

Cambridge Assessment International Education Cambridge International Advanced Level



9231/21 October/November 2017

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Paper 2 MARK SCHEME Maximum Mark: 100

Published

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

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# Cambridge International A Level – Mark Scheme **PUBLISHED**



#### Mark Scheme Notes

Marks are of the following three types:

- M Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the M mark and in some cases an M mark can be implied from a correct answer.
- A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).
- B Mark for a correct result or statement independent of method marks.
- When a part of a question has two or more "method" steps, the M marks are generally independent unless the scheme specifically says otherwise; and similarly when there are several B marks allocated. The notation DM or DB (or dep\*) is used to indicate that a particular M or B mark is dependent on an earlier M or B (asterisked) mark in the scheme. When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.
- The symbol FT implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A or B marks are given for correct work only. A and B marks are not given for fortuitously "correct" answers or results obtained from incorrect working.
  - Note: B2 or A2 means that the candidate can earn 2 or 0. B2/1/0 means that the candidate can earn anything from 0 to 2.

The marks indicated in the scheme may not be subdivided. If there is genuine doubt whether a candidate has earned a mark, allow the candidate the benefit of the doubt. Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored.

- Wrong or missing units in an answer should not lead to the loss of a mark unless the scheme specifically indicates otherwise.
- For a numerical answer, allow the A or B mark if a value is obtained which is correct to 3 s.f., or which would be correct to 3 s.f. if rounded (1 d.p. in the case of an angle). As stated above, an A or B mark is not given if a correct numerical answer arises fortuitously from incorrect working. For Mechanics questions, allow A or B marks for correct answers which arise from taking *g* equal to 9.8 or 9.81 instead of 10.

The following abbreviations may be used in a mark scheme or used on the scripts:

- AEF/OE Any Equivalent Form (of answer is equally acceptable) / Or Equivalent
- October/No. Mymainscioud.com AG Answer Given on the guestion paper (so extra checking is needed to ensure that the detailed working leading to the result is valid)
- CAO Correct Answer Only (emphasising that no "follow through" from a previous error is allowed)
- CWO Correct Working Only – often written by a 'fortuitous' answer
- ISW Ignore Subsequent Working
- SOI Seen or implied
- SR Special Ruling (detailing the mark to be given for a specific wrong solution, or a case where some standard marking practice is to be varied in the light of a particular circumstance)

#### **Penalties**

- MR –1 A penalty of MR –1 is deducted from A or B marks when the data of a question or part question are genuinely misread and the object and difficulty of the question remain unaltered. In this case all A and B marks then become "follow through" marks. MR is not applied when the candidate misreads his own figures – this is regarded as an error in accuracy. An MR –2 penalty may be applied in particular cases if agreed at the coordination meeting.
- PA –1 This is deducted from A or B marks in the case of premature approximation. The PA –1 penalty is usually discussed at the meeting.

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Question	Answer	Marks	Guidance	TINSCIO.
1	-p+2t=0, p=4	M1 A1	Find <i>p</i> by equating transverse acceln. to 0 at $t = 2$	JUC COM
	$a_R = (8 - pt + t^2)^2 / 0.8$	M1	Find radial acceleration $a_R$ at $t = 2$ in terms of p from $v^2/r$	"
	$=4^2/0.8=20 \text{ [m s}^{-2}\text{]}$	A1	Evaluate with $p = 4$	
		4		

Question	Answer		Marks	Guidance
2	$(3\pi/5)^2 = \omega^2 (a^2 - (a - 1 \cdot 6)^2)$	(AEF)	M1 A1	Use $v^2 = \omega^2 (a^2 - x^2)$ in each posn. (M1 for either)
	$(\pi/4)^2 = \omega^2 (a^2 - (a - 0.2)^2) (3\pi/5)^2 (0.4a - 0.04) = (\pi/4)^2 (3.2a - 2.56)$		A1	Combine to find amplitude <i>a</i> and $\omega^2$ (or $\omega$ )
	a = 2.6  [m]		M1 A1	(M1 for either)
	$\omega^2 = (\pi/4)^2 \text{ or } \omega = \pi/4$	(AEF)	A1	Find other unknown
	$T = 2\pi / (\pi/4) = 8 [s]$		B1FT	Find period T from $T = 2\pi/\omega$ ( $\sqrt{\text{ on } \omega^2 \text{ or } \omega}$ )
			7	

