



Cambridge O Level

CANDIDATE NAME					
CENTRE NUMBER		CANDIDATE NUMBER			
ADDITIONAL MATHEMATICS 4037/22					
Paper 2		May/June 2021			
		2 hours			
You must answ	ver on the question paper.				

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No additional materials are needed.

INSTRUCTIONS

- Answer **all** questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do **not** use an erasable pen or correction fluid.
- Do **not** write on any bar codes.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.

INFORMATION

- The total mark for this paper is 80.
- The number of marks for each question or part question is shown in brackets [].

This document has 16 pages.



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Mathematical Formulae

1. ALGEBRA

Quadratic Equation

For the equation $ax^2 + bx + c = 0$,

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Binomial Theorem

$$(a+b)^{n} = a^{n} + \binom{n}{1}a^{n-1}b + \binom{n}{2}a^{n-2}b^{2} + \dots + \binom{n}{r}a^{n-r}b^{r} + \dots + b^{n}$$

where *n* is a positive integer and $\binom{n}{r} = \frac{n!}{(n-r)!r!}$

Arithmetic series
$$u_n = a + (n-1)d$$

 $S_n = \frac{1}{2}n(a+l) = \frac{1}{2}n\{2a + (n-1)d\}$

Geometric series

$$u_{n} = ar^{n-1}$$

$$S_{n} = \frac{a(1-r^{n})}{1-r} \ (r \neq 1)$$

$$S_{\infty} = \frac{a}{1-r} \ (|r| < 1)$$

2. TRIGONOMETRY

Identities

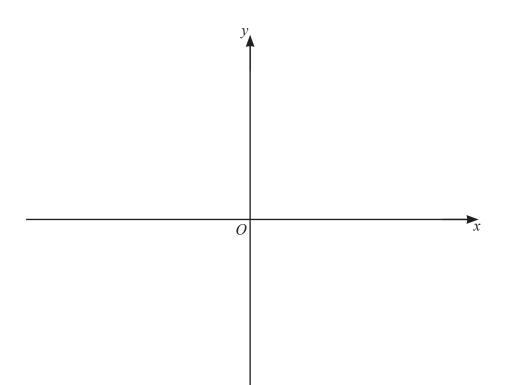
$$\sin^2 A + \cos^2 A = 1$$
$$\sec^2 A = 1 + \tan^2 A$$
$$\csc^2 A = 1 + \cot^2 A$$

Formulae for $\triangle ABC$

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$
$$a^2 = b^2 + c^2 - 2bc \cos A$$
$$\Delta = \frac{1}{2}bc \sin A$$

1 Using the binomial theorem, expand $(1+e^{2x})^4$, simplifying each term.

2 On the axes, sketch the graph of y = 3(x-3)(x-1)(x+2) stating the intercepts with the coordinate axes. [3]



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[2]

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3	Find the values of the constant <i>k</i> for which	$(2k-1)x^2 + 6x + k + 1 = 0$	has real roots.	[5]
•		(211 1)11 1 011 11 0	1145 1 0 41 10005.	[-]

4 The polynomial $p(x) = mx^3 - 29x^2 + 39x + n$, where *m* and *n* are constants, has a factor 3x - 1, and remainder 6 when divided by x - 1. Show that x - 2 is a factor of p(x). [6]

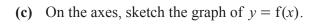
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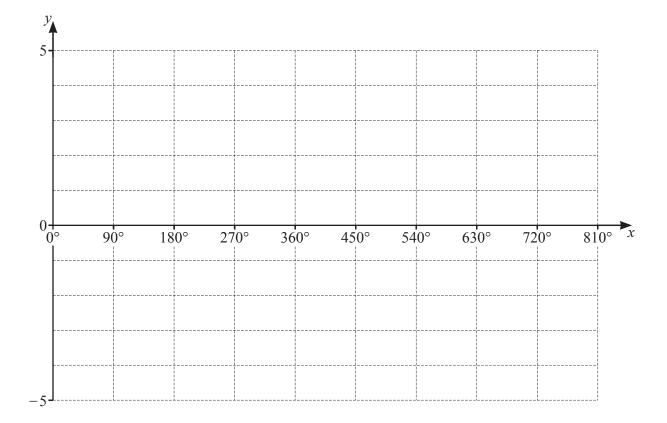
(a) Write down the amplitude of f.

The function f is defined, for $0^{\circ} \le x \le 810^{\circ}$, by $f(x) = -2 + \cos \frac{2x}{3}$.

(b) Find the period of f.

