



Cambridge Assessment International Education

Cambridge International Advanced Subsidiary and Advanced Level

MATHEMATICS
Paper 1
MARK SCHEME
Maximum Mark: 75

Published

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

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Generic Marking Principles

These general marking principles must be applied by all examiners when marking candidate answers. They should be applied alongside the specific content of the mark scheme or generic level descriptors for a question. Each question paper and mark scheme will also comply with these marking principles.

GENERIC MARKING PRINCIPLE 1:

Marks must be awarded in line with:

- the specific content of the mark scheme or the generic level descriptors for the question
- the specific skills defined in the mark scheme or in the generic level descriptors for the question
- the standard of response required by a candidate as exemplified by the standardisation scripts.

GENERIC MARKING PRINCIPLE 2:

Marks awarded are always whole marks (not half marks, or other fractions).

GENERIC MARKING PRINCIPLE 3:

Marks must be awarded **positively**:

- marks are awarded for correct/valid answers, as defined in the mark scheme. However, credit is given for valid answers which go beyond the scope of the syllabus and mark scheme, referring to your Team Leader as appropriate
- marks are awarded when candidates clearly demonstrate what they know and can do
- marks are not deducted for errors
- marks are not deducted for omissions
- answers should only be judged on the quality of spelling, punctuation and grammar when these features are specifically assessed by the question as indicated by the mark scheme. The meaning, however, should be unambiguous.

GENERIC MARKING PRINCIPLE 4:

Rules must be applied consistently e.g. in situations where candidates have not followed instructions or in the application of generic level descriptors.

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GENERIC MARKING PRINCIPLE 5:

Marks should be awarded using the full range of marks defined in the mark scheme for the question (however; the use of the full mark range may be limited according to the quality of the candidate responses seen).

GENERIC MARKING PRINCIPLE 6:

Marks awarded are based solely on the requirements as defined in the mark scheme. Marks should not be awarded with grade thresholds or grade descriptors in mind.

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Mark Scheme Notes

Marks are of the following three types:

- M Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the M mark and in some cases an M mark can be implied from a correct answer.
- A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).
- B Mark for a correct result or statement independent of method marks.
- When a part of a question has two or more 'method' steps, the M marks are generally independent unless the scheme specifically says otherwise; and similarly when there are several B marks allocated. The notation DM or DB (or dep*) is used to indicate that a particular M or B mark is dependent on an earlier M or B (asterisked) mark in the scheme. When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.
- The symbol FT implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A or B marks are given for correct work only. A and B marks are not given for fortuitously "correct" answers or results obtained from incorrect working.
 - Note: B2 or A2 means that the candidate can earn 2 or 0.
 B2/1/0 means that the candidate can earn anything from 0 to 2.

The marks indicated in the scheme may not be subdivided. If there is genuine doubt whether a candidate has earned a mark, allow the candidate the benefit of the doubt. Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored.

- Wrong or missing units in an answer should not lead to the loss of a mark unless the scheme specifically indicates otherwise.
- For a numerical answer, allow the A or B mark if a value is obtained which is correct to 3 s.f., or which would be correct to 3 s.f. if rounded (1 d.p. in the case of an angle). As stated above, an A or B mark is not given if a correct numerical answer arises fortuitously from incorrect working. For Mechanics questions, allow A or B marks for correct answers which arise from taking *g* equal to 9.8 or 9.81 instead of 10.

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The following abbreviations may be used in a mark scheme or used on the scripts:

AEF/OE	Any Equivalent Form (of answer is equally acceptable) / Or Equivalent
AG	Answer Given on the question paper (so extra checking is needed to ensure that the detailed working leading to the result is valid)
CAO	Correct Answer Only (emphasising that no 'follow through' from a previous error is allowed)
CWO	Correct Working Only – often written by a 'fortuitous' answer
ISW	Ignore Subsequent Working
SOI	Seen or implied
SR	Special Ruling (detailing the mark to be given for a specific wrong solution, or a case where some standard marking practice is to be varied in the light of a particular circumstance)

Penalties

- MR –1 A penalty of MR –1 is deducted from A or B marks when the data of a question or part question are genuinely misread and the object and difficulty of the question remain unaltered. In this case all A and B marks then become 'follow through' marks. MR is not applied when the candidate misreads his own figures this is regarded as an error in accuracy. An MR –2 penalty may be applied in particular cases if agreed at the coordination meeting.
- PA –1 This is deducted from A or B marks in the case of premature approximation. The PA –1 penalty is usually discussed at the meeting.