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Question	Answer	Marks	Guidance
3(i)	$mv_A + kmv_B = 2mu + kmu$ $[v_A + kv_B = 2u + ku]$ (AEF)	M1	Scheme October/No. M.M. M.M. M.M. M.M. M.M. M.M. M.M. M
	$v_B - v_A = \frac{1}{2} (2u - u) [= \frac{1}{2} u]$	M1	Use Newton's restitution law with consistent LHS signs
	$v_B = u (2k+5) / 2(k+1) \text{ or } u (k+5/2) / (k+1)$ (AEF)	A1	Combine to find $v_B$
	$[v_A = u (k+4) / 2(k+1)] v_B > 4u/3 \text{ if } k < 7/2$	M1 A1	Find inequality for $k$ from speeds of $B$ and $C$ after 1st collision
		5	
3(ii)	$kmw_B + mv_C = kmv_B + m(4u/3) $ $[2w_B + v_C = 2(3u/2) + 4u/3 $ $= 13u/3 \text{ when } k = 2]$ (AEF)	M1	Use conservation of momentum for <i>B</i> & <i>C</i>
	$v_C - w_B = \frac{1}{2} (v_B - 4u/3) [= u/12]$ (k + 1) w_B = (k - \frac{1}{2}) v_B + 2u	M1	Use Newton's restitution law with consistent LHS signs Combine to find $w_B$
	3 $w_B = (3/2) v_B + 2u$ with $v_B = 3u/2$ , so $w_B = 17u/12$	*A1	when $k = 2$
	$v_A = u, v_A < w_B$	DB1	Verify no further collisions between <i>A</i> and <i>B</i>
	<i>EITHER:</i> $(k + 1) v_C = (3k/2) v_B + (2 - k) (2u/3)$ 3 $v_C = 3 v_B$ with $v_B = 3u/2$ so $v_C = 3u/2 > w_B$	(DB1)	<i>EITHER:</i> Find $v_C$ and verify no further collisions between <i>B</i> and <i>C</i>
	OR: B and C cannot meet again since they move apart after colliding (AEF)	(DB1)	<i>OR:</i> State explicitly that no further collisions between <i>B</i> and <i>C</i>
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Question	Answer	Marks	Guidance
4(i)	$T \times 2a = (5W/2) \times a \cos \theta$	M1	Guidance Take moments for rod about A
	$T = \frac{1}{2} (5W/2) \times (4/5) = W$	A1	to find tension T
		2	
4(ii)	$T\sin\theta = \mu \left(W + T\cos\theta\right)$	M1	Use $F_P = \mu R_P$ at $P$
	$(3/5) W = \mu (1 + 4/5)W = \mu (9/5)W, \ \mu = 1/3$	A1	to find $\mu$
		2	
4(iii)	EITHER: $[\pm] X = T \sin \theta = 3W/5 \text{ or } 0.6W$ $[\pm] Y = 5W/2 - T \cos \theta \text{ or } 5W/2 + W - R_P$	(B1	<i>EITHER:</i> Find horizontal component <i>X</i> of force at <i>A</i> Find vertical component <i>Y</i> of force at <i>A</i>
	= 17W/10  or  1.7W	B1)	
	<i>OR:</i> $[\pm] X = (5W/2) \sin \theta = 3W/2 \text{ or } 1.5W$	(B1	<i>OR:</i> Find component <i>X</i> of force at <i>A</i> along <i>BA</i>
	$[\pm] Y = (5W/2) \cos \theta - T = W$	B1)	Find component <i>Y</i> of force at <i>A</i> perp. to <i>BA</i>
	$R_A^2 = X^2 + Y^2 = 13W^2/4, R_A = \frac{1}{2}W\sqrt{13} \text{ or } 1.80 W$	B1FT	Find magnitude of resultant force $R_A$ at A (FT on X, Y)
		3	
4(iv)	$PB = (a + 2a \sin \theta) / \cos \theta = 5a/4 + 3a/2 = 11a/4 \text{ or } 2.75a$ or $x = 3a/4 \text{ or } 0.75a$	B1	Find length <i>PB or</i> extension <i>x</i> of string
	$T = \lambda (PB - 2a)/2a, \ \lambda = 8W/3 \text{ or } 2.67W$	M1 A1	Find modulus $\lambda$ using Hooke's Law
		3	

