



**Cambridge International Examinations**  
Cambridge International Advanced Level

CANDIDATE NAME

CENTRE NUMBER

CANDIDATE NUMBER

\* 9 3 8 8 8 7 0 9 1 1 \*

**MATHEMATICS**

**9709/33**

Paper 3 Pure Mathematics 3 (P3)

**October/November 2017**

**1 hour 45 minutes**

Candidates answer on the Question Paper.

Additional Materials: List of Formulae (MF9)

**READ THESE INSTRUCTIONS FIRST**

Write your Centre number, candidate number and name in the spaces at the top of this page.  
Write in dark blue or black pen.  
You may use an HB pencil for any diagrams or graphs.  
Do not use staples, paper clips, glue or correction fluid.  
**DO NOT WRITE IN ANY BARCODES.**

Answer **all** the questions.  
Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place in the case of angles in degrees, unless a different level of accuracy is specified in the question.  
The use of an electronic calculator is expected, where appropriate.  
You are reminded of the need for clear presentation in your answers.

At the end of the examination, fasten all your work securely together.  
The number of marks is given in brackets [ ] at the end of each question or part question.  
The total number of marks for this paper is 75.

This document consists of **19** printed pages and **1** blank page.











(ii) Hence sketch the graph of  $y = \tan(45^\circ + x) + \tan(45^\circ - x)$  for  $0^\circ \leq x \leq 90^\circ$ .





(ii) Hence show that there are two points on the curve at which the tangent is parallel to the  $x$ -axis and find the coordinates of these points. [4]

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A series of horizontal dotted lines for writing.

- 7 (a) The complex number  $u$  is given by  $u = 8 - 15i$ . Showing all necessary working, find the two square roots of  $u$ . Give answers in the form  $a + ib$ , where the numbers  $a$  and  $b$  are real and exact. [5]

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- (b) On an Argand diagram, shade the region whose points represent complex numbers satisfying both the inequalities  $|z - 2 - i| \leq 2$  and  $0 \leq \arg(z - i) \leq \frac{1}{4}\pi$ . [4]

8 Let  $f(x) = \frac{4x^2 + 9x - 8}{(x+2)(2x-1)}$ .

(i) Express  $f(x)$  in the form  $A + \frac{B}{x+2} + \frac{C}{2x-1}$ . [4]

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(ii) Hence show that  $\int_1^4 f(x) dx = 6 + \frac{1}{2} \ln\left(\frac{16}{7}\right)$ .

[5]

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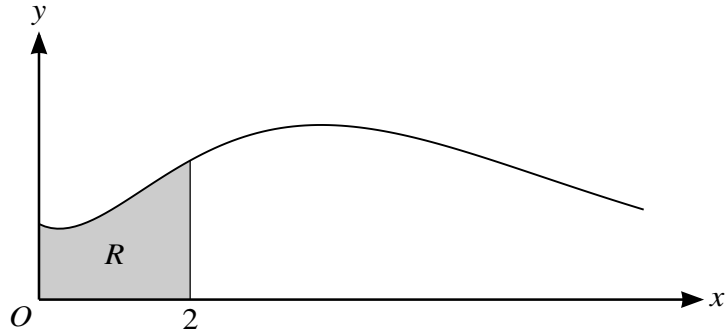
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The diagram shows the curve  $y = (1 + x^2)e^{-\frac{1}{2}x}$  for  $x \geq 0$ . The shaded region  $R$  is enclosed by the curve, the  $x$ -axis and the lines  $x = 0$  and  $x = 2$ .

- (i) Find the exact values of the  $x$ -coordinates of the stationary points of the curve. [4]

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10 The equations of two lines  $l$  and  $m$  are  $\mathbf{r} = 3\mathbf{i} - \mathbf{j} - 2\mathbf{k} + \lambda(-\mathbf{i} + \mathbf{j} + 4\mathbf{k})$  and  $\mathbf{r} = 4\mathbf{i} + 4\mathbf{j} - 3\mathbf{k} + \mu(2\mathbf{i} + \mathbf{j} - 2\mathbf{k})$ , respectively.

(i) Show that the lines do not intersect. [3]

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(ii) Calculate the acute angle between the directions of the lines. [3]

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