

## MARK SCHEME for the October/November 2009 question paper

## for the guidance of teachers

# 9709 MATHEMATICS

9709/21

Paper 21, maximum raw mark 50

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes must be read in conjunction with the question papers and the report on the examination.

• CIE will not enter into discussions or correspondence in connection with these mark schemes.

CIE is publishing the mark schemes for the October/November 2009 question papers for most IGCSE, GCE Advanced Level and Advanced Subsidiary Level syllabuses and some Ordinary Level syllabuses.



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#### Mark Scheme Notes

Marks are of the following three types:

- M Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the M mark and in some cases an M mark can be implied from a correct answer.
- A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).
- B Mark for a correct result or statement independent of method marks.
- When a part of a question has two or more "method" steps, the M marks are generally independent unless the scheme specifically says otherwise; and similarly when there are several B marks allocated. The notation DM or DB (or dep\*) is used to indicate that a particular M or B mark is dependent on an earlier M or B (asterisked) mark in the scheme. When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.
- The symbol √ implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A or B marks are given for correct work only. A and B marks are not given for fortuitously "correct" answers or results obtained from incorrect working.
- Note: B2 or A2 means that the candidate can earn 2 or 0. B2/1/0 means that the candidate can earn anything from 0 to 2.

The marks indicated in the scheme may not be subdivided. If there is genuine doubt whether a candidate has earned a mark, allow the candidate the benefit of the doubt. Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored.

- Wrong or missing units in an answer should not lead to the loss of a mark unless the scheme specifically indicates otherwise.
- For a numerical answer, allow the A or B mark if a value is obtained which is correct to 3 s.f., or which would be correct to 3 s.f. if rounded (1 d.p. in the case of an angle). As stated above, an A or B mark is not given if a correct numerical answer arises fortuitously from incorrect working. For Mechanics questions, allow A or B marks for correct answers which arise from taking *g* equal to 9.8 or 9.81 instead of 10.

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The following	scioud.com		

- AEF Any Equivalent Form (of answer is equally acceptable)
- AG Answer Given on the question paper (so extra checking is needed to ensure that the detailed working leading to the result is valid)
- BOD Benefit of Doubt (allowed when the validity of a solution may not be absolutely clear)
- CAO Correct Answer Only (emphasising that no "follow through" from a previous error is allowed)
- CWO Correct Working Only - often written by a 'fortuitous' answer
- ISW Ignore Subsequent Working
- MR Misread
- PA Premature Approximation (resulting in basically correct work that is insufficiently accurate)
- SOS See Other Solution (the candidate makes a better attempt at the same question)
- SR Special Ruling (detailing the mark to be given for a specific wrong solution, or a case where some standard marking practice is to be varied in the light of a particular circumstance)

### Penalties

- MR -1 A penalty of MR -1 is deducted from A or B marks when the data of a question or part question are genuinely misread and the object and difficulty of the question remain unaltered. In this case all A and B marks then become "follow through  $\sqrt{}$ " marks. MR is not applied when the candidate misreads his own figures - this is regarded as an error in accuracy. An MR-2 penalty may be applied in particular cases if agreed at the coordination meeting.
- PA -1 This is deducted from A or B marks in the case of premature approximation. The PA -1 penalty is usually discussed at the meeting.