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Question	Answer	Marks	Guidance		
5(i)	$A_{ABCD} = 24a^2, A_{EFGH} = 8a^2, A_{Frame} = 16a^2$ $M_{ABCD} = 3m/2 \text{ and } m_{EFGH} = m/2$	B1	Scheme October/No		
	$I_{ABCD} = \frac{1}{3} M_{ABCD} ((3a)^2 + (2a)^2)  [= (13/3) M_{ABCD} a^2 = (13/2) ma^2]$	B1			
	$I_{EFGH} = \frac{1}{3} m_{EFGH} ((2a)^2 + a^2)  [= (5/3) m_{EFGH} a^2 = (5/6) ma^2]$	B1	Find MI of <i>EFGH</i> about axis at centre <i>Q</i>		
	$\begin{bmatrix} I_{ABCD} - I_{EFGH} + m \times (6a)^2 \ [= (121/2 - 113/6) \ ma^2 \\ or \ (17/3 + 36) \ ma^2 = (125/3) \ ma^2 ] \end{bmatrix}$	M1 A1	Find MI of frame about axis at <i>O</i> Result also follows from combining four rectangular parts		
	$I_{Object} = (11m/12) \times (4a)^2 \qquad [= (44/3) ma^2]$	B1	Find MI of small object about axis at O		
	$I = (13/2 - 5/6 + 36 + 44/3) ma^2 = (169/3) ma^2$ AG	A1	Combine to verify MI of system about axis at O		
		7			
5(ii)	$\begin{bmatrix} -] I d^{2}\theta/dt^{2} \text{ or } [-] I\alpha \\ = mg \times 6a \sin \theta + (11/12)mg \times 4a \sin \theta \\ \text{ or } (23/12)mg \times (116/23)a \sin \theta \\ [ = (29/3) mga \sin \theta ] \end{bmatrix}$	M1 A1	Use eqn of circular motion to relate $d^2\theta/dt^2$ to sin $\theta$ , where $\theta$ is angle of $QO$ with vertical		
	$d^{2}\theta/dt^{2} \text{ or } \alpha = -(29g / 169a) \theta$ $or - (0.172 g / a) \theta$	M1 A1	Approximate $\sin \theta$ by $\theta$ to show SHM ( <b>M0</b> if wrong sign or $\cos \theta \approx \theta$ used)		
	$T = 2\pi / \sqrt{(29g/169a)} = 26\pi \sqrt{(a/29g)} \text{ or } 15.2\sqrt{(a/g)} \text{ or } 4.80\sqrt{a} $ (AEF)	A1	Find period T from $T = 2\pi/\omega$ (A1 requires some simplification)		
		5			

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Question	Answer	Marks	Guidance	This Clou
6(i)	$p = (1/6)^2 \text{ or } 1/36$	B1	Find (or imply) probability $p$ of pair of sixes in one throw	Ud.Com
	1/p = 36	B1	Find mean value of X	"
6(ii)	$P(X=12) = p (1-p)^{11} = 0.0204$	M1 A1	Find prob. of needing exactly 12 throws	
6(iii)	$P(X > 12) = (1 - p)^{12} = 0.713$	M1 A1	Find prob. of needing more than 12 throws	
		2		