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Question	Answer	Marks	Guidance
1	$[3]\left[\left(x-2\right)^2\right]\left[-5\right]$	B1B1B1	OR $a = 3$, $b = -2$, $c = -5$. 1st mark is dependent on the form $(x + a)^2$ following 3
		3	

Question	Answer	Marks	Guidance
2	$\int_{5} C_3 x^2 \left(\frac{-2}{x}\right)^3 SOI$	B2,1,0	−80 www scores B3. Accept ₅ C ₂ .
	$-80 \text{ Accept } \frac{-80}{x}$	B 1	+80 without clear working scores SCB1
		3	

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Question	Answer	Marks	Guidance
3	$\left[\frac{a(1-r^n)}{1-r}\right] \left[\div\right] \left[\frac{a}{1-r}\right]$	M1M1	Correct formulae <u>used</u> with/without $r = 0.99$ or $n = 100$.
		DM1	Allow numerical a (M1M1). 3rd M1 is for division $\frac{S_n}{S_{\infty}}$ (or ratio)
			501
	$1 - 0.99^{100}$ SOI OR $\frac{63(a)}{100(a)}$ SOI	A1	Could be shown multiplied by 100(%). Dep. on DM1
	63(%) Allow 63.4 or 0.63 but not 2 infringements (e.g. 0.634, 0.63%)	A1	$n = 99$ used scores Max M3. Condone $a = 0.99$ throughout $S_n = S_\infty$ (without division shown) scores 2/5
		5	

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Question	Answer	Marks	Guidance
4	$f(x) = \left[\frac{\left(3x - 1\right)^{\frac{2}{3}}}{\frac{2}{3}}\right] \left[\div 3\right] (+c)$	B1B1	
	$1 = \frac{8^{\frac{2}{3}}}{2} + c$	M1	Sub $y = 1, x = 3$ Dep. on attempt to integrate and c present
	$c = -1 \rightarrow y = \frac{1}{2} (3x - 1)^{\frac{2}{3}} - 1 \text{ SOI}$	A1	
	When $x = 0$, $y = \frac{1}{2}(-1)^{\frac{2}{3}} - 1 = -\frac{1}{2}$	DM1A1	Dep. on previous M1
		6	



Question	Answer		Marks	Guidance
5	Angle $AOC = \frac{6}{5}$ or 1.2		M1	Allow 68.8°. Allow $\frac{5}{6}$
	$AB = 5 \times \tan(their 1.2)$ OR by e.g. Sine Rule	Expect 12.86	DM1	$OR OB = \frac{5}{\cos their 1.2}$. Expect 13.80
	Area $\triangle OAB = \frac{1}{2} \times 5 \times their 12.86$	Expect 32.15	DM1	OR $\frac{1}{2} \times 5 \times their \ OB \times sin \ their \ 1.2$
	Area sector $\frac{1}{2} \times 5^2 \times their 1.2$	Expect 15	DM1	All DM marks are dependent on the first M1
	Shaded region = $32.15 - 15 = 17.2$		A1	Allow degrees used appropriately throughout. 17.25 scores A0
			5	

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Question	Answer	Marks	Guidance	
6(i)	Gradient, m, of $AB = \frac{3k+5-(k+3)}{k+3-(-3k-1)}$ OE $\left(=\frac{2k+2}{4k+4}\right) = \frac{1}{2}$	M1A1	Condone omission of brackets for M mark	
		2		
6(ii)	Mid-pt = $\left[\frac{1}{2}(-3k-1+k+3), \frac{1}{2}(3k+5+k+3)\right] =$	B1B1	B1 for $\frac{-2k+2}{2}$, B1 for $\frac{4k+8}{2}$ (ISW) or better, i.e. $\left(-k+1, 2k+4\right)$	
	$\left(\frac{-2k+2}{2}, \frac{4k+8}{2}\right) \text{ SOI}$			
	Gradient of perpendicular bisector is $\frac{-1}{their \ m}$ SOI Expect -2	M1	Could appear in subsequent equation and/or could be in terms of <i>k</i>	
	Equation: $y - (2k + 4) = -2[x - (-k + 1)]$ OE	DM1	Through <i>their</i> mid-point and with <i>their</i> $\frac{-1}{m}$ (now numerical)	
	y + 2x = 6	A1	Use of numerical k in (ii) throughout scores SC2/5 for correct answer	
		5		

