



UNIVERSITY OF CAMBRIDGE INTERNATIONAL EXAMINATIONS
General Certificate of Education
Advanced Subsidiary Level and Advanced Level

MATHEMATICS

9709/13

Paper 1 Pure Mathematics 1 (P1)

May/June 2013

1 hour 45 minutes

Additional Materials: Answer Booklet/Paper
Graph Paper
List of Formulae (MF9)

* 9 3 9 6 3 4 5 3 6 7 *

READ THESE INSTRUCTIONS FIRST

If you have been given an Answer Booklet, follow the instructions on the front cover of the Booklet.
Write your Centre number, candidate number and name on all the work you hand in.
Write in dark blue or black pen.
You may use a soft pencil for any diagrams or graphs.
Do not use staples, paper clips, highlighters, glue or correction fluid.

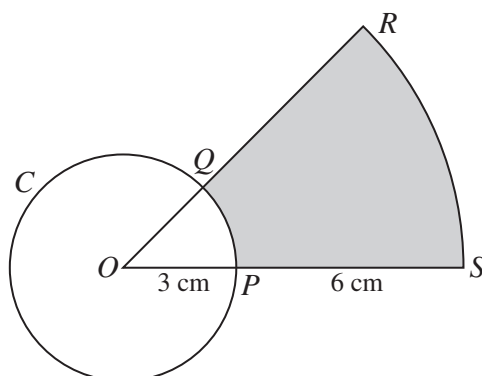
Answer **all** the questions.
Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place in the case of angles in degrees, unless a different level of accuracy is specified in the question.
The use of an electronic calculator is expected, where appropriate.
You are reminded of the need for clear presentation in your answers.

At the end of the examination, fasten all your work securely together.
The number of marks is given in brackets [] at the end of each question or part question.
The total number of marks for this paper is 75.
Questions carrying smaller numbers of marks are printed earlier in the paper, and questions carrying larger numbers of marks later in the paper.

This document consists of **4** printed pages.

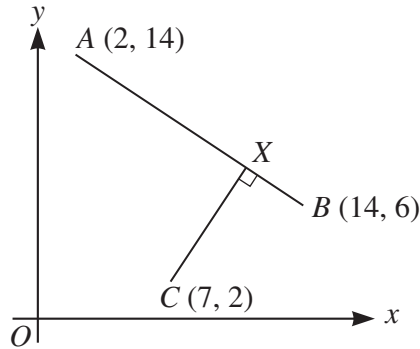
- 1 A curve is such that $\frac{dy}{dx} = \sqrt{(2x + 5)}$ and $(2, 5)$ is a point on the curve. Find the equation of the curve. [4]

2



- The diagram shows a circle C with centre O and radius 3 cm. The radii OP and OQ are extended to S and R respectively so that ORS is a sector of a circle with centre O . Given that $PS = 6$ cm and that the area of the shaded region is equal to the area of circle C ,
- (i) show that angle $POQ = \frac{1}{4}\pi$ radians, [3]
- (ii) find the perimeter of the shaded region. [2]
- 3 (i) Express the equation $2 \cos^2 \theta = \tan^2 \theta$ as a quadratic equation in $\cos^2 \theta$. [2]
- (ii) Solve the equation $2 \cos^2 \theta = \tan^2 \theta$ for $0 \leq \theta \leq \pi$, giving solutions in terms of π . [3]
- 4 (i) Find the first three terms in the expansion of $(2 + ax)^5$ in ascending powers of x . [3]
- (ii) Given that the coefficient of x^2 in the expansion of $(1 + 2x)(2 + ax)^5$ is 240 , find the possible values of a . [3]
- 5 (i) Sketch, on the same diagram, the curves $y = \sin 2x$ and $y = \cos x - 1$ for $0 \leq x \leq 2\pi$. [4]
- (ii) Hence state the number of solutions, in the interval $0 \leq x \leq 2\pi$, of the equations
- (a) $2 \sin 2x + 1 = 0$, [1]
- (b) $\sin 2x - \cos x + 1 = 0$. [1]
- 6 The non-zero variables x , y and u are such that $u = x^2y$. Given that $y + 3x = 9$, find the stationary value of u and determine whether this is a maximum or a minimum value. [7]

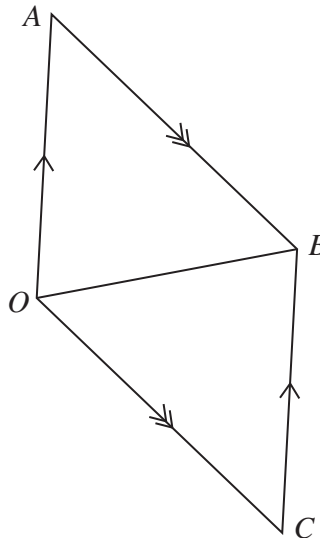
7



The diagram shows three points $A(2, 14)$, $B(14, 6)$ and $C(7, 2)$. The point X lies on AB , and CX is perpendicular to AB . Find, by calculation,

- (i) the coordinates of X , [6]
- (ii) the ratio $AX : XB$. [2]

8



The diagram shows a parallelogram $OABC$ in which

$$\vec{OA} = \begin{pmatrix} 3 \\ 3 \\ -4 \end{pmatrix} \quad \text{and} \quad \vec{OB} = \begin{pmatrix} 5 \\ 0 \\ 2 \end{pmatrix}.$$

- (i) Use a scalar product to find angle BOC . [6]
 - (ii) Find a vector which has magnitude 35 and is parallel to the vector \vec{OC} . [2]
- 9
- (a) In an arithmetic progression, the sum, S_n , of the first n terms is given by $S_n = 2n^2 + 8n$. Find the first term and the common difference of the progression. [3]
 - (b) The first 2 terms of a geometric progression are 64 and 48 respectively. The first 3 terms of the geometric progression are also the 1st term, the 9th term and the n th term respectively of an arithmetic progression. Find the value of n . [5]

10 The function f is defined by $f : x \mapsto 2x + k$, $x \in \mathbb{R}$, where k is a constant.

(i) In the case where $k = 3$, solve the equation $ff(x) = 25$. [2]

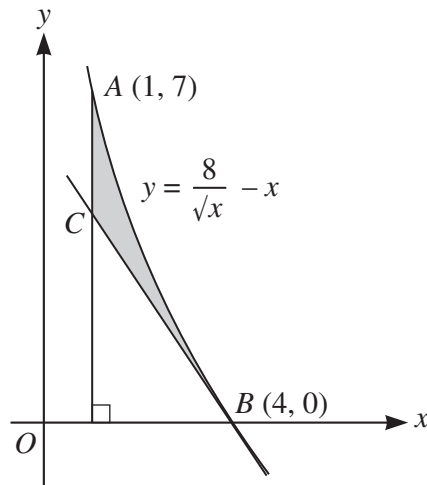
The function g is defined by $g : x \mapsto x^2 - 6x + 8$, $x \in \mathbb{R}$.

(ii) Find the set of values of k for which the equation $f(x) = g(x)$ has no real solutions. [3]

The function h is defined by $h : x \mapsto x^2 - 6x + 8$, $x > 3$.

(iii) Find an expression for $h^{-1}(x)$. [4]

11



The diagram shows part of the curve $y = \frac{8}{\sqrt{x}} - x$ and points $A(1, 7)$ and $B(4, 0)$ which lie on the curve. The tangent to the curve at B intersects the line $x = 1$ at the point C .

(i) Find the coordinates of C . [4]

(ii) Find the area of the shaded region. [5]