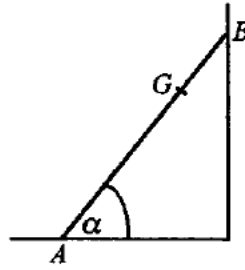


Take $g = 9.8 \text{ ms}^{-2}$ and give all answers correct to 3 significant figures where necessary.

- A ball, of mass m kg, is moving with velocity $(5\mathbf{i} - 3\mathbf{j}) \text{ ms}^{-1}$ when it receives an impulse of $(-2\mathbf{i} - 4\mathbf{j}) \text{ Ns}$. Immediately after the impulse is applied, the ball has velocity $(3\mathbf{i} + k\mathbf{j}) \text{ ms}^{-1}$. Find the values of the constants k and m . (6 marks)
- A particle P , initially at rest at the point O , moves in a straight line such that at time t seconds after leaving O its acceleration is $(12t - 15) \text{ ms}^{-2}$. Find

 - the velocity of P at time t seconds after it leaves O , (3 marks)
 - the value of t when the speed of P is 36 ms^{-1} . (3 marks)
- A non-uniform ladder AB , of length $3a$, has its centre of mass at G , where $AG = 2a$. The ladder rests in limiting equilibrium with the end B against a smooth vertical wall and the end A resting on rough horizontal ground. The angle between AB and the horizontal in this position is α , where $\tan \alpha = \frac{14}{9}$. Calculate the coefficient of friction between the ladder and the ground. (7 marks)

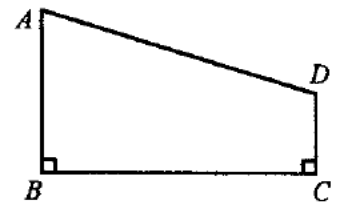

- A particle P starts from the point O and moves such that its position vector \mathbf{r} m relative to O after t seconds is given by $\mathbf{r} = at^2\mathbf{i} + bt\mathbf{j}$. 60 seconds after P leaves O it is at the point Q with position vector $(90\mathbf{i} + 30\mathbf{j}) \text{ m}$.

 - Find the values of the constants a and b . (3 marks)
 - Find the speed of P when it is at Q . (4 marks)
 - Sketch the path followed by P for $0 \leq t \leq 60$. (2 marks)
- A lorry of mass 4200 kg can develop a maximum power of 84 kW . On any road the lorry experiences a non-gravitational resisting force which is directly proportional to its speed. When the lorry is travelling at 20 ms^{-1} the resisting force has magnitude 2400 N . Find the maximum speed of the lorry when it is

 - travelling on a horizontal road, (4 marks)
 - climbing a hill inclined at an angle α to the horizontal, where $\sin \alpha = \frac{1}{7}$. (6 marks)

6. Two railway trucks, P and Q , of equal mass, are moving towards each other with speeds $4u$ and $5u$ respectively along a straight stretch of rail which may be modelled as being smooth. They collide and move apart. The coefficient of restitution between P and Q is e .
- (a) Find, in terms of u and e , the speed of Q after the collision. **(6 marks)**
- (b) Show that $e > \frac{1}{9}$. **(2 marks)**
- Q now hits a fixed buffer and rebounds along the track. P continues to move with the speed that it had immediately after it collided with Q .
- (c) Prove that it is impossible for a further collision between P and Q to occur. **(3 marks)**

7. A uniform lamina is in the form of a trapezium $ABCD$, as shown. AB and DC are perpendicular to BC . $AB = 17$ cm, $BC = 21$ cm and $CD = 8$ cm.



- (a) Find the distances of the centre of mass of the lamina from
(i) AB , (ii) BC . **(8 marks)**

The lamina is freely suspended from C and rests in equilibrium.

- (b) Find the angle between CD and the vertical. **(3 marks)**

8. A stone, of mass 1.5 kg, is projected horizontally with speed 4 ms^{-1} from a height of 7 m above horizontal ground.
- (a) Show that the stone travels about 4.78 m horizontally before it hits the ground. **(4 marks)**
- (b) Find the height of the stone above the ground when it has travelled half of this horizontal distance. **(4 marks)**
- (c) Calculate the potential energy lost by the stone as it moves from its point of projection to the ground. **(2 marks)**
- (d) Showing your method clearly, use your answer to part (c) to find the speed with which the stone hits the ground. **(3 marks)**
- (e) State **two** modelling assumptions that you have made in answering this question. **(2 marks)**