Question	Answer	Marks	Guidance
7(a)(i)	$\frac{\tan^2\theta - 1}{\tan^2\theta + 1} = \frac{\frac{\sin\theta^2}{\cos\theta^2} - 1}{\frac{\sin\theta^2}{\cos\theta^2} + 1}$	M1	
	$= \frac{\sin \theta^2 - \cos \theta^2}{\sin \theta^2 + \cos \theta^2}$	A1	multiplying by $\cos \theta^2$ Intermediate stage can be omitted by multiplying directly by $\cos \theta^2$
	$= \sin \theta^2 - \cos \theta^2 = \sin \theta^2 - (1 - \sin \theta^2) = 2\sin^2 \theta - 1$	A1	Using $\sin \theta^2 + \cos \theta^2 = 1$ twice. Accept $a = 2$, $b = -1$
	ALT 1 $\frac{\sec^2\theta - 2}{\sec^2\theta}$	M1	ALT 2 $\frac{\tan^2 \theta - 1}{\sec^2 \theta}$
	$1 - \frac{2}{\sec^2 \theta} = 1 - 2\cos^2 \theta$	A1	$(\tan^2\theta - 1)\cos^2\theta$
	$1 - 2\left(1 - \sin^2\theta\right) = 2\sin^2\theta - 1$	A1	$\sin^2\theta - \cos^2\theta = \sin^2\theta - (1 - \sin^2\theta) = 2\sin^2\theta - 1$
		3	
7(a)(ii)	$2\sin^2\theta - 1 = \frac{1}{4} \rightarrow \sin\theta = (\pm)\sqrt{\frac{5}{8}} \text{ or } (\pm)0.7906$	M1	OR $\frac{t^2 - 1}{t^2 + 1} = \frac{1}{4} \rightarrow 3t^2 = 5 \rightarrow t = (\pm)\sqrt{\frac{5}{3}}$ or $t = (\pm)1.2910$
	$\theta = -52.2$	A1	
		2	

Question	Answer	Marks	Guidance
7(b)(i)	$\sin x = 2\cos x \to \tan x = 2$	M1	Or $\sin x = \sqrt{\frac{4}{5}}$ or $\cos x = \sqrt{\frac{1}{5}}$
	x = 1.11 with no additional solutions	A1	Accept 0.352π or 0.353π . Accept in co-ord form ignoring y co-ord
		2	
7(b)(ii)	Negative answer in range $-1 < y < -0.8$	B1	
	-0.894 or -0.895 or -0.896	B1	
		2	

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Question	Answer	Marks	Guidance	
8(i)	$\frac{\mathrm{d}y}{\mathrm{d}x} = 3x^2 - 18x + 24$	M1A1	Attempt to differentiate. All correct for A mark	
	$3x^2 - 18x + 24 = -3$	M1	Equate their $\frac{dy}{dx}$ to -3	
	x = 3	A1		
	y = 6	A1		
	y-6=-3(x-3)	A1FT	FT on their A. Expect $y = -3x + 15$	
		6		
8(ii)	(3)(x-2)(x-4) SOI or $x=2$, 4 Allow $(3)(x+2)(x+4)$	M1	Attempt to factorise or solve. Ignore a RHS, e.g. = 0 or > 0, etc.	
	Smallest value of <i>k</i> is 4	A1	Allow $k \ge 4$. Allow $k = 4$. Must be in terms of k	
		2		

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Question	Answer	Marks	Guidance		
9(i)	$\mathbf{OE} = \frac{2}{10} (8\mathbf{i} + 6\mathbf{j}) = 1.6\mathbf{i} + 1.2\mathbf{j}$ AG	M1A1	Evidence of $OB = 10$ or other valid method (e.g. trigonometry) is required		
		2			
9(ii)	$\mathbf{OD} = 1.6i + 1.2j + 7k$	B1	Allow reversal of one or both of OD , BD .		
	$\mathbf{BD} = -8\mathbf{i} - 6\mathbf{j} + 1.6\mathbf{i} + 1.2\mathbf{j} + 7\mathbf{k} \text{ OE} = -6.4\mathbf{i} - 4.8\mathbf{j} + 7\mathbf{k}$	M1A1	For M mark allow sign errors. Also if 2 out of 3 components correct		
	Correct method for \pm OD. \pm BD (using <i>their</i> answers)	M1	Expect $1.6 \times -6.4 + 1.2 \times -4.8 + 49 = 33$ or $\frac{825}{25} 825 / 25$.		
	Correct method for OD or BD (using <i>their</i> answers)	M1	Expect $\sqrt{1.6^2 + 1.2^2 + 7^2}$ or $\sqrt{6.4^2 + 4.8^2 + 7^2} = \sqrt{53}$ or $\sqrt{113}$		
	$\cos BDO = their \frac{\mathbf{OD.BD}}{ \mathbf{OD} \times \mathbf{BD} }$	DM1	Expect $\frac{33}{77.4}$. Dep. on all previous M marks and either B1 or A1		
	64.8° Allow 1.13(rad)	A1	Can't score A1 if 1 vector only is reversed unless explained well		
		7			