Question	Answer	Marks	Guidance
7(i)	$F(x) = \int f(x)  dx = -e^{-0.2x} + c = 1 - e^{-0.2x}  (x \ge 0)$	M1	State, or integrate and use $F(0) = 0$ or $F(x) \rightarrow 1$ as $x \rightarrow \infty$
	and $F(x) = 0$ ( $x < 0$ or otherwise)	A1	to find, $F(x)$ ( <b>A0</b> if case $x < 0$ omitted)
		2	
7(ii)	$P(X > 2) = 1 - F(2) = e^{-0.4} = 0.670$	M1 A1	Find $P(X > 2)$ : ( <b>M0</b> for F(2))
		3	
7(iii)	$1 - e^{-0.2m} = \frac{1}{2}, e^{0.2m} = 2$	M1	Find median value <i>m</i> from $F(m)$ or $1 - F(m) = \frac{1}{2}$
	$m = 5 \ln 2 \text{ or } 3.47$	M1 A1	
		3	

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9231/21	Cambrid	Scheme October/No. Mun. Mynatha Guidance State (at least) null hypothesis	42 1383		
Question	Answer		Marks	Guidance	SCIO
8	H <sub>0</sub> : No association <i>or</i> method is independent of gender	(AEF)	B1	State (at least) null hypothesis	SUU.COM
	$ \begin{array}{c} E_i: 9.0 \ 19.8 \ 31.2 \\ 6.0 \ 13.2 \ 20.8 \end{array} $		M1 A1	Find expected values $E_i$ (A0 if rounded to integers)	
	$\chi^{2} = 0.111 + 3.073 + 1.482 + 0.167 + 4.610 + 2.223 = 11.7 (or 12.3)$	(to 2 d.p.)	M1 A1	Find value of $\chi^2$ from $\Sigma (E_i - O_i)^2 / E_i$ [or $\Sigma O_i^2 / E_i - n$ ] (allow 12.3 if integer values of $E_i$ used)	
	$\chi_{2,0.99}^{2} = 9.21$		B1	State or use correct tabular $\chi^2$ value	
	Reject H <sub>0</sub> if $\chi^2$ > tabular value	(AEF)	M1	Valid method for reaching conclusion	
	$11.7 \pm 0.1 > 9.21$ so there is an association		A1	Correct conclusion, from correct values	
			8		

Question	Answer	Marks	Guidance
9(i)	$r = S_{xy} / \sqrt{(S_{xx}S_{yy})} \text{ with e.g.}$ $S_{xy} = 212.62 - 35.9 \times 36.8/8 = 47.48 \text{ (or } 5.935\text{)}$ $S_{xx} = 216.47 - 35.9^2/8 = 55.37 \text{ (or } 6.921\text{)}$ $S_{yy} = 244.96 - 36.8^2/8 = 75.68 \text{ (or } 9.46\text{) (all to } 3 \text{ s.f.)}$	M1 A1	Find correlation coefficient <i>r</i> (Insufficient working loses first <b>A1</b> )
	r = 0.733	*A1	
		3	

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October/No. Mymainscloud.com Marks Guidance Ouestion Answer State both hypotheses (**B0** for  $r \dots$ ) 9(ii)  $H_0: \rho = 0, H_1: \rho > 0$ **B1** State or use correct tabular one-tail *r*-value (\*B1 EITHER:  $r_{8.1\%} = 0.789$ M1) State or imply valid method for conclusion Accept  $H_0$  if |r| < tab. r-value (AEF)  $t_r = r\sqrt{((n-2)/(1-r^2))} = 2.64, t_{6.0.99} = 3.143$ (\*B1 OR: Accept  $H_0$  if  $|t_r| < tab. t$ -value (AEF) M1) No positive correlation (AEF) DA1 4 9(iii) M1 A1 Find *n<sub>min</sub>* from relevant two-tail tabular value[s]  $r_{14, 1\%} = 0.661, r_{15, 1\%} = 0.641$  so  $n_{min} = 15$ SC: Award **B1** for stating 15 without any justification 2