5





[1]

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[2]

[2]

6 The points A(5, -4) and C(11, 6) are such that AC is the diagonal of a square, ABCD.

(a) Find the length of the line AC.

(b) (i) The coordinates of the centre, E, of the square are (8, y). Find the value of y. [1]

(ii) Find the equation of the diagonal *BD*.

(iii) Given that the x-coordinate of B is less than the x-coordinate of D, write \overrightarrow{EB} and \overrightarrow{ED} as column vectors. [2]

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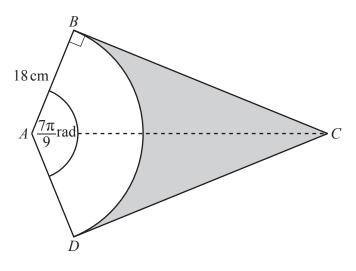
[2]

[3]

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DAB is a sector of a circle, centre *A*, radius 18 cm. The lines *CB* and *CD* are tangents to the circle. Angle *DAB* is $\frac{7\pi}{9}$ radians.

(a) Find the perimeter of the shaded region.

(b) Find the area of the shaded region.

[3]

[3]

- NUM TOT BITSCOUS CON A particle moves in a straight line so that, t seconds after passing through a fixed point O, its velocity, $v \text{ ms}^{-1}$, is given by $v = 3t^2 - 30t + 72$. 8
 - (a) Find the distance between the particle's two positions of instantaneous rest. [6]

(b) Find the acceleration of the particle when t = 2.

[2]



9 Solve the following simultaneous equations.

$$4x^2 + 3xy + y^2 = 8$$
$$xy + 4 = 0$$

[6]



[2]

10 (a) Find
$$\int (e^{x+1})^3 dx$$
.

(b) (i) Differentiate, with respect to x, $y = x \sin 4x$.

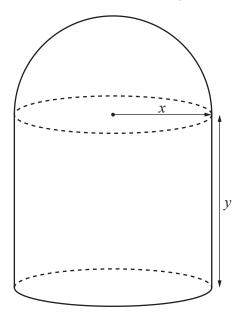
(ii) Hence show that
$$\int_{\frac{\pi}{4}}^{\frac{\pi}{3}} 4x \cos 4x dx = \frac{1}{8} - \frac{\pi\sqrt{3}}{6}$$
. [4]

11



11 In this question all lengths are in centimetres.

The volume and surface area of a sphere of radius r are $\frac{4}{3}\pi r^3$ and $4\pi r^2$ respectively.

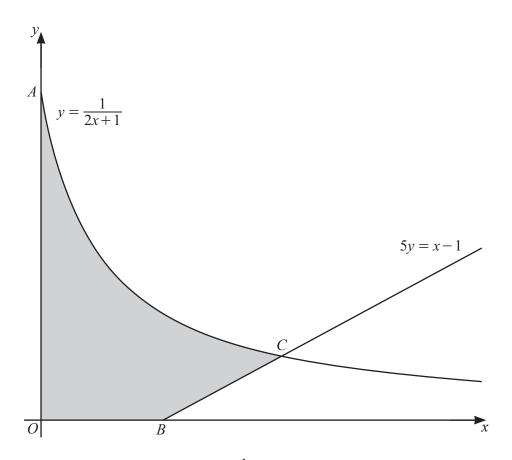


The diagram shows a solid object made from a hemisphere of radius x and a cylinder of radius x and height y. The volume of the object is 500 cm^3 .

(a) Find an expression for y in terms of x and show that the surface area, S, of the object is given by $S = \frac{5}{3}\pi x^2 + \frac{1000}{x}.$ [4]

MANN. ITS IT A REAL ST (b) Given that x can vary and that S has a minimum value, find the value of x for which S is a minimum.

[4]



The diagram shows part of the curve $y = \frac{1}{2x+1}$ and part of the line 5y = x-1. The curve meets the *y*-axis at point *A*. The line meets the *x*-axis at point *B*. The line and curve intersect at point *C*.

(a) (i) Find the coordinates of A and B.

(ii) Verify that the *x*-coordinate of *C* is 2.

[2]

[1]

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(b) Find the exact area of the shaded region.



Question 13 is printed on the next page.

13 The functions f and g are defined, for x > 0, by

$$f(x) = \frac{2x^2 - 1}{3x},$$
$$g(x) = \frac{1}{x}.$$

(a) Find and simplify an expression for fg(x).

(b) (i) Given that f^{-1} exists, write down the range of f^{-1} . [1]

(ii) Show that
$$f^{-1}(x) = \frac{px + \sqrt{qx^2 + r}}{4}$$
, where p, q and r are integers. [4]

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