

**Exam–style Practice paper**

**Section A: Statistics**

**1 a**  $0.2 + y + 0.3 + 0.35 = 1$   
 $y = 1 - 0.85 = 0.15$

**b**  $P(B \text{ and } M) = 0.15$   
 $P(B) \times P(M) = (0.2 + 0.15) \times (0.3 + 0.15) = 0.35 \times 0.45 = 0.1575$   
 $P(B \text{ and } M) \neq P(B) \times P(M)$ , so 'likes bananas' and 'likes mangoes' are not independent events.

**2 a**  $t$  is a continuous variable, because it is a measured variable which can take any value.

**b**  $\text{mean} = \frac{\sum t}{n} = \frac{140.1}{10} = 14.01$

$\text{standard deviation} = \sqrt{\frac{\sum t^2}{n} - \left(\frac{\sum t}{n}\right)^2} = \sqrt{\frac{1981.33}{10} - \left(\frac{140.1}{10}\right)^2} = 1.36 \text{ (to 3 s.f.)}$

**c**  $15.8^\circ\text{C}$  is higher than the current mean so the mean would increase.

**d** Clare could take a random sample of days from the whole of September for the different locations in the UK.

**3 a**  $0.1 + 0.2 + 0.15 + p + 0.1 + 0.25 = 1$   
 $p = 1 - 0.8 = 0.2$

**b**  $P(2 \leq X \leq 5) = 1 - P(X = 1) - P(X = 6)$   
 $= 1 - 0.1 - 0.25 = 0.65$

**c i**  $P(\text{odd}) = 0.1 + 0.15 + 0.1 = 0.35$   
 $P(\text{odd exactly twice}) = \binom{10}{2} 0.35^2 0.65^8$   
 $= 0.1757 \text{ (to 4 d.p.)}$

**ii**  $P(\text{odd more than 6 times}) = \binom{10}{7} 0.35^7 0.65^3 + \binom{10}{8} 0.35^8 0.65^2 + \binom{10}{9} 0.35^9 0.65^1 + 0.35^{10}$   
 $= 0.0260 \text{ (to 4 d.p.)}$

**4 a** The test statistic is the number of plates that are flawed.  
 $H_0: p = 0.3, H_1: p < 0.3$

**b**  $X \sim B(20, 0.3)$   
 $P(X \leq 2) = 0.0355 < 0.05$   
 $P(X \leq 3) = 0.1071 > 0.05$   
 The critical region is  $X \leq 2$

**c** The actual significance level is  $0.0355 = 3.55\%$

**d** 1 falls into the critical region, therefore there is evidence to support the claim.

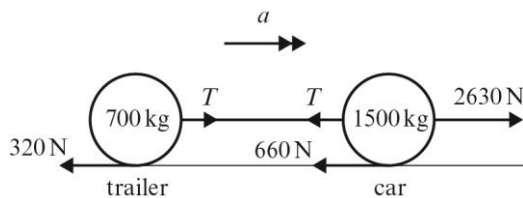
**5 a** The increase in energy released is 3.1 Joules for each degree of temperature.

- 5 **b** This value of  $h$  is a long way from the range of the experimental data: hence the extrapolation is excessive and the predicted value of  $e$  would be too unreliable.
- c** It is not sensible. The regression line predicts a value of  $e$  given  $h$ , not the other way round.

$$\begin{aligned}
 6 \quad P(4.6 \leq h \leq 6.1) &= \frac{0.4 \times 10 + 0.2 \times 45 + 0.2 \times 60 + 0.2 \times 80 + 0.4 \times 25 + 0.1 \times 10}{0.5 \times 5 + 0.5 \times 10 + 0.2 \times 45 + 0.2 \times 60 + 0.2 \times 80 + 0.4 \times 25 + 0.5 \times 10} \\
 &= \frac{4 + 9 + 12 + 16 + 10 + 1}{2.5 + 5 + 9 + 12 + 16 + 10 + 5} \\
 &= \frac{52}{59.5} \\
 &= 0.8739 \text{ (to 4 d.p.)}
 \end{aligned}$$

**Section B: Mechanics**

7



$$F = ma$$

**a** For the whole system:

$$F = 2630 - 660 - 320 = 1650$$

$$m = 1500 + 700 = 2200$$

$$1650 = 2200a$$

The acceleration of the car is  $0.75 \text{ m s}^{-2}$

**b** For the trailer:

$$F = T - 320, m = 700, a = 0.75$$

$$T - 320 = 700 \times 0.75 = 525$$

$$T = 525 + 320$$

The tension in the tow-rod is 845 N.