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Question	Answer	UBLISHED	Guidance
10(i)	$\overline{x} = 0.91, \ \overline{y} = 1.205$ $s_X^2 = 19.56 / 49 \ [= 489/1225 \ or \ 0.3992] \ and$ $s_Y^2 = 30.25 / 59 \ [= 121/236 \ or \ 0.5127]$	B1 M1	Scheme October/No. WWW. The Control of the Control
	<i>EITHER:</i> $s^2 = s_X^2 / 50 + s_Y^2 / 60$	(M1	Estimate or imply combined variance
	$= 0.01653 \text{ or } 0.1286^2$ (to 3 s.f. throughout)	A1	
	$[\pm] (\overline{y} - \overline{x}) \pm z s$	M1	Find confidence interval for difference $Y - X \text{ or } X - Y$
	$z_{0.95} = 1.645$ [±] 0.295 ± 0.211 (allow 0.212)	A1	Use appropriate tabular value Evaluate confidence interval (either form)
	<i>or</i> [±] [0.084, 0.506] (allow [±] [0.083, 0.507])	A1)	
	<i>OR:</i> Assume equal [population] variances $s^2 = (49 s_x^2 + 59 s_y^2) / 108$ <i>or</i> (19.56 + 30.25) / 108	(B1	State assumption Find or imply pooled estimate of common variance (note $s_X^2$ and $s_Y^2$ not needed explicitly so first M1 may be implied by result)
	$= 4981/10800 \text{ or } 0.461 \text{ or } 0.679^2$	B1	
	$[\pm](\overline{y} - \overline{x}) \pm z  s  \sqrt{(1/50 + 1/60)}$	M1	Find confidence interval for difference $Y - X \text{ or } X - Y$
	$z_{0.95} = 1.645$	A1	Use appropriate tabular <i>z</i> -value (or <i>t</i> -value from calculator)
	[±] 0·295 ± 0·214 or [±] [0·081, 0·509]	A1)	Evaluate confidence interval (either form)
		7	

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Question	Answer	Marks	Guidance	N <sub>SCIO</sub>	
10(ii)	$z = (1 \cdot 205 - 0 \cdot 91) / s = 0 \cdot 295 / s$ = 2 \cdot 29[4] [or 2 \cdot 26[9]] (to 3 s.f.)	M1 A1	Find value of z (either sign)	ASCIOUD.COM	
	(z) = 0.989[1]  [or  0.988[4]]	A1	Find $\Phi(z)$		
	$100 \times (1 - 0.989) \times 2 = 2.2 \text{ [or } 2.3 \text{]}$ (to 1 d.p.)	M1 A1	Find limiting value for $\alpha$ , based on two-tail test ( <b>M0</b> for basing on one-tail test)		
	$\alpha < (or \leqslant) 2 \cdot 2 \text{ [or } 2 \cdot 3 \text{]}$	A1	Find set of possible values of $\alpha$ (Treat $\alpha$ instead of $\alpha$ % as misread)		
		6			

Question	Answer	Marks	Guidance
11A(i)	$\frac{1}{2}mv^2 = \frac{1}{2}mu^2 - mga\left(\cos\alpha + \cos\beta\right)$	M1 A1	Find $v^2$ at A' from conservation of energy (A0 if no m)
	$mv^{2}/a = mg \cos \beta$ $u^{2} = ag \cos \beta + 2ag (1/16 + \cos \beta)$	B1	Use $F = ma$ radially at A' with $R_{A'} = 0$ Use $\cos \alpha = 1/16$ and eliminate $v^2$ to verify $u^2$
	$= (1/8) ag (1 + 24 \cos \beta)$ AG	M1 A1	
		5	