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		GC	CE A/AS LEVEL – October/November 2009	9709	21	Ally is
1	EITHER:	quadratic	non-modular inequality from $(2x + 3)^2 < (x - 3)^2$ , or ce equation, or pair of linear equations $2x + 3 = \pm(x - 3)^2$ sonable solution attempt at a 3-term quadratic, or solv	)	M1	mainscloud.com
		equations	· · · ·		M1	
			itical values $x = -6$ and $x = 0$		Al	
		State ansv	wer $-6 < x < 0$		A1	
	OR:	obtain the solving a l Obtain the	e critical value $x = -6$ from a graphical method or by i linear equation or inequality e critical value $x = 0$ similarly wer $-6 < x < 0$	inspection, or by	B1 B2 B1	[4]
2	Use $\ln x^2 =$ Obtain 3 – Solve for	$-x^2 = x^2$ , or	equivalent		B1 B1 M1	
			22, having rejected $x = -1.22$		A1	[4]
3	(i)	Substitute Obtain <i>a</i> =	$e_x = -\frac{1}{2}$ and equate to zero		M1 A1	[0]
					AI	[2]
	(ii)	<i>EITHER</i> : <i>OR</i> :	Attempt division by $2x + 1$ reaching a partial quotie Obtain quadratic factor $2x^2 - 5x - 3$ Obtain complete factorisation $(2x + 1)^2(x - 3)$ Obtain factor $(x - 3)$ by inspection or factor theorem Attempt division by $(x - 3)$ reaching a partial quotie	n	M1 A1 A1 + A1 B2 M1	
4			Obtain complete factorisation $(2x + 1)^2(x - 3)$		A1	[4]
4	(i)	•	formulae to express equation in terms of sin x and cos $0^\circ = \frac{1}{2}$ and sin $60^\circ = \frac{\sqrt{3}}{2}$ , or equivalent	X	M1 M1	
			2 2		Al	
		-	uation in sin x and cos x in any correct form n x = $\sqrt{3}/5$ , or 0.3464, or equivalent			٢/٦
	(ii)		$x = \sqrt{3}/5$ , or 0.3464, or equivalent swer $x = 19.1^{\circ}$		A1 B1	[4]
	<- <i>,</i>	Obtain ans	swer $x = 199.1^{\circ}$ and no others in the range aswers outside the given range.]		B1√	[2]
5	(i)	Use doub!	le angle formulae and obtain $a + b\cos 4x$		M1	
-	(-)		aswer $\frac{1}{2} + \frac{1}{2}\cos 4x$ , or equivalent		A1	[2]
	(ii)	Integrate a	and obtain $\frac{1}{2}x + \frac{1}{8}\sin 4x$	1	$A1\sqrt{+}A1\sqrt{-}$	
		Substitute	e limits correctly		M1	
			swer $\frac{1}{16}\pi + \frac{1}{8}$ , or exact equivalent		A1	[4]

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6	(i)	Use product rule		M1*	COUR
U	(1)	Obtain derivative in any correct form		Al	Y. CO.
		Equate derivative to zero and solve for x		M1(dep*)	<i>'n</i>
		Obtain $x = 1/e$ , or exact equivalent		Aĺ	
		Obtain $y = -1/e$ , or exact equivalent		A1	[5]
	(ii)	Carry out complete method for determining the nature of a stat	ionary point	M1	
		Show that at $x = 1/e$ there is a minimum point, with no errors s	een	A1	[2]
7	(i)	<i>EITHER</i> : Integrate $1 - e^{-x}$ obtaining $x \pm e^{-x}$		M1	
		Obtain indefinite integral $x - e^{-x}$		A1	
		Substitute limits $x = 0$ , $x = p$ correctly		M1	
		Obtain answer $p + e^{-p} - 1$ , or equivalent		A1	
		<i>OR</i> : Integrate $e^{-x}$ obtaining $\pm e^{-x}$		M1	
		Substitute limits $x = 0$ , $x = p$ correctly Obtain area below curve is $1 - e^{-p}$		M1 A1	
		Obtain answer $p + e^{-p} - 1$ , or equivalent		A1	[4]
	(ii)	Show that $p + e^{-p} - 1 = 1$ is equivalent to $p = 2 - e^{-p}$ or vice ver	rsa	B1	[1]
	(iii)	Use the iterative formula correctly at least once		M1	
		Obtain final answer 1.84		A1	
		Show sufficient iterations to justify its accuracy to 2 d.p.		A1	[3]
8	(i)	<i>EITHER</i> : Substitute $x = 1$ and attempt to solve 3-term quadrated and the solution of the so	tic in y	M1	
		Obtain answers $(1, 1)$ and $(1, -3)$		A1	[0]
		OR: State answers $(1, 1)$ and $(1, -3)$		B1 + B1	[2]
	(ii)	State $2y \frac{dy}{dx}$ as derivative of $y^2$		B1	
	(11)	a.t		DI	
		State $2y + 2x \frac{dy}{dx}$ as derivative of $2xy$		B1	
		Substitute for <i>x</i> and <i>y</i> , and solve for $\frac{dy}{dx}$		M1	
		Obtain $\frac{dy}{dx} = 0$ when $x = 1$ and $y = 1$		A1	
		Obtain $\frac{dy}{dx} = -2$ when $x = 1$ and $y = -3$		A1	
		Form the equation of the tangent at $(1, -3)$		M1	
		Obtain answer $2x + y + 1 = 0$		A1	[7]