



**Cambridge International Examinations**  
Cambridge International Advanced Subsidiary and Advanced Level

CANDIDATE NAME

CENTRE NUMBER

CANDIDATE NUMBER

\* 0 1 2 3 4 5 6 7 8 9 \*

**MATHEMATICS**

**9709/01**

Paper 1 Pure Mathematics 1 (P1)

**For Examination from 2017**

SPECIMEN PAPER

**1 hour 45 minutes**

Candidates answer on the Question Paper.

Additional Materials: List of Formulae (MF9)

**READ THESE INSTRUCTIONS FIRST**

Write your Centre number, candidate number and name in the spaces at the top of this page.

Write in dark blue or black pen.

You may use an HB pencil for any diagrams or graphs.

Do not use staples, paper clips, glue or correction fluid.

DO **NOT** WRITE IN ANY BARCODES.

Answer **all** the questions.

Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place in the case of angles in degrees, unless a different level of accuracy is specified in the question.

The use of an electronic calculator is expected, where appropriate.

You are reminded of the need for clear presentation in your answers.

At the end of the examination, fasten all your work securely together.

The number of marks is given in brackets [ ] at the end of each question or part question.

The total number of marks for this paper is 75.

This document consists of **19** printed pages and **1** blank page.

- 1 In the expansion of  $\left(1 - \frac{2x}{a}\right)(a+x)^5$ , where  $a$  is a non-zero constant, show that the coefficient of  $x$  is zero. [3]

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- 2 The function  $f$  is such that  $f'(x) = 3x^2 - 7$  and  $f(3) = 5$ . Find  $f(x)$ . [3]

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3 Solve the equation  $\sin^{-1}(4x^4 + x^2) = \frac{1}{6}\pi$ .

[4]





(ii) Hence solve the equation  $\frac{4 \cos \theta}{\tan \theta} + 15 = 0$  for  $0^\circ \leq \theta \leq 360^\circ$ .

[3]

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5 A curve has equation  $y = \frac{8}{x} + 2x$ .

(i) Find  $\frac{dy}{dx}$  and  $\frac{d^2y}{dx^2}$ .

[3]

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(ii) Find the coordinates of the stationary points and state, with a reason, the nature of each stationary point. [5]

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6 A curve has equation  $y = x^2 - x + 3$  and a line has equation  $y = 3x + a$ , where  $a$  is a constant.

- (i) Show that the  $x$ -coordinates of the points of intersection of the line and the curve are given by the equation  $x^2 - 4x + (3 - a) = 0$ . [1]

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- (ii) For the case where the line intersects the curve at two points, it is given that the  $x$ -coordinate of one of the points of intersection is  $-1$ . Find the  $x$ -coordinate of the other point of intersection. [2]

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(iii) For the case where the line is a tangent to the curve at a point  $P$ , find the value of  $a$  and the coordinates of  $P$ . [4]

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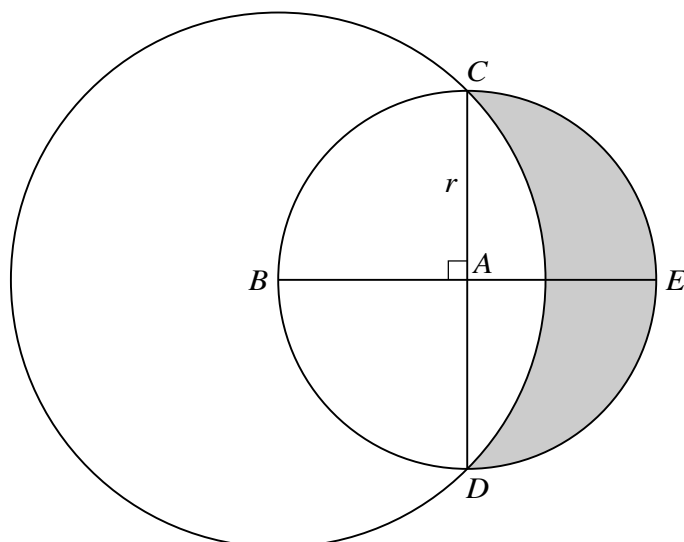
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The diagram shows a circle with centre  $A$  and radius  $r$ . Diameters  $CAD$  and  $BAE$  are perpendicular to each other. A larger circle has centre  $B$  and passes through  $C$  and  $D$ .