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Question	Answer	Marks	Guidance
11A(ii)	$\frac{1}{2}mw^2 = \frac{1}{2}mu^2 - mga(1 + \cos 2\beta)$	B1	Guidance       Refuse         Find $w^2$ at $B'$ from conservation of energy ( <b>B0</b> if no $m$ )
	$mw^{2}/a = mg \cos 2\beta$ $u^{2} = ag \cos 2\beta + 2ag (1 + \cos 2\beta)$	B1	Use $F = ma$ radially at B' with $R_{B'} = 0$ Eliminate $w^2$ to find $u^2$
	$= ag\left(2 + 3\cos 2\beta\right)$	M1	
	$1 + 24 \cos \beta = 8 (2 + 3 \cos 2\beta)$ = 16 + 48 cos <sup>2</sup> \beta - 24 16 cos <sup>2</sup> \beta - 8 cos \beta - 3 = 0	M1	Combine eqns for $u^2$ Formulate and solve quadratic to find $\cos \beta$
	$\cos\beta = \frac{3}{4} [rejecting - \frac{1}{4}]$	M1 A1	
		6	
11A(iii)	$u^{2} = (19/8) ag or 2.375 ag$ $R = mu^{2}/a + mg \cos \alpha$ = (19/8 + 1/16) mg	B1	Find $u^2$ using value of $\cos \beta$ Use $F = ma$ radially at A to find reaction R at A
	= (39/16) mg  or  2.44 mg	M1 A1	
		3	

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Question	Answer	Marks	Guidance
11B(i)	e.g. $S_{xy} = 218.72 - 45.3 \times 40.5/9 = 14.87 \text{ or } 1.652$ $S_{xx} = 245.59 - 45.3^2/9 = 17.58 \text{ or } 1.953$ or $S_{yy} = 195.11 - 40.5^2/9 = 12.86 \text{ or } 1.429$		Find reqd. values
	<i>EITHER:</i> $b_1 = S_{xy} / S_{xx} = 14.87 / 17.58 = 0.84585 = 0.846$ $(y - 40.5/9) = b_1 (x - 45.3/9)$ (y - 4.5) = 0.846 (x - 5.033)	(M1 A1	Find gradient in $y - \overline{y} = b_1 (x - \overline{x})$ to 3 s.f. Find eqn. of regression line to 3 s.f.
	y = 0.846x + 0.24257 = 0.846x + 0.243	M1 A1	
	x = 4.68	A1)	Find x when $y = 4.2$
	<i>OR:</i> $b_2 = S_{xy} / S_{yy} = 14.87 / 12.86 = 1.1563 = 1.16$ $(x - 45.3/9) = b_2 (y - 40.5/9)$ (x - 5.033) = 1.16 (y - 4.5)	(M1 A1	Find gradient in $x - \overline{x} = b_2 (y - \overline{y})$ to 3 s.f. Find eqn. of regression line to 3 s.f.
	x = 1.16y - 0.170[04]	M1A1	
	x = 4.69	A1)	Find <i>x</i> when $y = 4.2$ ( <b>A0</b> for $x = 4.70$ )
		5	

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Question	Answer	Marks	Guidance     State hypotheses     (B0 for $\overline{x} \dots$ )	25
11B(ii)	H <sub>0</sub> : $\mu_x - \mu_y = 0.3$ , H <sub>1</sub> : $\mu_x - \mu_y > 0.3$ (AEF)	<b>B</b> 1	State hypotheses ( <b>B0</b> for $\overline{x}$ )	Y.COD
	$\overline{d} = 4.8 / 9 \text{ or } 8/15 \text{ or } 0.533$ (where $d = x - y$ )	B1	Find sample mean	
	$s^{2} = (3 \cdot 26 - 4 \cdot 8^{2}/9) / 8$ = 7/80 or 0.0875 or 0.296 <sup>2</sup>	M1 A1	Estimate population variance (allow biased here: $7/90 \text{ or } 0.0778 \text{ or } 0.279^2$ )	
	$t = (\bar{d} - 0.3) / (s/\sqrt{9}) = 2.37$	M1 A1	Find value of <i>t</i>	
	$t_{8,0.975} = 2.306 \text{ or } 2.31$	B1	State or use correct tabular <i>t</i> -value (or can compare $\overline{d}$ with $0.3 + t_{8, 0.975} \text{ s/}\sqrt{9} = 0.527$ )	
	Reject $H_0$ if $t >$ tabular value(AEF) $2.37 [\pm 0.1] > 2.31$ so accept belief	M1	Valid method for reaching conclusion Correct conclusion, from correct values	
	[of increase of more than 0.3] (AEF)	A1	SC: Wrong (hypothesis) test can earn only <b>B1</b> for hypotheses	
		9		