**c** Since the tow-rod is inextensible, the acceleration of each part of the system is identical and the tension in it is constant throughout.

**8 a** Resultant force,  $F = \mathbf{F}_1 + \mathbf{F}_2 + \mathbf{F}_3$

$$F = (3\mathbf{i} - 6\mathbf{j}) + (4\mathbf{i} + 5\mathbf{j}) + (2\mathbf{i} - 2\mathbf{j}) = (9\mathbf{i} - 3\mathbf{j})$$

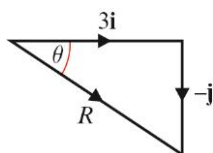
$$m = 3, \mathbf{a} = ?$$

$$F = m\mathbf{a}$$

$$(9\mathbf{i} - 3\mathbf{j}) = 3\mathbf{a}$$

The acceleration of the particle is  $(3\mathbf{i} - \mathbf{j}) \text{ m s}^{-2}$

**b**



$$\tan \theta = \frac{1}{3}$$

8 b The acceleration acts at an angle of  $18.4^\circ$  below i.

$$\text{c } |\mathbf{a}| = \sqrt{1^2 + 3^2} = \sqrt{10}$$

The magnitude of the acceleration is  $\sqrt{10} \text{ m s}^{-2}$

9 a Taking up as positive:

$$s = 0, a = -9.8, t = 5, u = ?$$

$$s = ut + \frac{1}{2}at^2$$

$$0 = (u \times 5) + \frac{1}{2}(-9.8 \times 5^2) = 5u - 122.5$$

$$u = \frac{122.5}{5} = 24.5$$

The ball is projected at a speed of  $24.5 \text{ m s}^{-1}$

b  $u = 24.5, a = -9.8, v = 0, s = ?$

$$v^2 = u^2 + 2as$$

$$0 = 24.5^2 + (2 \times (-9.8s))$$

$$s = \frac{24.5^2}{2 \times 9.8} = \frac{600.25}{19.6} = 30.625$$

The ball reaches a height of 30.6 m above  $P$ .

c  $s = 15, u = 24.5, a = -9.8, t = ?$

$$s = ut + \frac{1}{2}at^2$$

$$15 = 24.5t + \frac{1}{2}(-9.8 \times t^2)$$

$$4.9t^2 - 24.5t + 15 = 0$$

$$t = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$t = \frac{24.5 \pm \sqrt{24.5^2 - (4 \times 4.9 \times 15)}}{2 \times 4.9}$$

$$= \frac{24.5 \pm \sqrt{306.25}}{9.8}$$

$$= \frac{24.5 \pm 17.5}{9.8}$$

$$= \frac{42}{9.8} \text{ or } \frac{7}{9.8}$$

The ball is at a height of 15 m above  $P$  at 0.714 s and 4.29 s after leaving  $P$ .

10  $v = 3 + 9t^2 - 4t^3$

When the particle is moving at maximum velocity,  $a = \frac{dv}{dt} = 0$

$$0 = \frac{d(3 + 9t^2 - 4t^3)}{dt}$$

$$= 18t - 12t^2$$

$$= 6t(3 - 2t)$$

- 10 At  $t = 0$ , the particle moves at minimum velocity (see graph).  
 The particle has maximum velocity at  $t = \frac{3}{2}$  seconds.

$$s = \int v \, dt = \int_0^{\frac{3}{2}} (3 + 9t^2 - 4t^3) \, dt$$

$$= \left[ 3t + \frac{9t^3}{3} - \frac{4t^4}{4} \right]_0^{\frac{3}{2}} = \left[ 3t + 3t^3 - t^4 \right]_0^{\frac{3}{2}}$$

For  $t = 0$ , all terms are zero, so this becomes:

$$s = 3 \times \left( \frac{3}{2} \right) + 3 \times \left( \frac{3}{2} \right)^3 - \left( \frac{3}{2} \right)^4$$

$$= \frac{9}{2} + \frac{81}{8} - \frac{81}{16} = \frac{153}{16}$$

The particle is moving at maximum velocity when it is  $\frac{153}{16}$  m from  $O$ .