- (i) Show that the radius of the larger circle is  $r\sqrt{2}$ . [1]

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- (ii) Find the area of the shaded region in terms of  $r$ . [6]

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A series of horizontal dotted lines for writing, spanning the width of the page.







9 (i) Express  $-x^2 + 6x - 5$  in the form  $a(x + b)^2 + c$ , where  $a$ ,  $b$  and  $c$  are constants. [3]

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The function  $f : x \mapsto -x^2 + 6x - 5$  is defined for  $x \geq m$ , where  $m$  is a constant.

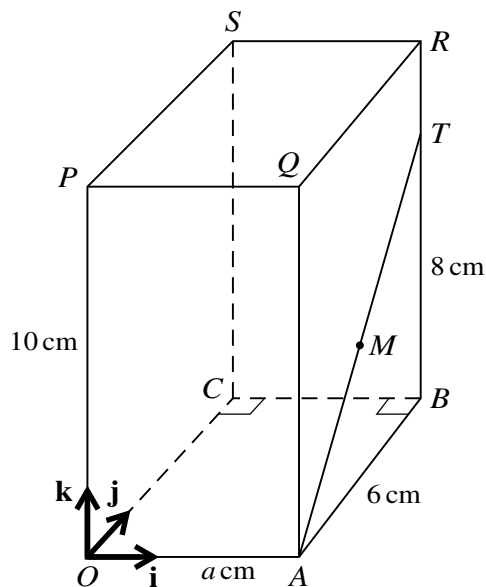
(ii) State the smallest value of  $m$  for which  $f$  is one-one. [1]

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(iii) For the case where  $m = 5$ , find an expression for  $f^{-1}(x)$  and state the domain of  $f^{-1}$ . [4]

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The diagram shows a cuboid  $OABCPQRS$  with a horizontal base  $OABC$  in which  $AB = 6$  cm and  $OA = a$  cm, where  $a$  is a constant. The height  $OP$  of the cuboid is 10 cm. The point  $T$  on  $BR$  is such that  $BT = 8$  cm, and  $M$  is the mid-point of  $AT$ . Unit vectors  $\mathbf{i}$ ,  $\mathbf{j}$  and  $\mathbf{k}$  are parallel to  $OA$ ,  $OC$  and  $OP$  respectively.

- (i) For the case where  $a = 2$ , find the unit vector in the direction of  $\overrightarrow{PM}$ . [4]

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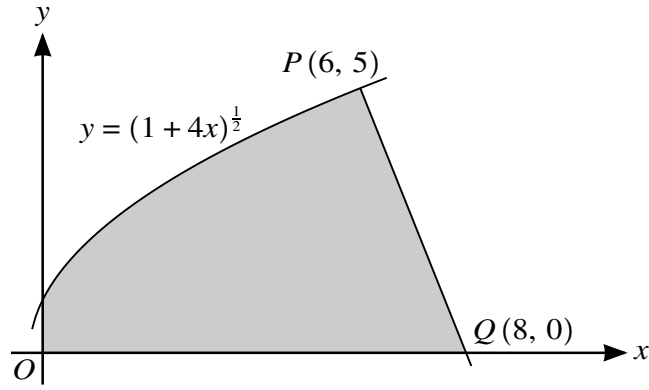
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The diagram shows part of the curve  $y = (1 + 4x)^{\frac{1}{2}}$  and a point  $P(6, 5)$  lying on the curve. The line  $PQ$  intersects the  $x$ -axis at  $Q(8, 0)$ .

(i) Show that  $PQ$  is a normal to the curve. [5]

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- (ii) Find, showing all necessary working, the exact volume of revolution obtained when the shaded region is rotated through 360 degrees about the x-axis. [7]

[In part (ii) you may find it useful to apply the fact that the volume, V, of a cone of base radius r and vertical height h, is given by V = 1/3 \* pi \* r^2 \* h.]

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