times 0.0003$	M1			
	= 0.09		A1 [4]			

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10	(i)	0 1	$\frac{4}{PA}$ , $PA = 4\sqrt{3}$	B1	B1 for <i>P</i>	PA (answer given)	Pap nymain	SUD.COM
		$PB = \frac{4}{\sin^2}$	$\frac{\pi}{6}$ + 4, <i>PB</i> = 12	B1	B1 for F	<i>B</i> (answer given)		
			o ivalent methods	[2]				
	(ii)		$ea = \frac{1}{2}12^2 \times \frac{\pi}{3}$	√ B1	√B1 sec	ctor area, ft on thei	r PB	
		Area of k	ite = $2 \times \frac{1}{2} \times 4\sqrt{3} \times 4$	M1, A1		attempt to find area ate triangle	a of kite or	
		Shaded an	rea = 47.7	A1 [4]	appropri	are triangre		
	(iii)	$P = \left(12 \times \right)$	$\left(\frac{\pi}{3}\right) + 2\left(12 - 4\sqrt{3}\right) + 2(4)$	B1, B1, B1	B1 for e	ach of the 3 terms		
		= 30.7		B1 [4]	B1 for f	nal answer		
11	(i)	$2(1+x)^{\frac{1}{2}}($	+c)	M1, A1 [2]	M1 for(	$(1+x)^{\frac{1}{2}}$ , A1 for 2		
	(ii)	$\frac{\mathrm{d}y}{\mathrm{d}x} = \frac{2\sqrt{1}}{2}$	$\frac{1}{x} + \frac{1}{2} x - 2x \frac{1}{2} (1 + x)^{-\frac{1}{2}}}{1 + x}$	M1 A2, 1, 0	M1 atter –1 each	npt at differentiati error	on	
		$=\frac{2}{\left(\sqrt{1+x}\right)}$	$\left(\frac{x}{\sqrt{1+x}}\right)^{-} \frac{x}{\left(\sqrt{1+x}\right)^{3}}$	A1 [4]	A1 all c	orrect		
	(iii)	<b>`</b>	$\int_{\frac{3}{2}}^{3} dx = \int \frac{2}{\left(\sqrt{1+x}\right)} dx - \frac{2x}{\sqrt{1+x}}$	M1	M1 for i	dea of using (ii) 'i	n reverse'	
		$=4\sqrt{1+x}$	$-\frac{2x}{\sqrt{1+x}}(+c)$	A1	A1 all co	orrect		
		$\int_0^3 \frac{x}{\left(\sqrt{1+x}\right)^3}$	$\frac{1}{c^{3}} dx = (8-3) - (4), = 1$	M1, A1	M1 for a	attempt evaluation		
		`	·	[4]				

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(ii) $4x^2 - 9 =$	-9x(+c) = 3, y = 1, so c = -8 0, leads to x = ±1.5 .5, -17), (-1.5, 1)	M1, A1 M1, A1 [4] M1 A1, A1 [3]	M1 for a	attempt to integrate the solve $\frac{d}{d}$ ach pair	
	t AB: $(0, -8)$ of AB = -6, perp grad = $\frac{1}{6}$ : $x - 6y = 48$	M1 M1 M1, A1 [4]	M1 for a	attempt to find mid attempt to find gra t be working with	d of perp
-20 = 2A	$4e^{2x} - Be^{-x}$	B1 M1 A1 DM1 A1 [5]	A1 all co	attempt to differen orrect r attempt to solve	
(ii) $\frac{dy}{dx} = 20e^{2x} - 40e^{-x}, \ 20e^{2x} = 40e^{-x}$ $e^{3x} = 2$ $x = \frac{1}{3}\ln 2 \text{ or } 0.231$ y = 47.6		M1 M1 M1 A1 [4]	solution M1 for c	equating to zero ar lealing with expor attempt to obtain <i>x</i> oth	nentials
<b>u</b> A	$40e^{2x} + 40e^{-x}$ +ve, so min	M1 A1 [2]	other va	attempt at second o lid method correct conclusio	