Question	Answer	Marks	Guidance
10(i)	Smallest value of c is 2. Accept 2, $c = 2$, $c \ge 2$. Not in terms of x	B1	Ignore superfluous working, e.g. $\frac{d^2y}{dx^2} = 2$
		1	
10(ii)	$y = (x-2)^2 + 2 \rightarrow x - 2 = (\pm)\sqrt{y-2} \rightarrow x = (\pm)\sqrt{y-2} + 2$	M1	Order of operations correct. Allow sign errors
	$f^{-1}(x) = \sqrt{x-2} + 2$	A1	$Accept y = \sqrt{x-2} + 2$
	Domain of f^{-1} is $x \ge 6$. Allow ≥ 6 .	B1	Not $f^{-1}(x) \ge 6$. Not $f(x) \ge 6$. Not $y \ge 6$
		3	
10(iii)	$[(x-2)^{2} + 2 - 2]^{2} + 2 = 51 \text{ SOI Allow 1 term missing for M mark}$ $Or (x^{2} - 4x + 6)^{2} - 4(x^{2} - 4x + 6) + 6 = 51$	M1A1	ALT. $f(x) = f^{-1}(51) (M1) = \sqrt{51-2} + 2 (A1)$
	$(x-2)^4 = 49$ or $(x^2 - 4x + 4)^2 = 49$ OR $x^4 - 8x^3 + 24x^2 - 32x - 33 = 0$ often implied by next line	A1	$(x-2)^2 + 2 = \sqrt{49} + 2 \text{ OR } f(x) = 9$
	$(x-2)^2 = (\pm)7$ OR $x^2 - 4x - 3 = 0$. Ignore $x^2 - 4x + 11 = 0$	A1	$(x-2)^2 = 7 \text{ OR } x = f^{-1}(9)$
	$x = 2 + \sqrt{7}$ only CAO $x = 2 + \sqrt[4]{49}$ scores 3/5	A1	$x = 2 + \sqrt{7}$
		5	

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Question	Answer	Marks	Guidance
11(i)	$\frac{dy}{dx} = 2(x+1) - (x+1)^{-2}$	B 1	
	Set = 0 and obtain $2(x+1)^3 = 1$ convincingly www AG	B1	
	$\frac{d^2 y}{dx^2} = 2 + 2(x+1)^{-3} \text{ www}$	B1	
	Sub, e.g., $(x+1)^{-3} = 2$ OE or $x = \left(\frac{1}{2}\right)^{\frac{1}{3}} - 1$	M1	Requires <u>exact</u> method – otherwise scores M0
	$\frac{d^2y}{dx^2} = 6$ CAO www	A1	and exact answer – otherwise scores A0
		5	

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Question	Answer	Marks	Guidance
11(ii)	$y^2 = (x+1)^4 + (x+1)^{-2} + 2(x+1)$ SOI	B1	OR $y^2 = (x^4 + 4x^3 + 6x^2 + 4x + 1) + (2x + 2) + (x + 1)^{-2}$
	$(\pi) \int y^2 dx = (\pi) \left[\frac{(x+1)^5}{5} \right] + \left[\frac{(x+1)^{-1}}{-1} \right] + \left[\frac{2(x+1)^2}{2} \right]$ $OR(\pi) \left[\frac{x^5}{5} + x^4 + 2x^3 + 2x^2 + x \right] + \left[x^2 + 2x \right] + \left[-\frac{1}{x+1} \right]$	B1B1B1	Attempt to integrate y^2 . Last term might appear as $(x^2 + 2x)$
	$(\pi) \left[\frac{32}{5} - \frac{1}{2} + 4 - \left(\frac{1}{5} - 1 + 1 \right) \right]$	M1	Substitute limits $0 \rightarrow 1$ into an attempted integration of y^2 . Do not condone omission of value when $x = 0$
	$9.7\pi \text{ or } 30.5$	A1	Note: omission of $2(x+1)$ in first line $\rightarrow 6.7\pi$ scores $3/6$ Ignore initially an extra volume, e.g. $(\pi) \int (4\frac{1}{2})^2$. Only take into account for the final answer
		6	

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