

Cambridge O Level

CANDIDATE NAME					
CENTRE NUMBER			CANDIDATE NUMBER		

8 9 9 8 2 1 6 1 1 2

ADDITIONAL MATHEMATICS

4037/21

Paper 2 May/June 2021

2 hours

You must answer on the question paper.

No additional materials are needed.

INSTRUCTIONS

- Answer all questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do not use an erasable pen or correction fluid.
- Do not write on any bar codes.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.

INFORMATION

- The total mark for this paper is 80.
- The number of marks for each question or part question is shown in brackets [].

This document has 16 pages. Any blank pages are indicated.

Mathematical Formulae

1. ALGEBRA

Quadratic Equation

For the equation $ax^2 + bx + c = 0$,

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Binomial Theorem

$$(a+b)^{n} = a^{n} + \binom{n}{1}a^{n-1}b + \binom{n}{2}a^{n-2}b^{2} + \dots + \binom{n}{r}a^{n-r}b^{r} + \dots + b^{n}$$

where *n* is a positive integer and $\binom{n}{r} = \frac{n!}{(n-r)!r!}$

Arithmetic series
$$u_n = a + (n-1)d$$

$$S_n = \frac{1}{2}n(a+l) = \frac{1}{2}n\left\{2a + (n-1)d\right\}$$

Geometric series
$$u_n = ar^{n-1}$$

$$S_n = \frac{a(1-r^n)}{1-r} \ (r \neq 1)$$

$$S_{\infty} = \frac{a}{1-r} (|r| < 1)$$

2. TRIGONOMETRY

Identities

$$\sin^2 A + \cos^2 A = 1$$
$$\sec^2 A = 1 + \tan^2 A$$
$$\csc^2 A = 1 + \cot^2 A$$

Formulae for $\triangle ABC$

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$
$$a^2 = b^2 + c^2 - 2bc \cos A$$
$$\Delta = \frac{1}{2}bc \sin A$$

1 (a) Write the expression $x^2 - 6x + 1$ in the form $(x+a)^2 + b$, where a and b are constants. [2]

- **(b)** Hence write down the coordinates of the minimum point on the curve $y = x^2 6x + 1$. [1]
- Variables x and y are such that, when $\ln y$ is plotted against $\ln x$, a straight line graph passing through the points (6, 5) and (8, 9) is obtained. Show that $y = e^p x^q$ where p and q are integers. [4]

3 (a) Solve the inequality |4x-1| > 9. [3]

(b) Solve the equation $2x - 11\sqrt{x} + 12 = 0$. [3]

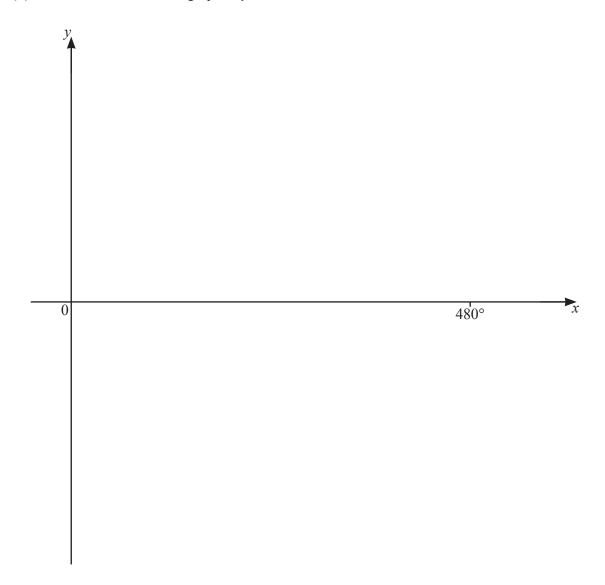
4 The graph of $y = a + 2 \tan bx$, where a and b are constants, passes through the point (0, -4) and has period 480° .

(a) Find the value of a and of b.

[3]

(b) On the axes, sketch the graph of y for values of x between 0° and 480° .

[2]



5 The curves $y = x^2$ and $y^2 = 27x$ intersect at O(0, 0) and at the point A. Find the equation of the perpendicular bisector of the line OA. [8]

Variables x and y are such that $y = e^{\frac{x}{2}} + x \cos 2x$, where x is in radians. Use differentiation to find the approximate change in y as x increases from 1 to 1+h, where h is small. [6]

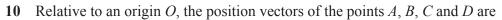
Find the exact values of the constant k for which the line y = 2x + 1 is a tangent to the curve $y = 4x^2 + kx + k - 2$. 7 [6]

- 8 In this question, a, b, c and d are positive constants.
 - (a) (i) It is given that $y = \log_a(x+3) + \log_a(2x-1)$. Explain why x must be greater than $\frac{1}{2}$. [1]

(ii) Find the exact solution of the equation
$$\frac{\log_a 6}{\log_a (y+3)} = 2$$
. [3]

(b) Write the expression $\log_a 9 + (\log_a b)(\log_{\sqrt{b}} 9a)$ in the form $c + d\log_a 9$, where c and d are integers. [4]

A curve is such that $\frac{d^2y}{dx^2} = \sin(6x - \frac{\pi}{2})$. Given that $\frac{dy}{dx} = \frac{1}{2}$ at the point $(\frac{\pi}{4}, \frac{13\pi}{12})$ on the curve, find the equation of the curve. [7]



$$\overrightarrow{OA} = \begin{pmatrix} 6 \\ -5 \end{pmatrix}, \overrightarrow{OB} = \begin{pmatrix} 10 \\ 3 \end{pmatrix}, \overrightarrow{OC} = \begin{pmatrix} x \\ y \end{pmatrix} \text{ and } \overrightarrow{OD} = \begin{pmatrix} 12 \\ 7 \end{pmatrix}.$$

[3]

(a) Find the unit vector in the direction of
$$\overrightarrow{AB}$$
.

(b) The point
$$A$$
 is the mid-point of BC . Find the value of x and of y . [2]

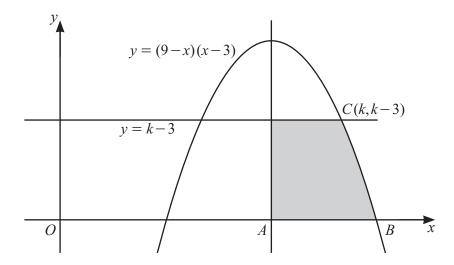
(c) The point *E* lies on *OD* such that
$$OE : OD$$
 is $1 : 1 + \lambda$. Find the value of λ such that \overrightarrow{BE} is parallel to the *x*-axis.

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	(a)	(i)	Show that the common difference of the arithmetic progression is 5.	[5]			
		(ii)	Find the sum of the first 20 terms of the arithmetic progression.	[2]			

(b) (i)	Find the 5th term of the geometric progression.	[2]

(ii) Explain whether or not the sum to infinity of this geometric progression exists. [1]

12



The diagram shows part of the curve y = (9-x)(x-3) and the line y = k-3, where k > 3. The line through the maximum point of the curve, parallel to the y-axis, meets the x-axis at A. The curve meets the x-axis at B, and the line y = k-3 meets the curve at the point C(k, k-3). Find the area of the shaded region.

Continuation of working space for Question 12.



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